

# Leptons

- Leptons are *spin 1/2 fermions*, not subject to strong interaction

$$\begin{pmatrix} e^- \\ \nu_e \end{pmatrix} \quad \begin{pmatrix} \mu^- \\ \nu_\mu \end{pmatrix} \quad \begin{pmatrix} \tau^- \\ \nu_\tau \end{pmatrix}$$

$$M_e(0.511 \text{ MeV}/c^2) < M_\mu(105.7 \text{ MeV}/c^2) < M_\tau(1777.1 \text{ MeV}/c^2)$$

- ❖ Electron  $e^-$ , muon  $\mu^-$  and tau  $\tau^-$  have corresponding neutrinos  $\nu_e, \nu_\mu, \nu_\tau$ .
  - ❖ Electron, muon and tau have *electric charge of  $-e$* . Neutrinos are neutral.
  - ❖ Neutrinos possibly have zero or very small mass.
  - ❖ For neutrinos, only weak interactions have been observed so far.
- Antileptons are positron  $e^+$ , positive muon  $\mu^+$  and positive tau  $\tau^+$  and antineutrinos:

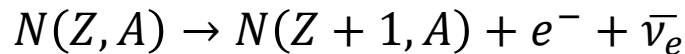
$$\begin{pmatrix} e^+ \\ \bar{\nu}_e \end{pmatrix} \quad \begin{pmatrix} \mu^+ \\ \bar{\nu}_\mu \end{pmatrix} \quad \begin{pmatrix} \tau^+ \\ \bar{\nu}_\tau \end{pmatrix}$$

- Neutrinos and antineutrinos differ by the *lepton number*. Leptons possess lepton number  $L_\alpha = 1$  ( $\alpha$  stands for  $e, \mu, \text{ or } \tau$ , and antileptons have  $L_\alpha = -1$ ).
- Lepton numbers are conserved in any interaction.

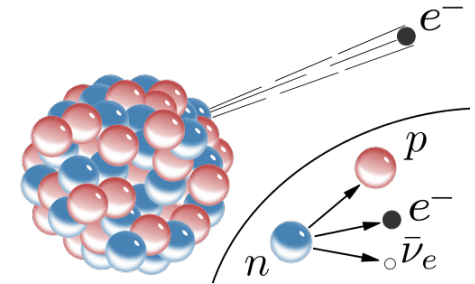
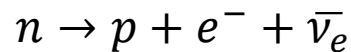
# Leptons

Neutrinos can not be registered by any detector, there are only indirect indications of their quantities.

- ❖ First indication of neutrino existence came from  $\beta$ -decays of a nucleus N:



$\beta$ -decay is nothing but a neutron decay



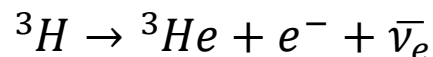
- ❖ Necessity of a neutrino existence comes from the apparent energy and angular momentum non-conservation in observed reactions.

➤ Note that for the sake of the lepton number conservation, electron must be accompanied by an antineutrino and not neutrino!

Mass limit for  $\bar{\nu}_e$  can be estimated from the precise measurements of the  $\beta$ -decay:

$$m_e \leq E_e \leq \Delta M_N - m_{\bar{\nu}_e}$$

The best results are obtained from the tritium decay:



