

Doubly Magic Nucleus ^{208}Pb

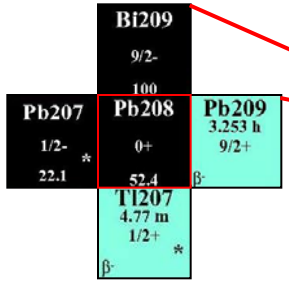
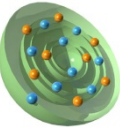


Table 1 -- Nuclear Shell Structure (from *Elementary Theory of Nuclear Shell Structure*, Maria Goeppert Mayer & J. Hans D. Jensen, John Wiley & Sons, Inc., New York, 1955.)

Angular Momentum (h Ω /2 π)	Spin-Orbit Coupling (1/2, 3/2, 5/2, 7/2, ...)	Number of Nucleons Shell	Total	Magic Number
7	1j	1j 15/2	16	[184] -- {184}
		3d 3/2	4	[168]
6	4s	4s 1/2	2	[164]
6	3d	2g 7/2	8	[162]
		1i 11/2	12	[154]
6	2g	3d 5/2	6	[142]
		2g 9/2	10	[136]
6	1i	1i 13/2	14	[126] -- {126}
		3p 1/2	2	[112]
5	3p	3p 3/2	4	[110]
		2f 5/2	6	[106]
5	2f	2f 7/2	8	[100]
		1h 9/2	10	[92]
5	1h	1h 11/2	12	[82] -- {82}
4	3s	3s 1/2	2	[70]
		2d 3/2	4	[68]
4	2d	2d 5/2	6	[64]
		1g 7/2	8	[58]
4	1g	1g 9/2	10	[50] -- {50}
3	2p	2p 1/2	2	[40] -- {40}
		1f 5/2	6	[38]
3	1f	2p 3/2	4	[32]
		1f 7/2	8	[28] -- {28}
2	2s	1d 3/2	4	[20] -- {20}
2	1d	2s 1/2	2	[16]
		1d 5/2	6	[14]
1	1p	1p 1/2	2	[8] -- {8}
		1p 3/2	4	[6]
0	1s	1s 1/2	2	[2] -- {2}



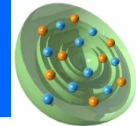
Maria Goeppert-Mayer



J. Hans D. Jensen

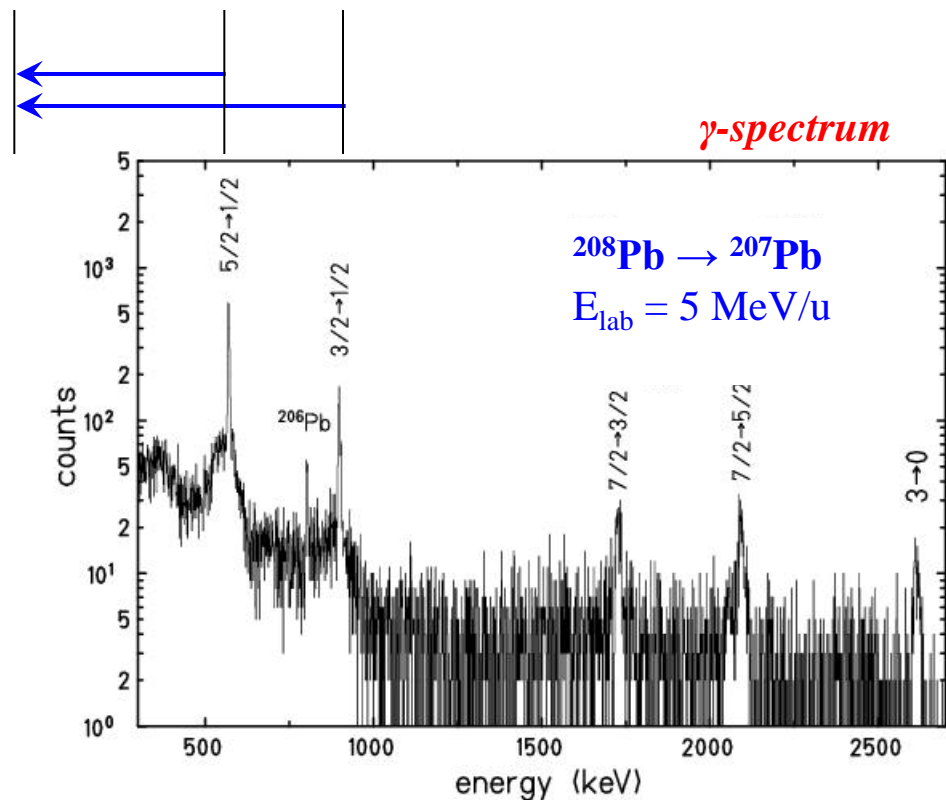
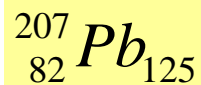
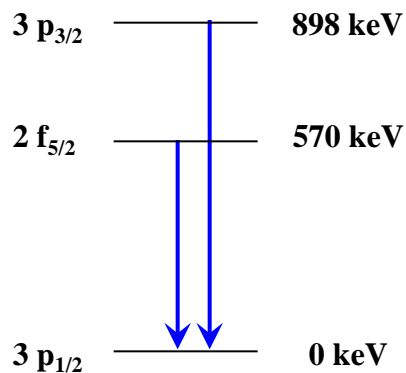


Experimental single-particle energies

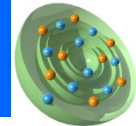


Pb207 1/2- 22.1	Bi209 9/2- 100	Pb209 3.253 h 9/2+ β ⁻
	Pb208 0+ 52.4	
	Tl207 4.77 m 1/2+ *	
	β ⁻	

single-hole energies

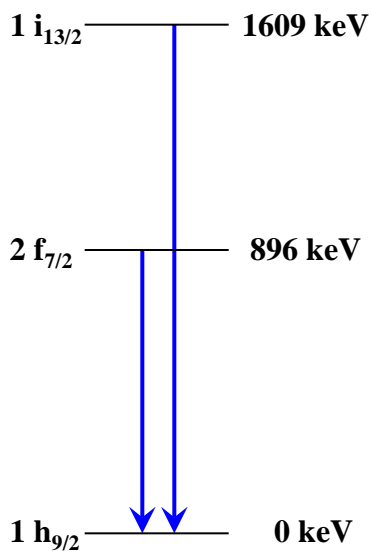


Experimental single-particle energies

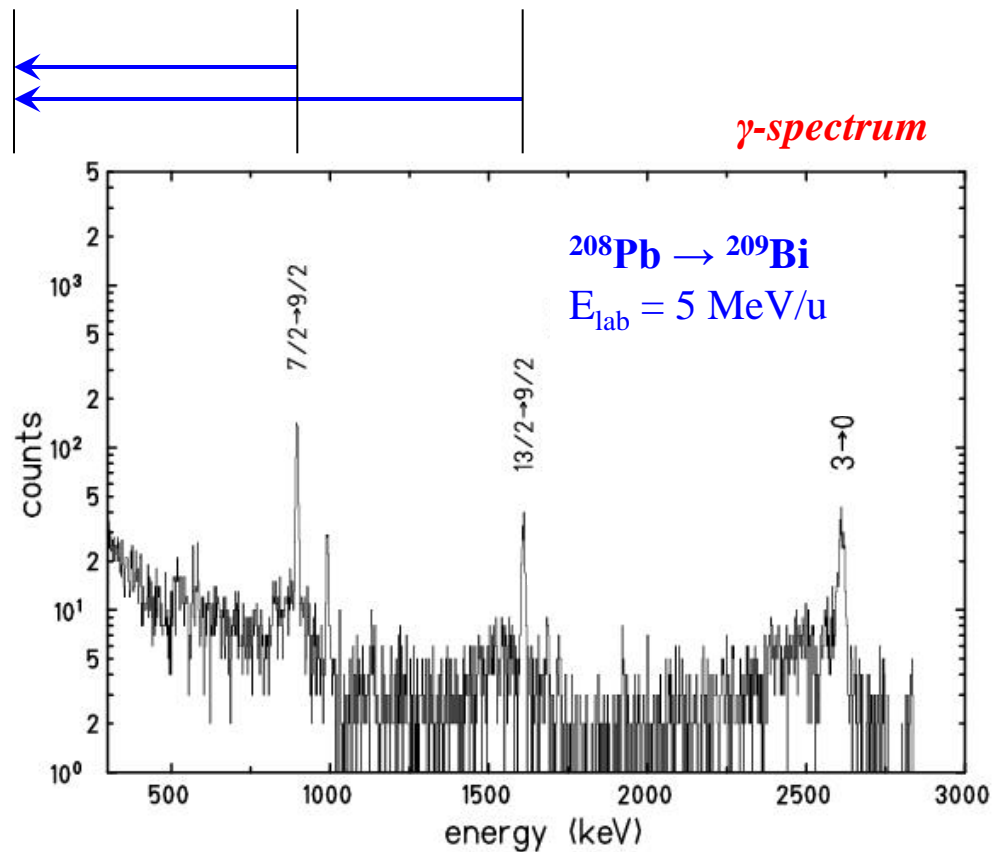


Bi209		
9/2-		
100		
Pb207	Pb208	Pb209
1/2- 22.1	0+ 52.4	3.253 h 9/2+
*	β ⁻	
	Tl207	
	4.77 m 1/2+ *	
	β ⁻	

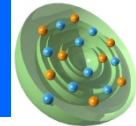
single-particle energies



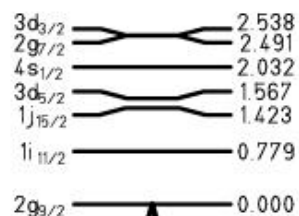
$^{209}_{83}\text{Bi}_{126}$



Experimental single-particle energies



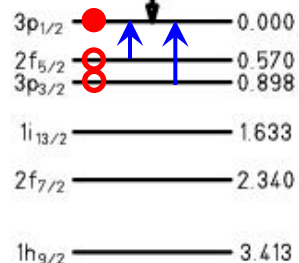
particle states



²⁰⁹Bi

²⁰⁹Pb

²⁰⁸₈₂Pb₁₂₆ 3.431 --



²⁰⁷Tl

²⁰⁷Pb

hole states

neutrons

energy of shell closure:

$$BE(^{209}\text{Pb}) - BE(^{208}\text{Pb}) = E(2 g_{9/2})$$

$$BE(^{207}\text{Pb}) - BE(^{208}\text{Pb}) = -E(3 p_{1/2})$$

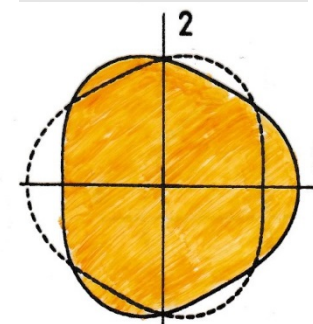
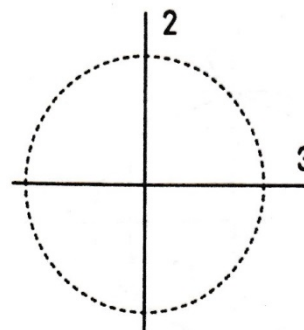
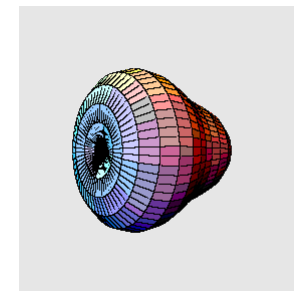
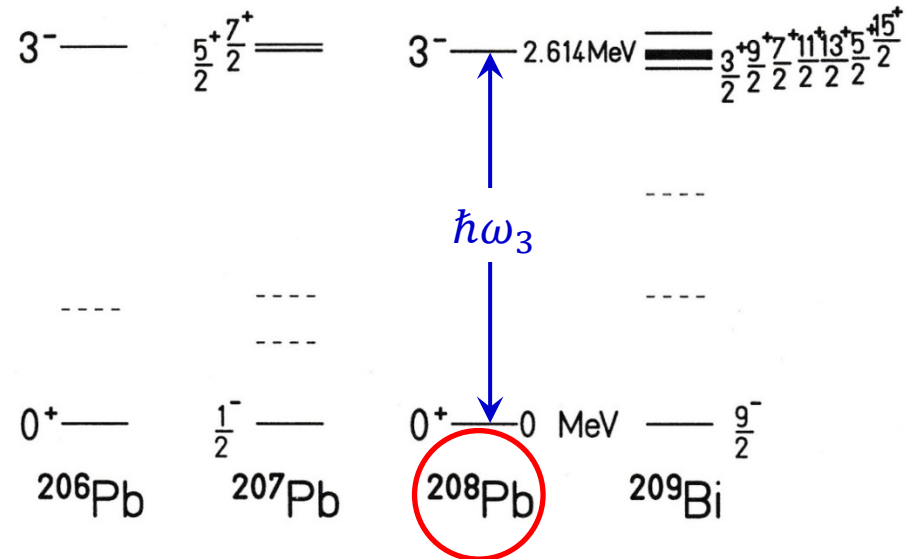
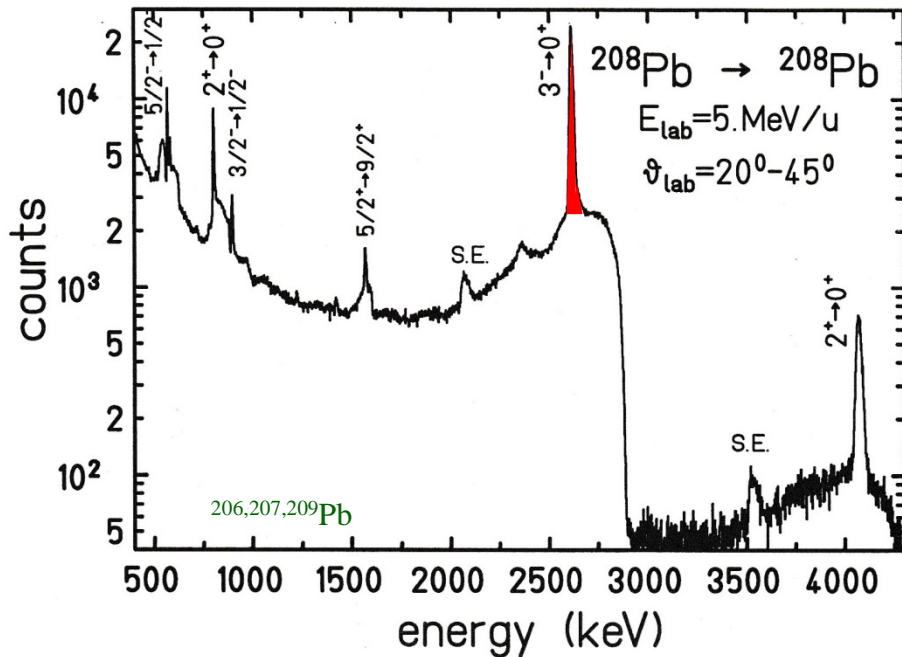
$$E(2 g_{9/2}) - E(3 p_{1/2}) = BE(^{209}\text{Pb}) + BE(^{207}\text{Pb}) - 2 \cdot BE(^{208}\text{Pb}) = -3.432$$

$$BE(^{209}\text{Bi}) - BE(^{208}\text{Pb}) = E(1 h_{9/2})$$

$$BE(^{207}\text{Tl}) - BE(^{208}\text{Pb}) = -E(3 s_{1/2})$$

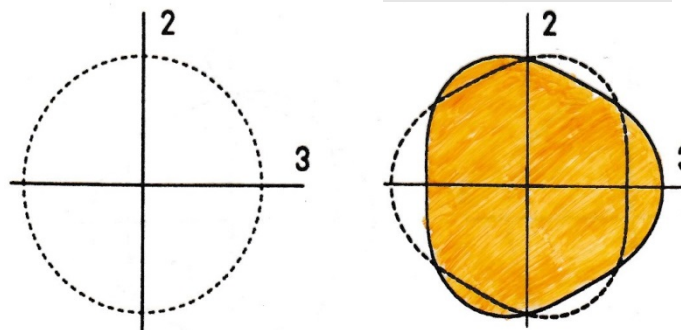
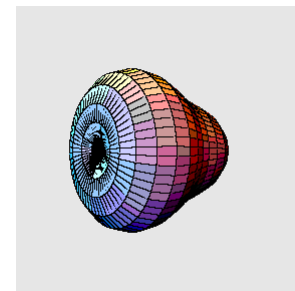
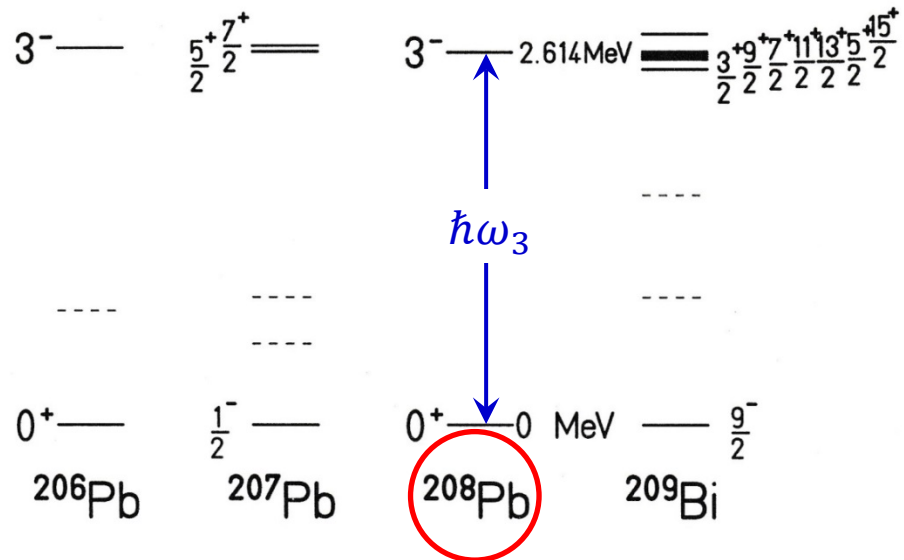
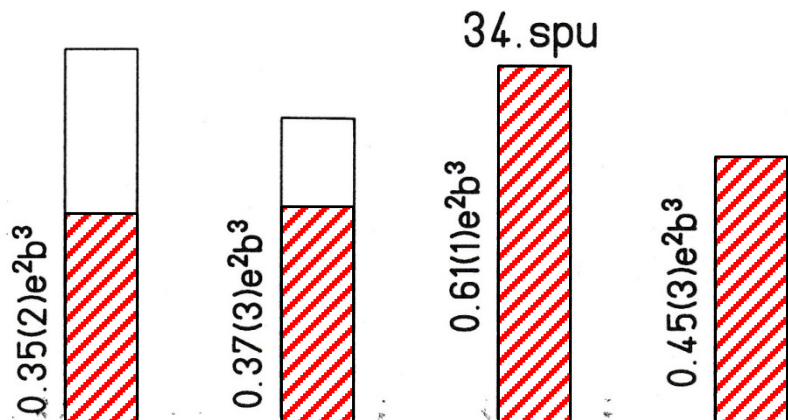
$$E(1 h_{9/2}) - E(3 s_{1/2}) = BE(^{209}\text{Bi}) + BE(^{207}\text{Tl}) - 2 \cdot BE(^{208}\text{Pb}) = -4.211 \text{ MeV}$$