$$m_{\bar{\nu}_e} \leq 15 \text{ eV}/c^2$$

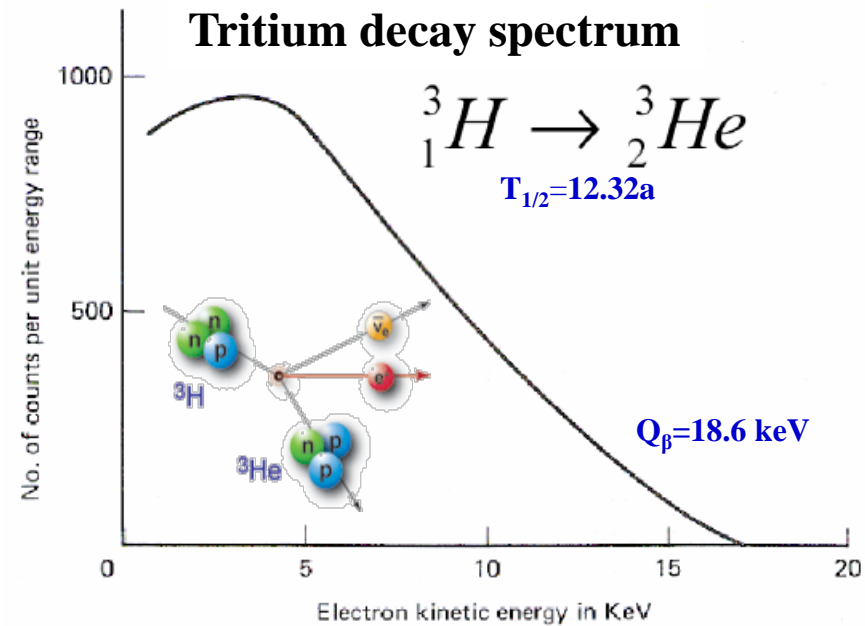
# Tritium decay

The  $\beta^-$  decay energy is given by the mass difference between mother and daughter nucleus.

This energy will be distributed as kinetic energy on the emitting particles, the electron and the anti-neutrino.

Hence, the electron spectrum is continuous.

It starts at zero energy and ends at the maximum possible energy  $E_{\max} = E_0 - m_\nu \cdot c^2 (= Q_\beta)$ .

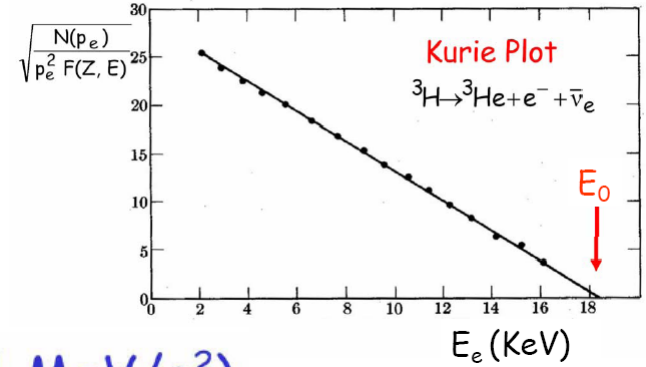


$\beta$  decays have a long lifetime and a small decay probability, the related interaction is small compared to other interactions in the nucleus, therefore time dependent perturbation theory is a good approximation.