Octupole Vibrational States in the Lead Region

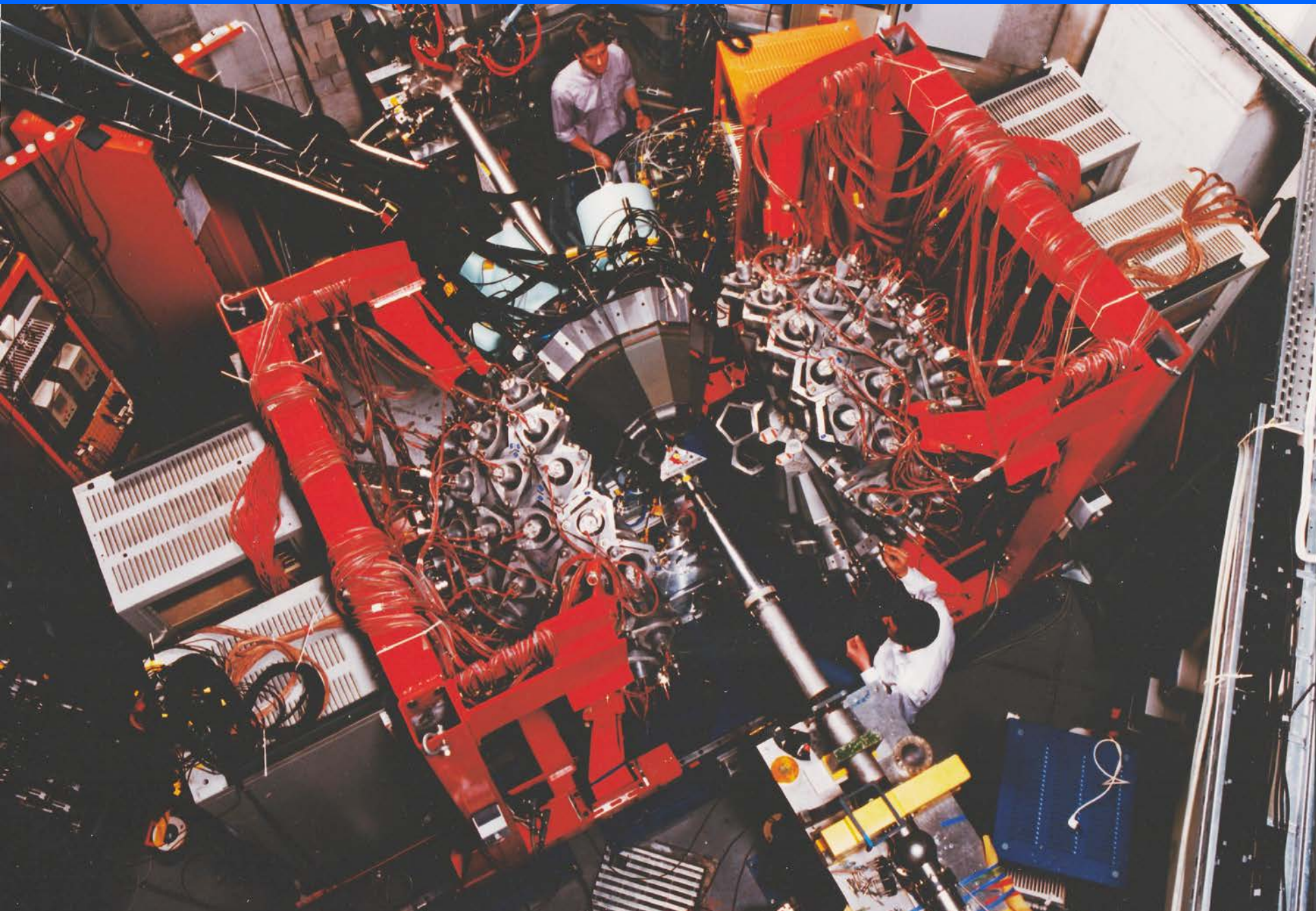


Octupole Vibrational States in the Lead Region

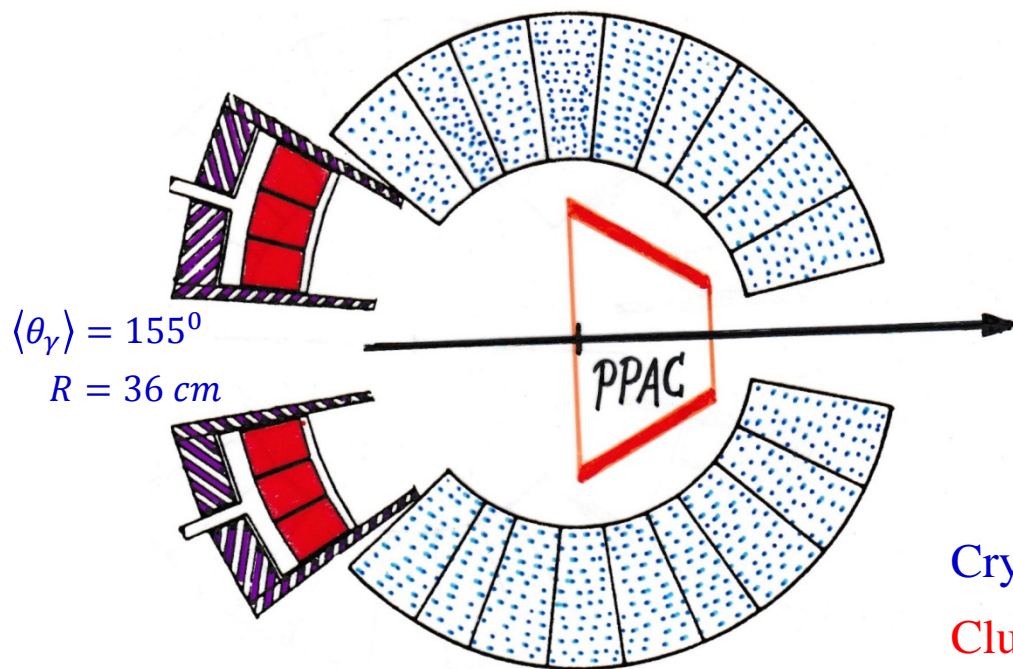
$$\Sigma B(E3; gs \rightarrow I)$$



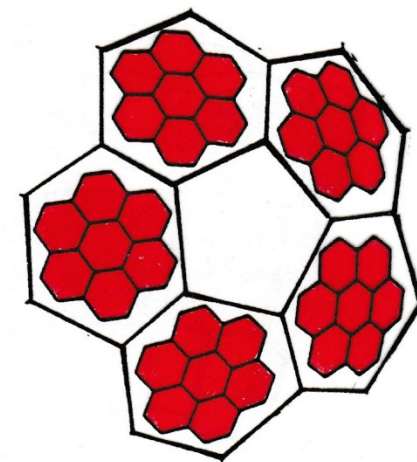
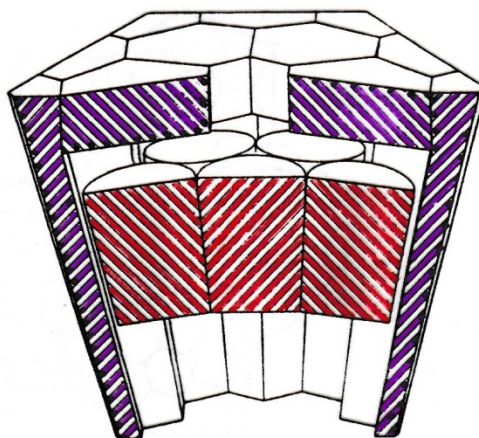
The Darmstadt-Heidelberg Crystal Ball extended by EUROBALL-3 Ge-detectors



The Darmstadt-Heidelberg Crystal Ball extended by EUROBALL-3 Ge-detectors

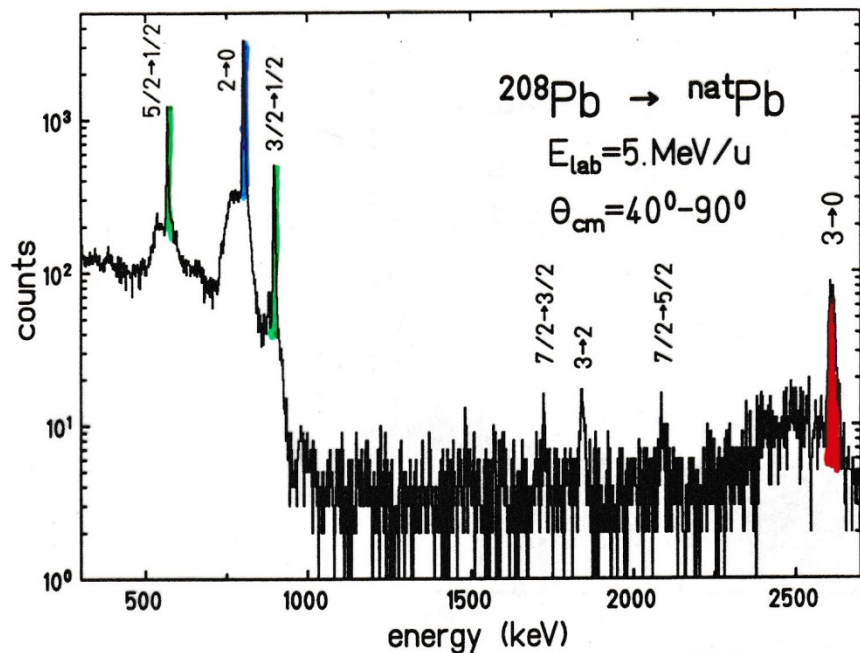


Crystal Ball: $\Omega_{\text{CB}} = 83\%$ $P_{\text{photopeak}} \approx 53\%$
Cluster ring: $\Omega_{\text{EB}} = 7\%$ $P_{\text{photopeak}} \approx 2.2\%$



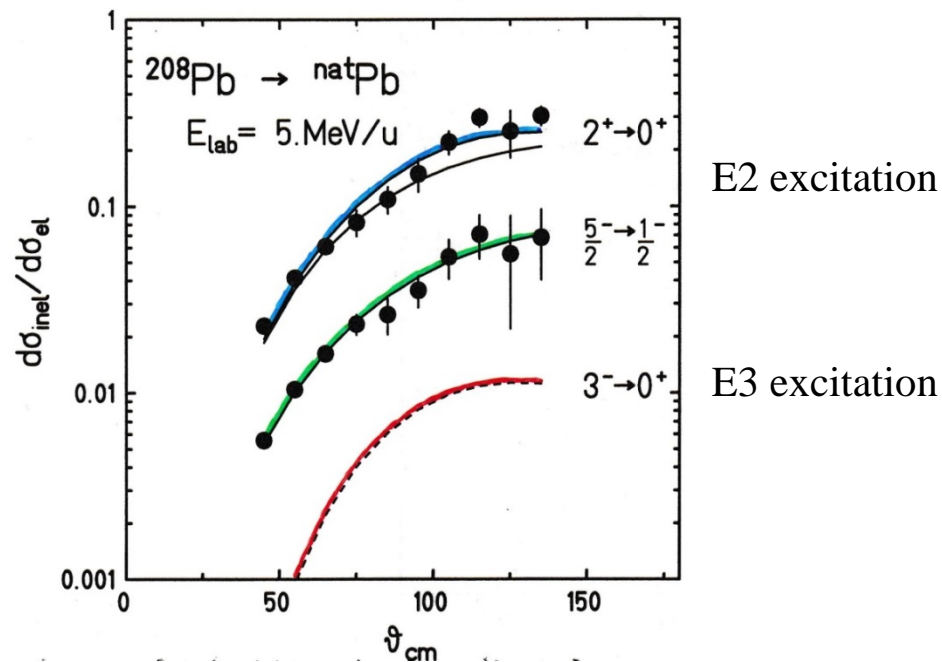
March 27 – September 6, 1996

Octupole Vibrational States in the Lead Region

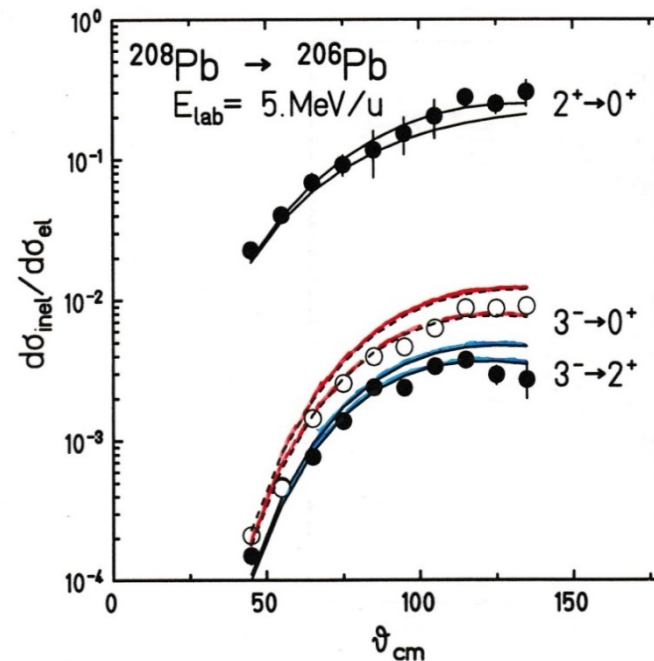
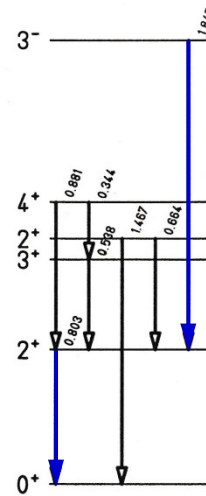
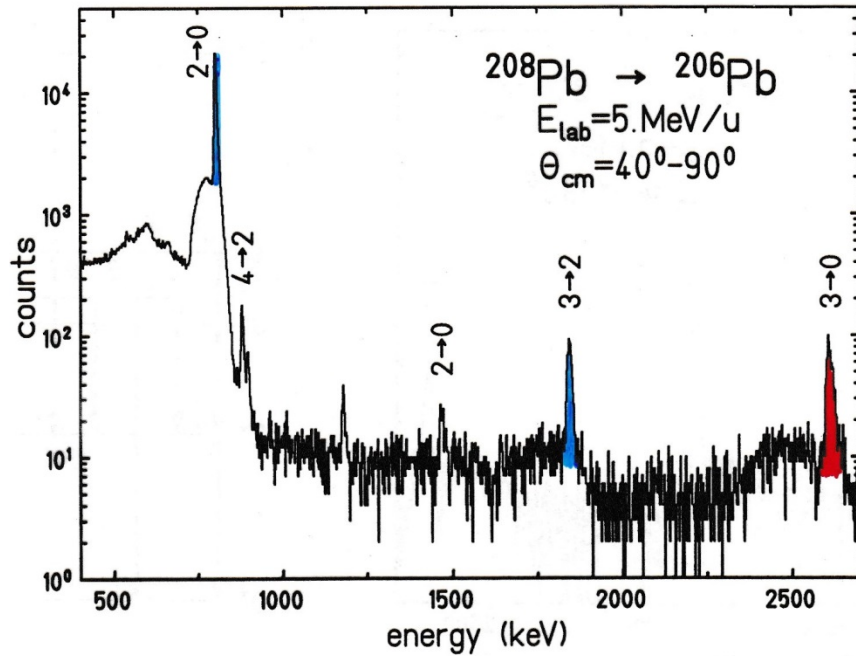


^{206}Pb 24%
 ^{207}Pb 22%
 ^{208}Pb 52%

excitation probability for the 1-excited state



Coulomb Excitation for ^{208}Pb on ^{206}Pb



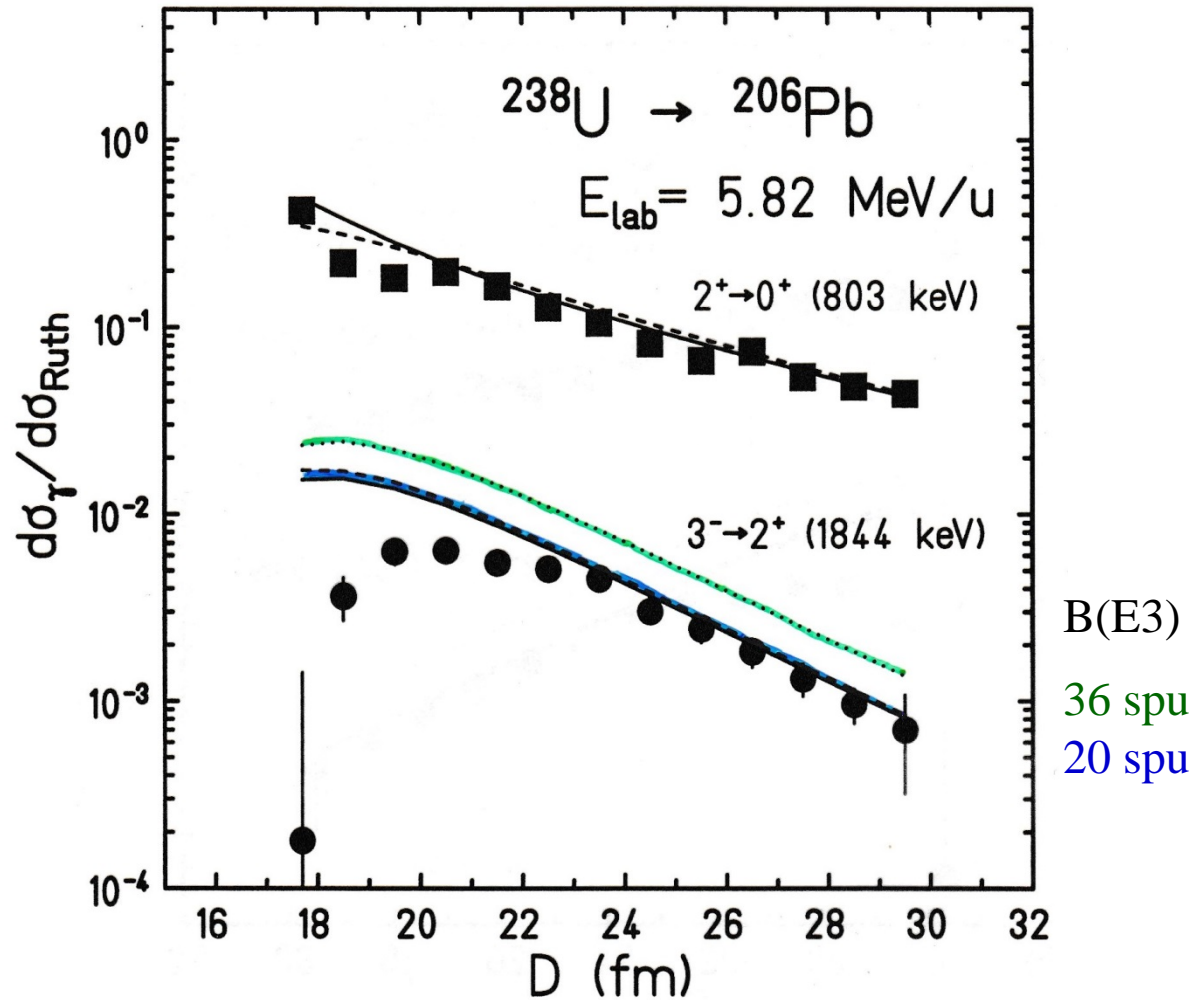
B(E3)

34 spu

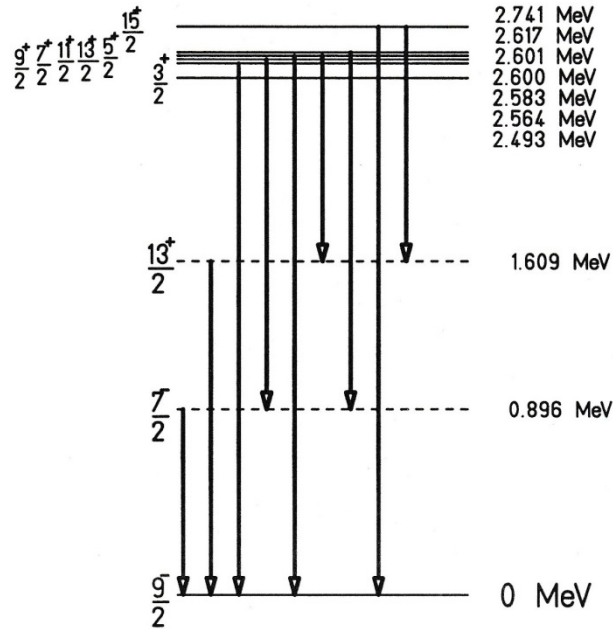
20 spu

Nucl Data: 36 spu

Coulomb Excitation for ^{238}U on ^{206}Pb



Superposition of Vibrational and Particle Motion



$3^- |h_{9/2}\rangle$ septuplet

^{209}Bi

$|h_{9/2}\rangle$

weak coupling:

$$B(E3; n_3 = 0, j \rightarrow (n_3 = 1, j)I) = \frac{2I + 1}{7(2j + 1)} B(E3; n_3 = 0 \rightarrow n_3 = 1)$$

j^π	I^π	$B(E3; n_3 = 0 \rightarrow n_3 = 1)$
$9/2^-$	$3/2^+$	0.017(3) 0.29(5)
$9/2^-$	$9/2^+$	0.073(10) 0.51(7)
$9/2^-$	$7/2^+$	0.052(8) 0.45(7)
$9/2^-$	$11/2^+$	0.093(16) 0.54(9)
$9/2^-$	$13/2^+$	0.080(18) 0.40(9)
$9/2^-$	$5/2^+$	0.034(6) 0.40(7)
$9/2^-$	$15/2^+$	0.104(17) 0.45(7)