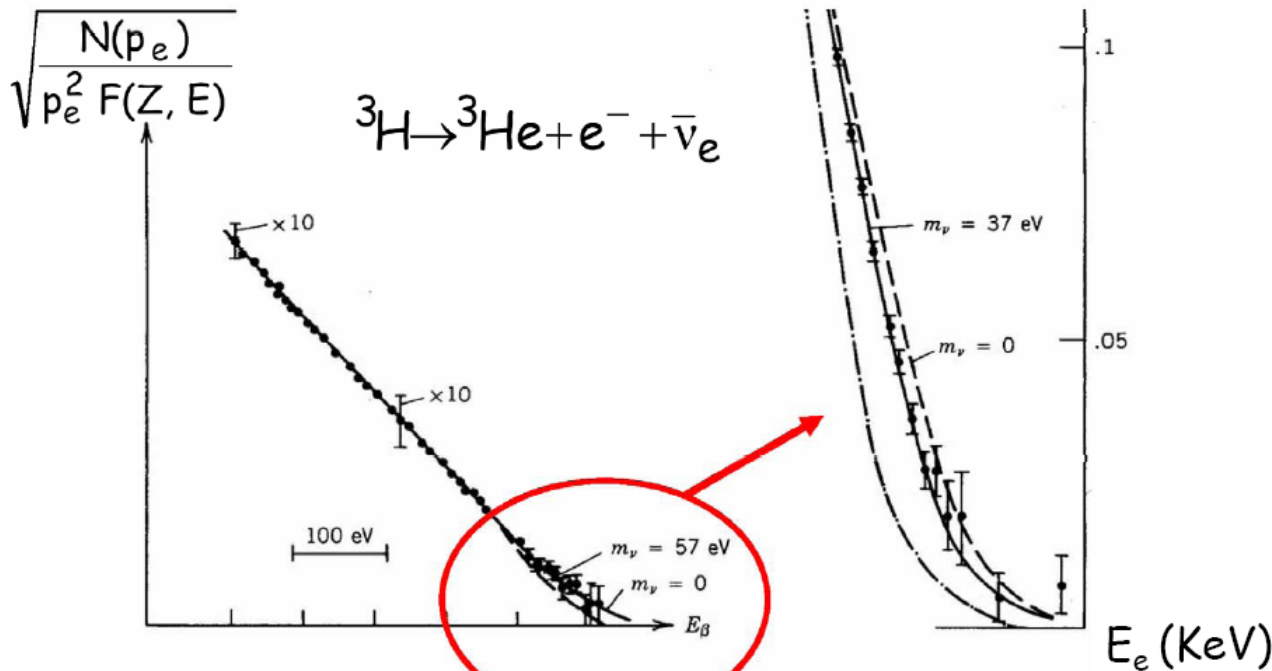
# Tritium decay

Kurie plot:

$$\sqrt{\frac{N(p_e)}{F(Z, \varepsilon) \cdot p_e^2}} = \text{const} \cdot (\varepsilon_0 - \varepsilon)$$



$m_\nu < 3 \text{ eV}/c^2$  (c.f.  $m_e = 0.511 \text{ MeV}/c^2$ )



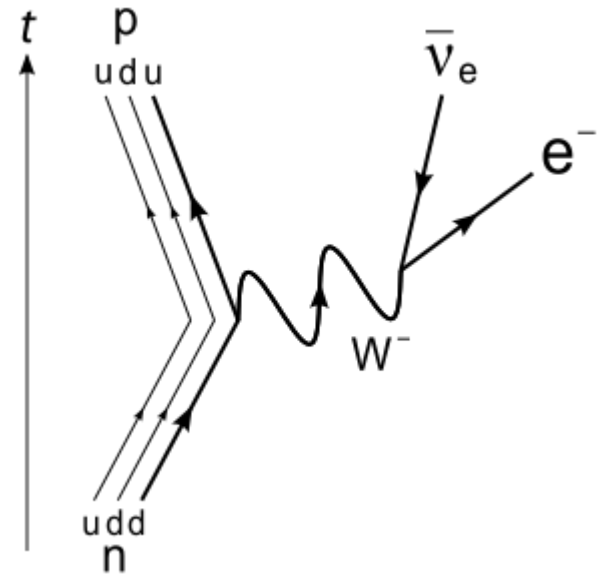
# Weak Interaction

- ❖ Consider a neutron  $n$  ( $udd$ )  $\beta$ -decay

Although the neutron is heavier than its sister proton  $p$  ( $uud$ ), it cannot decay to proton without changing the flavor of one of its **down quarks**  $d$ .

- ❖ Neither EM nor strong interactions allow to change the flavor. It must proceed through weak interaction.