$\Sigma: 0.45(3) e^2 b^3$

Superposition of Vibrational and Particle Motion

$$B(E3; n_3=0 \rightarrow n_3=1)$$

$$0.35(2)e^2b^3$$



$^{206}\text{Pb} \quad \nu(p_{1/2}, -2)$

$$0.37(3)e^2b^3$$



$^{207}\text{Pb} \quad \nu(p_{1/2}, -1)$

$$0.61(1)e^2b^3$$

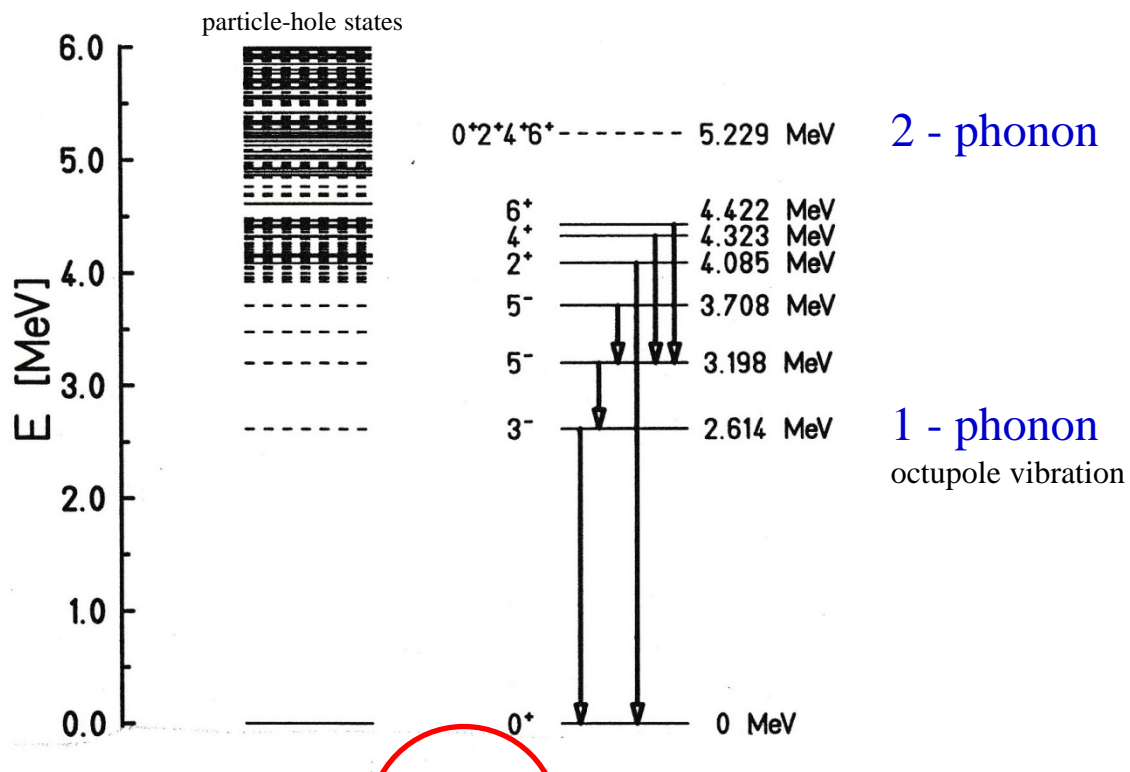


^{208}Pb

$$0.45(3)e^2b^3$$

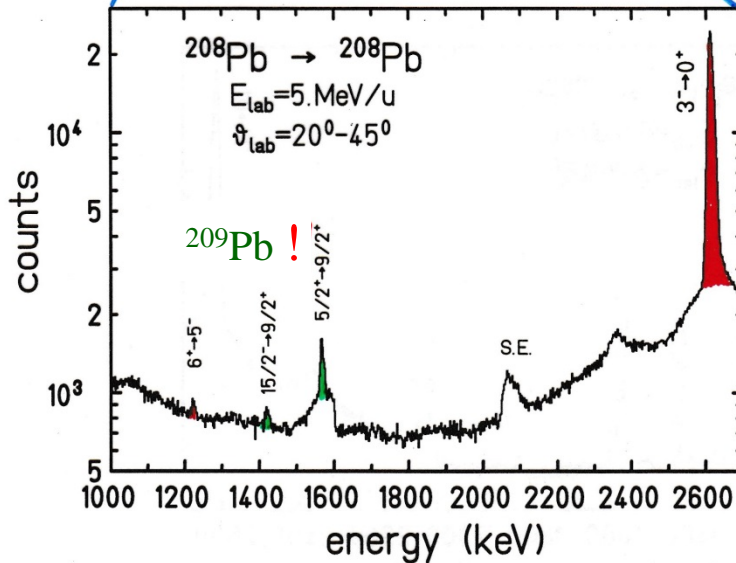
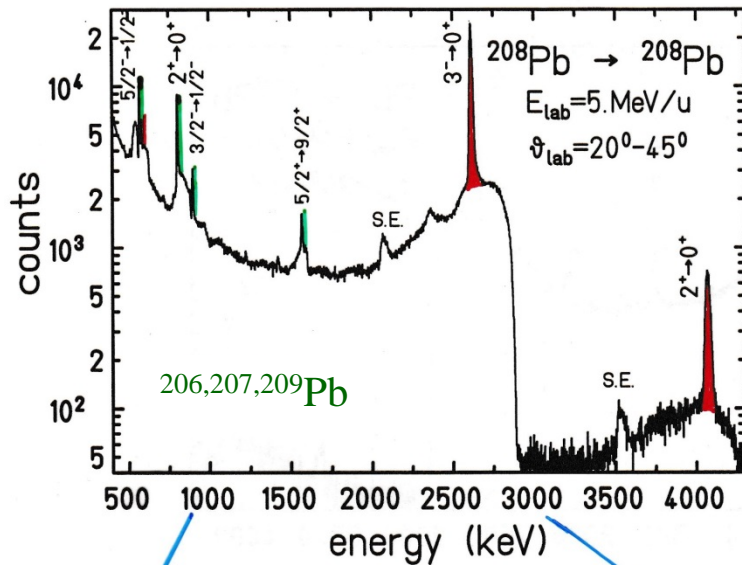


$^{209}\text{Bi} \quad \pi(h_{9/2}, +1)$

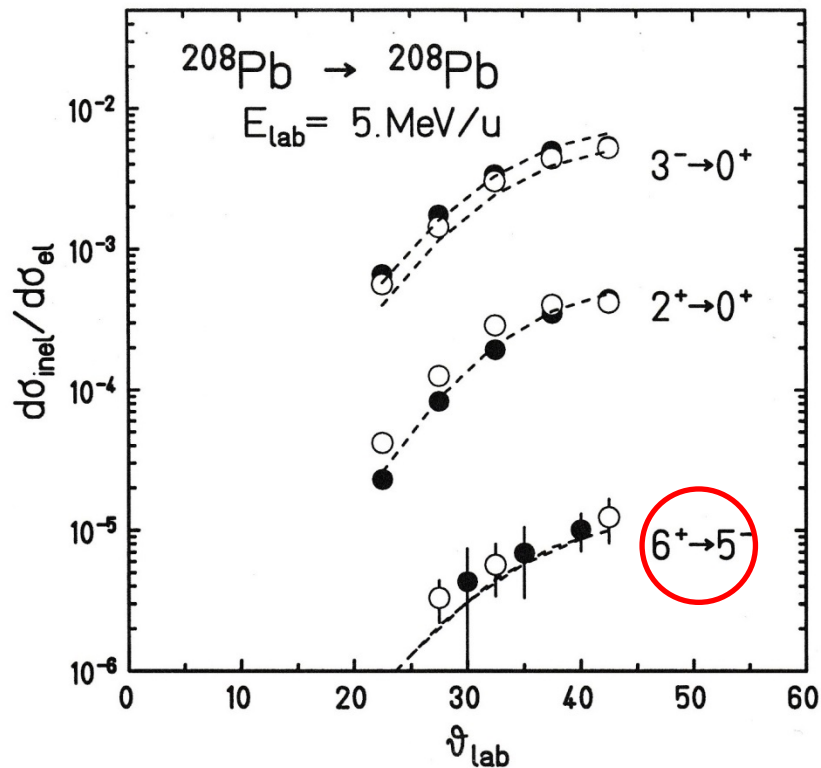


^{208}Pb

Coulomb Excitation for ^{208}Pb on ^{208}Pb



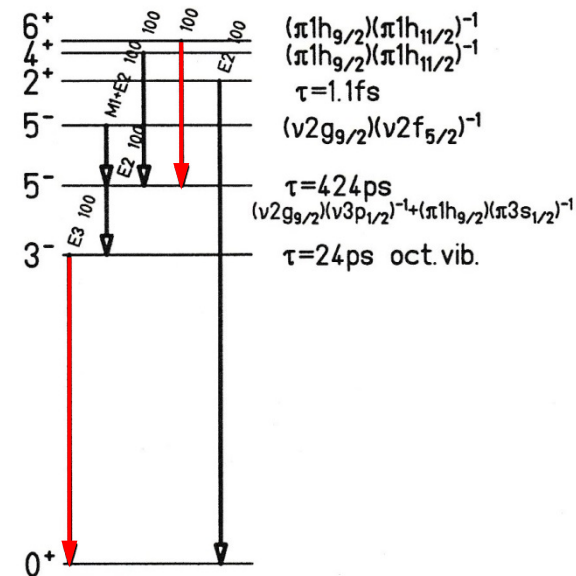
Coulomb Excitation for ^{208}Pb on ^{208}Pb at 5.0 MeV/u



$$\frac{B(E3; 6^+ \rightarrow 3^-)}{B(E3; 3^- \rightarrow 0^+)} = 0.35(11)$$

2.0_{vibrational}

$0^+ 2^+ 4^+ 6^+ \dots$ 2-phonon oct.vib



Octupole Vibrational States in ^{206}Pb , ^{207}Pb , ^{208}Pb and ^{209}Bi

- vibrational excitation $\hbar\omega_3$ is very similar
- $B(E3)$ values are well described in weak coupling model
- collective strength depends on particle configuration
- 2 – phonon octupole vibrational states not observed at 5 MeV/u (insufficient Compton suppression of EUROBALL detectors)
- 6^+ particle-hole state contains 18% of the collective vibrational strength
- transfer reactions (^{209}Pb) observed at 5 MeV/u

Octupole Vibrational States in the Lead Region

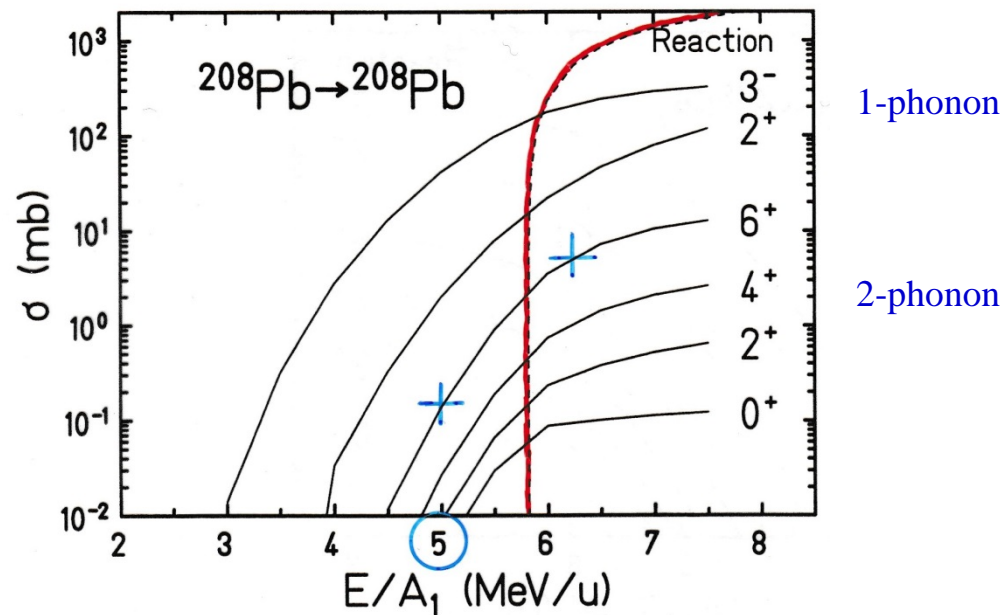
$^{208}\text{Pb} + ^{208}\text{Pb}; E/A_1 = 5 \text{ MeV/u}$