$$d \rightarrow u + W^- \rightarrow u + e^- + \bar{\nu}_e$$



$$n \rightarrow p + e^- + \bar{\nu}_e$$

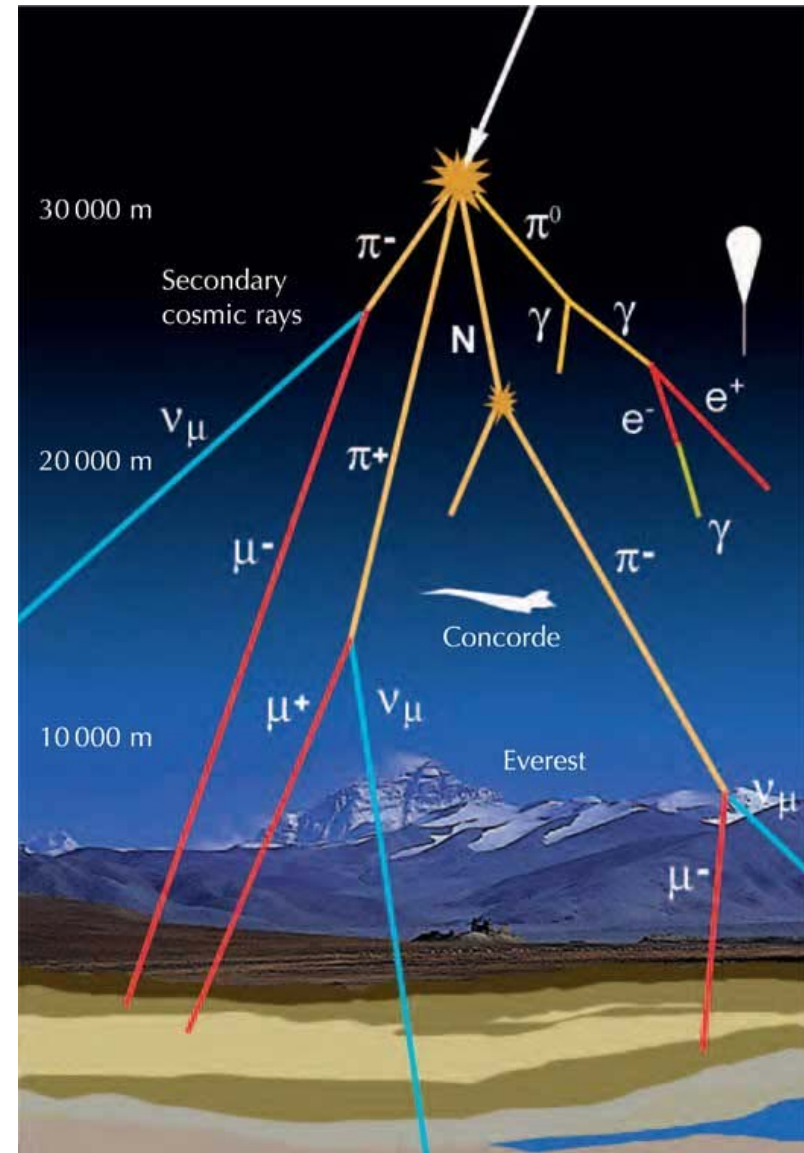
# Source of Neutrinos

## *Nuclear reactions*

- Fusion in the sun
- Fission in reactors
- Big bang nucleosynthesis

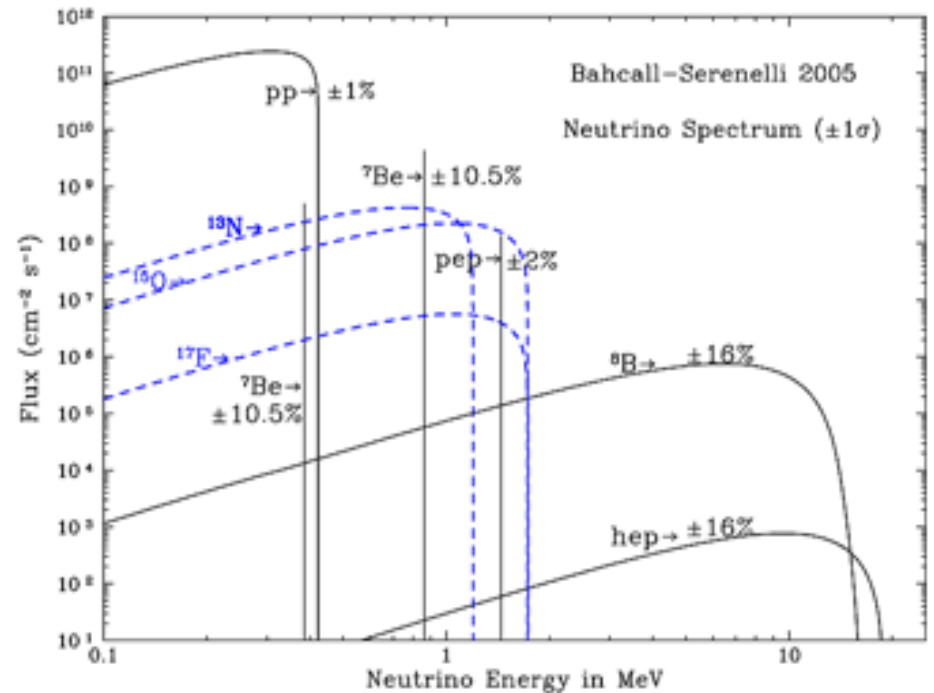
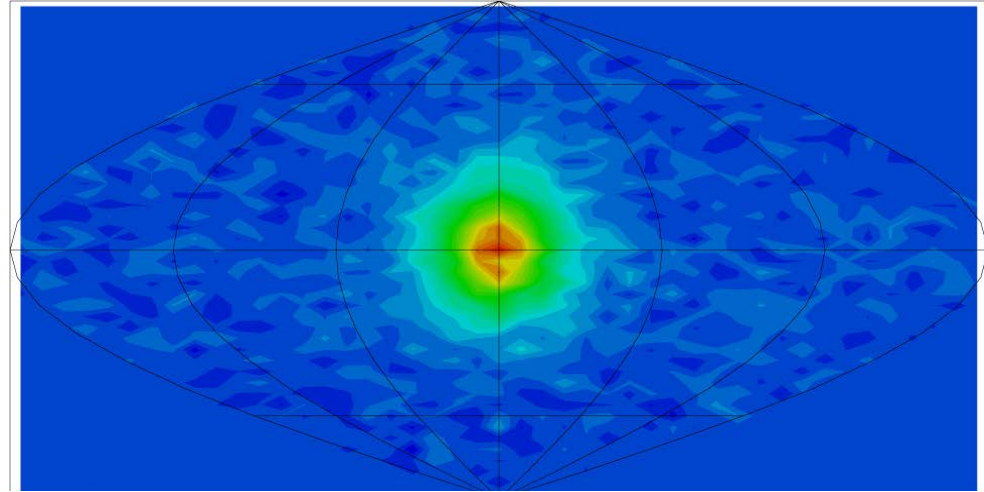
## *High energy collisions*