$$\sigma_{6^+} = 0.138 \text{ mb}$$

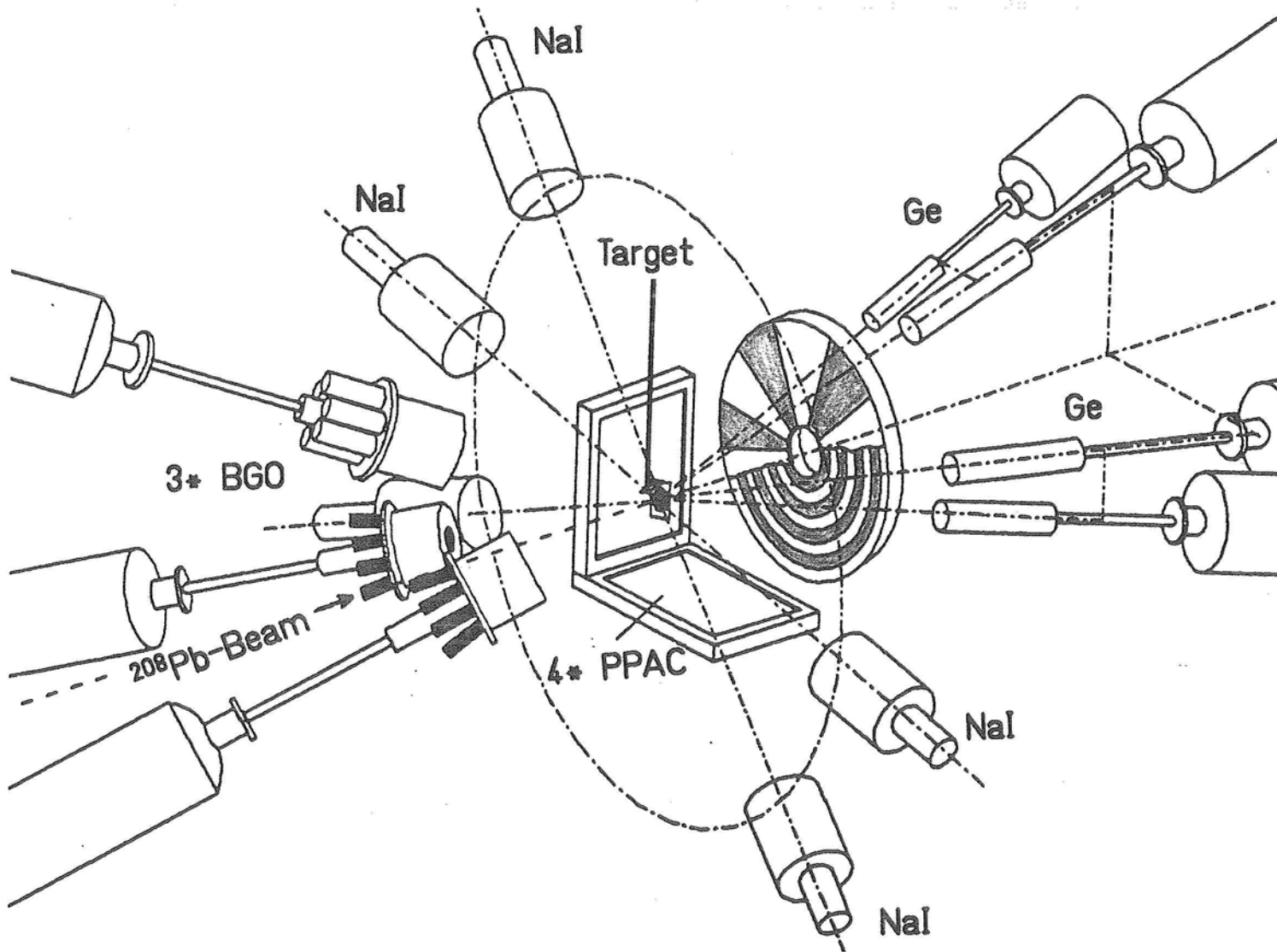
$$\sigma_{4^+} = 0.027 \text{ mb}$$

$$\sigma_{2^+} = 0.009 \text{ mb}$$

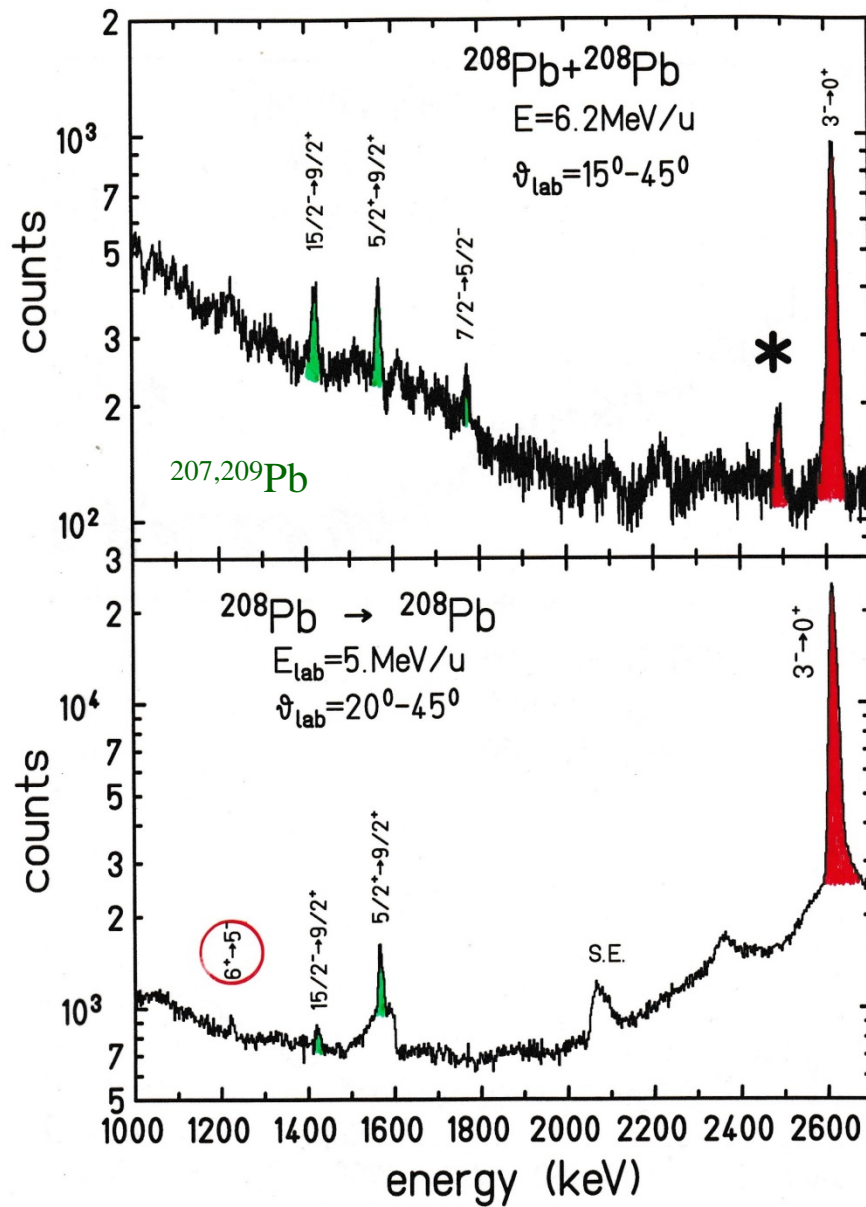
$$\sigma_{0^+} = 0.004 \text{ mb}$$



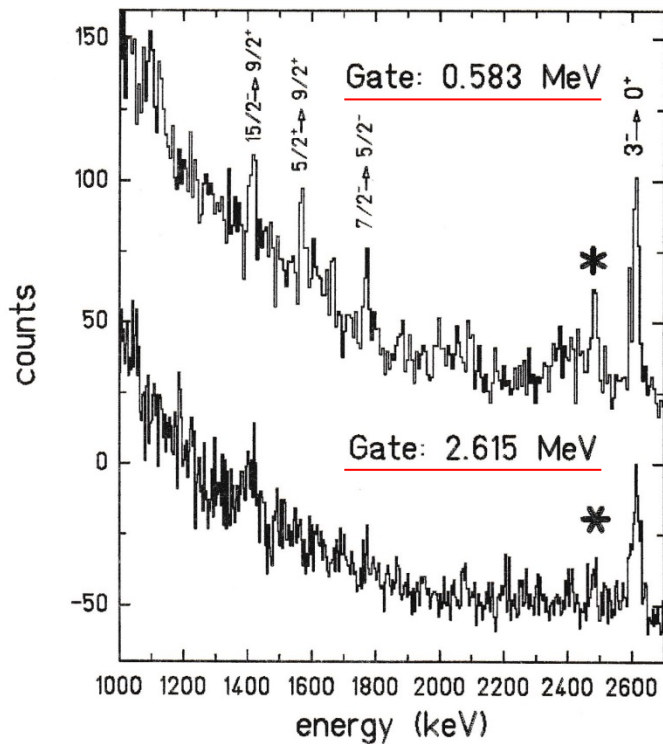
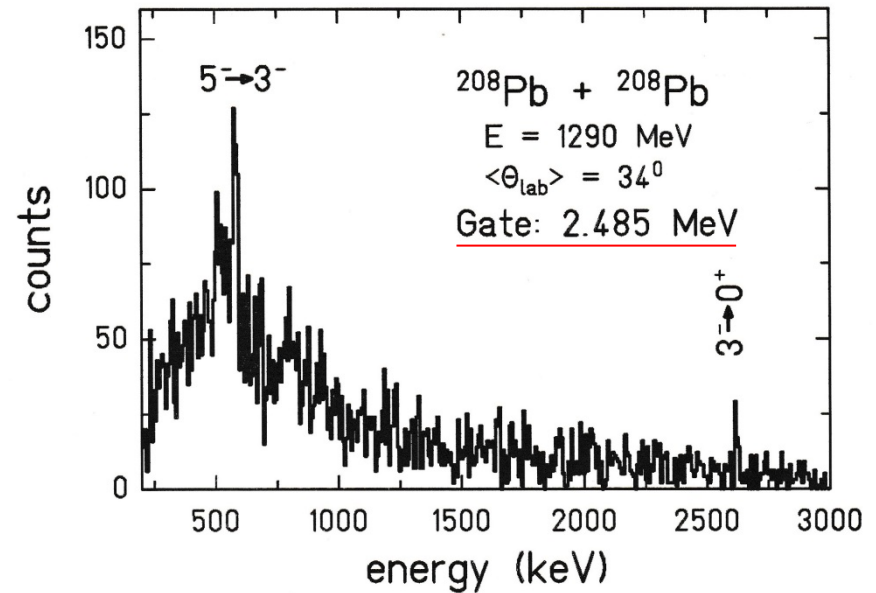
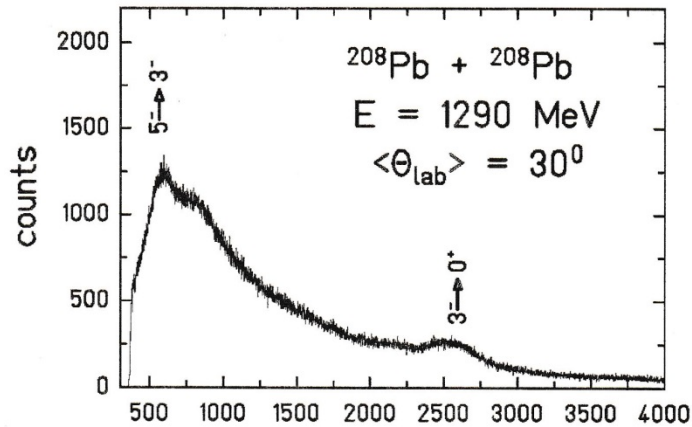
Experimental Setup for ^{208}Pb on ^{208}Pb at 6.2 MeV/u



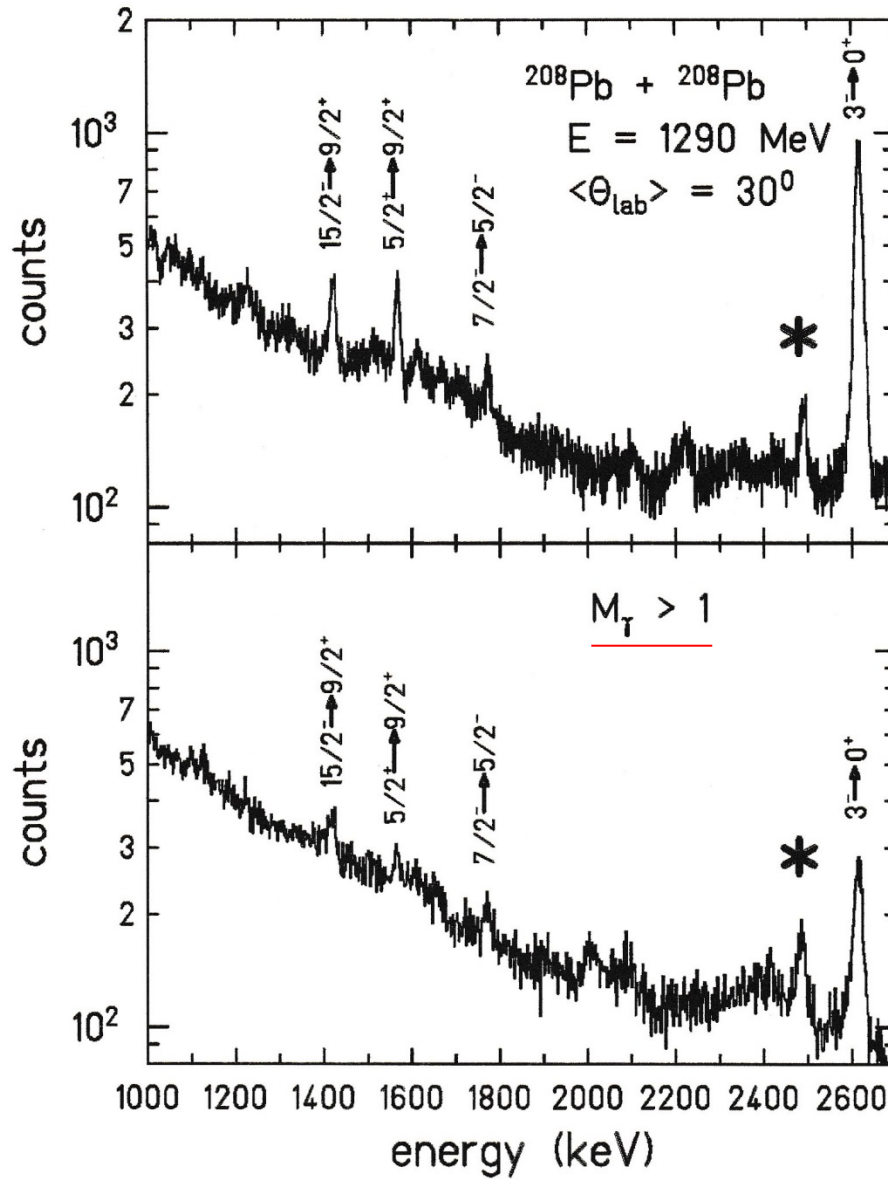
Coulomb Excitation for ^{208}Pb on ^{208}Pb at 6.2 MeV/u



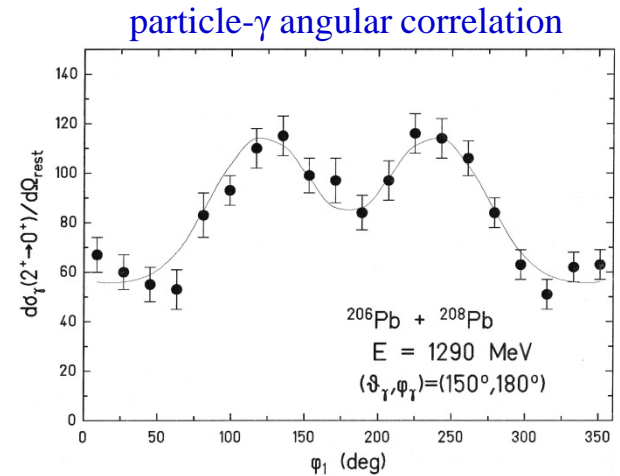
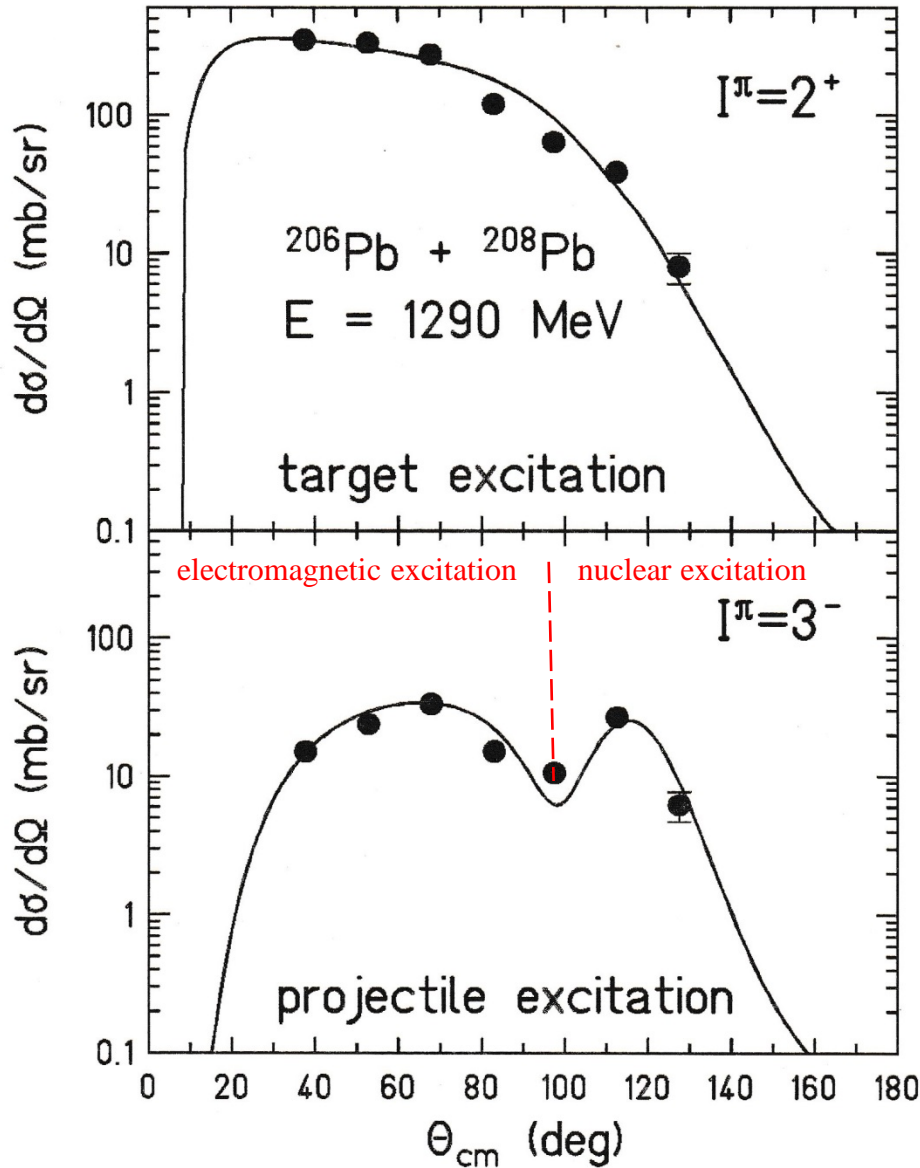
Coulomb Excitation for ^{208}Pb on ^{208}Pb at 6.2 MeV/u