- Particle colliders
- Cosmic ray showers



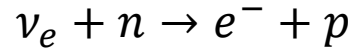
# Solar Neutrinos

- Electron neutrinos produced in fusion chain
  - 99% of solar neutrinos from pp fusion
  - First observation in 2014 by Borexino
  - Small fraction from  ${}^7\text{Be}$  and  ${}^8\text{B}$
  - Extend to high energy, easier to detect
- 
- Bahcall predicted the solar neutrino flux in 1964. He refined this with an incredibly precise solar model over the next 50 years.

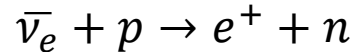


# Leptons

- An inverse  $\beta$ -decay also takes place:



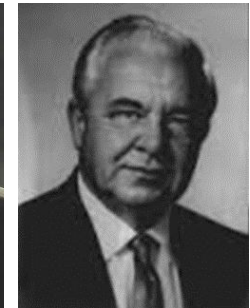
or



However, the probability of these processes is very low, therefore to register it one needs a very intense flux of neutrinos. **Reines and Cowan experiment (1956)**



Frederick Reines

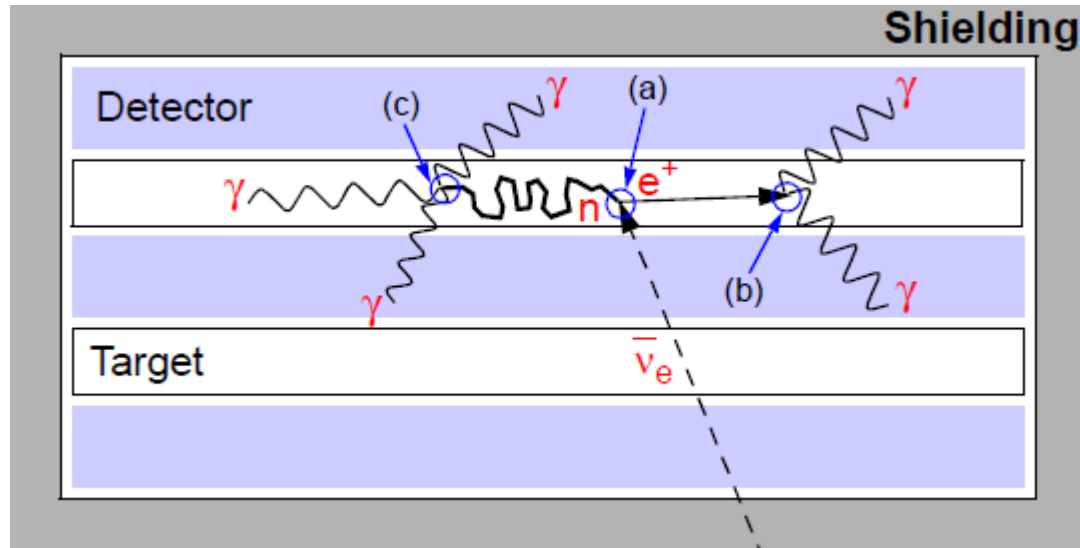


Clyde L. Cowan

- ❖ Using antineutrinos produced in a nuclear reactor, it is possible to obtain around 2 (10) events per hour.
- ❖ Aqueous solution of  $\text{CdCl}_2$  used as the target (Cd used to capture neutrons).
- ❖ To separate the signal from the background, the “delayed coincidence” scheme was used: signal from neutron comes later than one from positron.



# Leptons



Schematic representation of the F. Reines and C. Cowan experiment

Main stages:

- Antineutrino interacts with proton, producing neutron and positron
- Positron annihilates with an atomic electron, produces fast photon which gives rise to softer photons through the Compton effect.
- Neutron captured by a Cd nucleus, releasing more photons

# Leptons

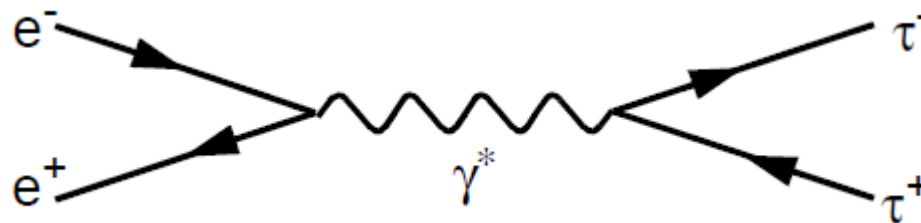
- Muons were first observed in 1936, in *cosmic rays*

Cosmic rays have two components:

- 1) *primaries*, which are high-energy particles coming from the outer space, mostly hydrogen nuclei
- 2) *secondaries*, the particles which are produced in collisions of primaries with nuclei in the Earth atmosphere; muons belong to this component

- ❖ Muons are 200 times heavier than electrons and are very penetrating particles.
- ❖ Electromagnetic properties of muon are identical to those of electron (upon the proper account of the mass difference)

**Tau** is the heaviest of leptons, was discovered in  $e^+e^-$  annihilation experiments in 1975



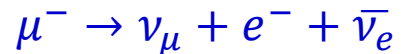
$\tau$  pair production in  $e^+e^-$  annihilation

# Lepton Type Conservation

- Electron is a stable particle, while muon and tau have a finite lifetime:

$$\tau_{\mu} = 2.2 \cdot 10^{-6} \text{ s} \quad \text{and} \quad \tau_{\tau} = 2.9 \cdot 10^{-13} \text{ s}$$

Muon decays in a purely leptonic mode:



electron number	0	=	0	+	1	+	-1
muon number	1	=	1	+	0	+	0
tau number	0	=	0	+	0	+	0

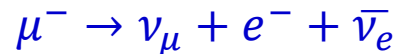
Electrons and their neutrinos have electron number +1  
Positrons and their antineutrinos have electron number -1

# Lepton Decay

- Electron is a stable particle, while muon and tau have a finite lifetime:

$$\tau_{\mu} = 2.2 \cdot 10^{-6} \text{ s} \quad \text{and} \quad \tau_{\tau} = 2.9 \cdot 10^{-13} \text{ s}$$

- Muon decays in a purely leptonic mode:



- Tau has a mass sufficient to produce hadrons, but has leptonic decay modes as well:



- Fraction of a particular decay mode with respect to all possible decays is called ***branching ratio***.

Branching ratio of both processes are 17.81% and 17.37%, respectively

- **Note: lepton numbers are conserved in all reactions ever observed**

# Leptons

## Important assumptions:

- 1) Weak interactions of leptons are identical, just like electromagnetic ones (“interactions universality”)
- 2) One can neglect final state lepton masses for many basic calculations

The *decay rate* of a muon is given by the expression:

$$\Gamma(\mu^- \rightarrow e^- + \bar{\nu}_e + \nu_\mu) = \frac{G_F^2 m_\mu^5}{195 \pi^3}$$

Here  $G_F$  is the *Fermi constant* ( $G_F^0 = \frac{G_F}{(\hbar c)^3} = \frac{\sqrt{2}}{8} \frac{g^2}{m_W^2 c^4} = 1.1664 \cdot 10^{-5} \text{ GeV}^{-2}$ )

Substituting  $m_\mu$  with  $m_\tau$  one obtains decay rates of tau leptonic decays, equal for both processes. It explains why branching ratios of these processes have very close values.

# Leptons

Using the decay rate, the lifetime of a lepton is:

$$\tau_\ell = \frac{B(\ell^- \rightarrow e^- \bar{\nu}_e \nu_\ell)}{\Gamma(\ell^- \rightarrow e^- \bar{\nu}_e \nu_\ell)}$$

Here  $\ell$  stands for  $\mu$  or  $\tau$ . Since muons have basically only one decay mode,  $B = 1$  in their case. Using experimental values of  $B$  and formula for  $\Gamma$ , one obtains the ratio of muon and tau lifetimes:

$$\frac{\tau_\tau}{\tau_\mu} \approx 0.178 \cdot \left(\frac{m_\mu}{m_\tau}\right)^5 \approx 1.3 \cdot 10^{-7}$$

This again is in very good agreement with independent experimental measurements

- Universality of lepton interactions is provided to big extend. That means that there is basically no difference between lepton generations, *apart of the mass*.

# Electroweak

In the Standard Model the weak and the electromagnetic interactions have been combined into a unified *electroweak* theory.

- ❖ At very short distances ( $\sim 10^{-18}$  m) the strength of the weak interaction is comparable to that of the electromagnetic.
- ❖ At thirty times that distance ( $3 \cdot 10^{-17}$  m) the strength of the weak interaction is  $1/10000^{\text{th}}$  than that of the electromagnetic interaction. At distances typical for quarks in a proton or neutron ( $10^{-15}$  m) the force is even tinier.

## PROPERTIES OF THE INTERACTIONS

Property \ Interaction	Gravitational	Weak (Electroweak)			Strong	
					Fundamental	Residual
Acts on:	Mass – Energy	Flavor			Color Charge	See Residual Strong Interaction Note
Particles experiencing:	All	Quarks, Leptons			Quarks, Gluons	Hadrons
Particles mediating:	Graviton (not yet observed)	W <sup>+</sup> W <sup>-</sup> Z <sup>0</sup>			Gluons	Mesons
Strength relative to electromag for two u quarks at:	$10^{-18}$ m	10 <sup>-41</sup>	0.8	1	25	Not applicable to quarks
	$3 \times 10^{-17}$ m	10 <sup>-41</sup>	10 <sup>-4</sup>	1	60	
	for two protons in nucleus	10 <sup>-36</sup>	10 <sup>-7</sup>	1	Not applicable to hadrons	20

## PROPERTIES OF THE INTERACTIONS

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		(Electroweak)		Fundamental	Residual
Acts on:	Mass – Energy	Flavor	Electric Charge	Color Charge	See Residual Strong Interaction Note
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Particles mediating:	Graviton (not yet observed)	$W^+$ $W^-$ $Z^0$	$\gamma$	Gluons	Mesons
Strength relative to electromag for two u quarks at:	$10^{-41}$	0.8	1	25	Not applicable to quarks
for two protons in nucleus	$10^{-41}$	$10^{-4}$	1	60	
	$10^{-36}$	$10^{-7}$	1	Not applicable to hadrons	

- ❖ The strength of the interaction depends strongly on both the mass of the force carrier and the distance of the interaction.
- ❖ The difference between their observed strengths is due to the huge difference in mass between the  $W^\pm$  and  $Z^0$  particles, which are very massive, and the photon, which has no mass.

Unified Electroweak spin = 1		
Name	Mass GeV/c <sup>2</sup>	Electric charge
$\gamma$ photon	0	0
$W^-$	80.4	-1
$W^+$	80.4	+1
$Z^0$	91.187	0