Coulomb Excitation for ^{208}Pb on ^{208}Pb at 6.2 MeV/u



Coulomb and Nuclear Excitation for ^{208}Pb on ^{206}Pb at 6.2 MeV/u

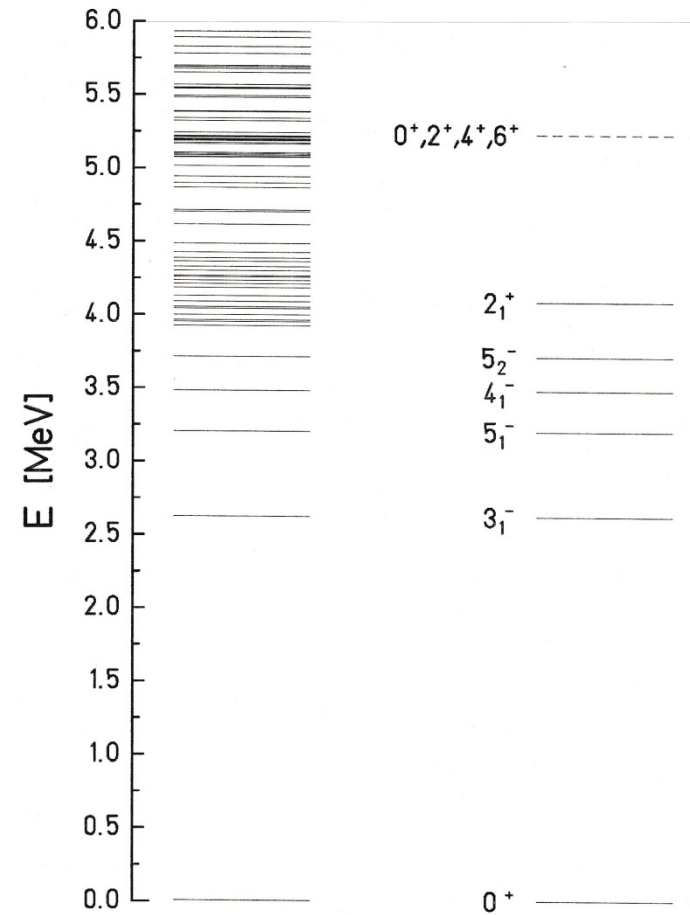
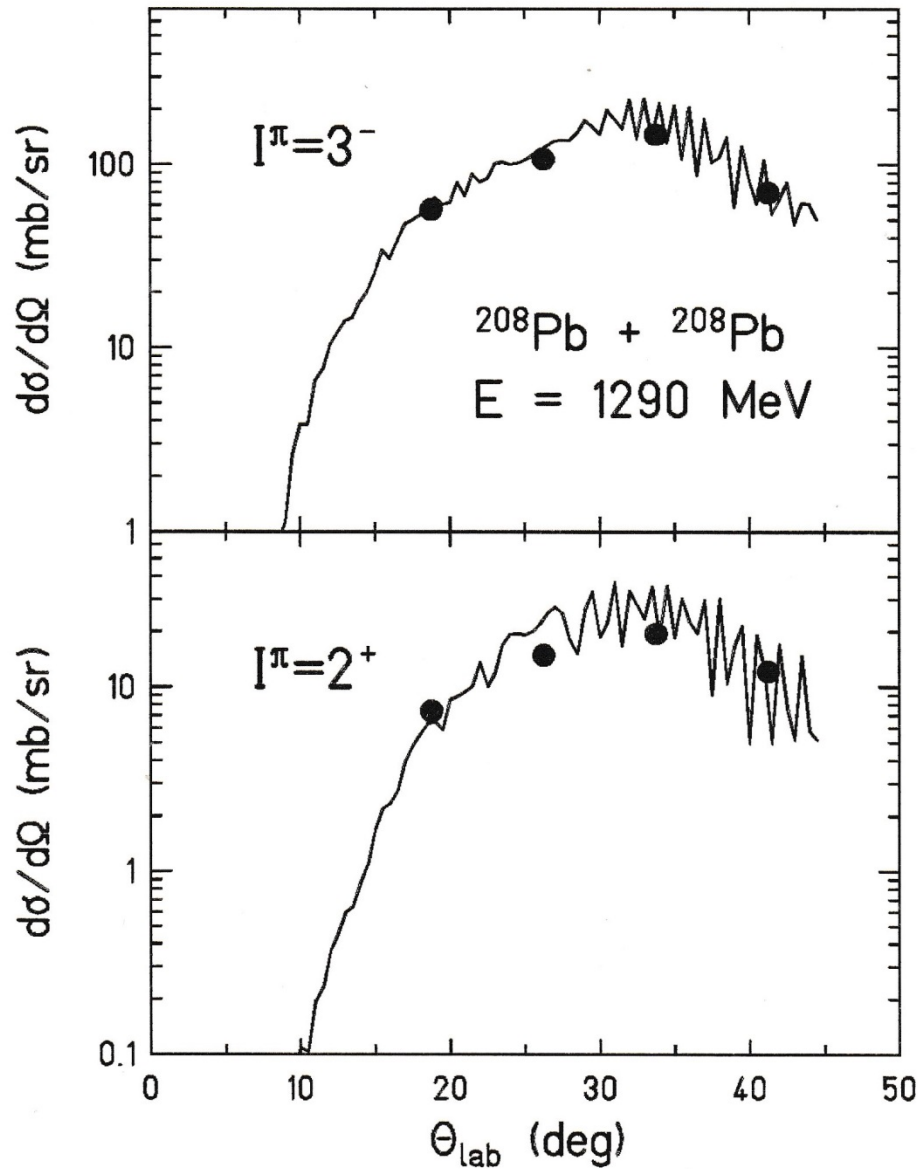


❖ $g(2^+) = 0 \rightarrow$ unperturbed p- γ angular correlation

$$\frac{\sigma_{\text{nucl}}}{\sigma_{\text{total}}} = 63\%$$

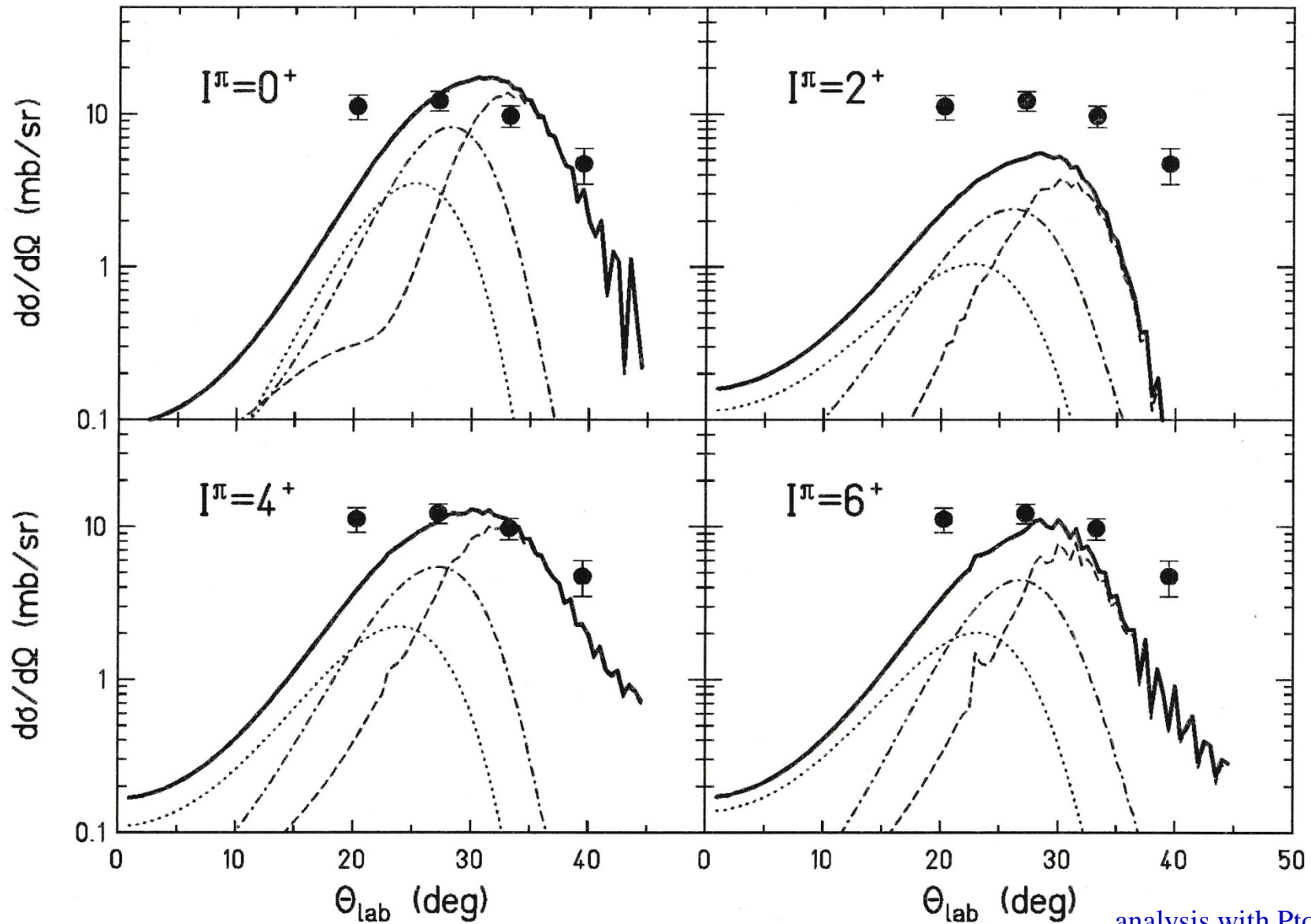
analysis with Ptolemy code

Coulomb and Nuclear Excitation for ^{208}Pb on ^{208}Pb at 6.2 MeV/u



analysis with Ptolemy code

Coulomb and Nuclear Excitation for ^{208}Pb on ^{208}Pb at 6.2 MeV/u



analysis with Ptolemy code

Energy Splitting of the 2-Phonon States

