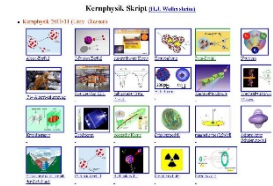


# Outline: Future UNILAC experiments

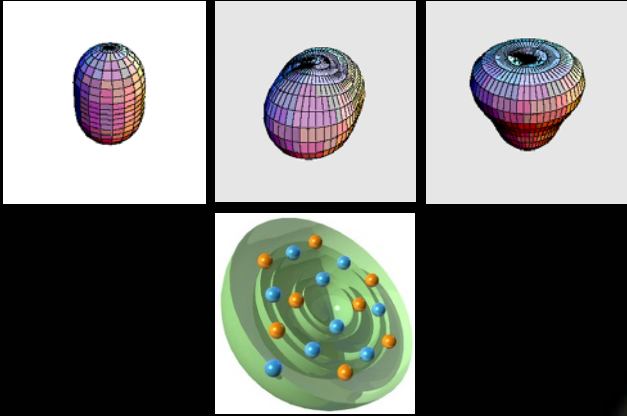
Lecturer: Hans-Jürgen Wollersheim

e-mail: [h.j.wollersheim@gsi.de](mailto:h.j.wollersheim@gsi.de)

web-page: <https://web-docs.gsi.de/~wolle/> and click on



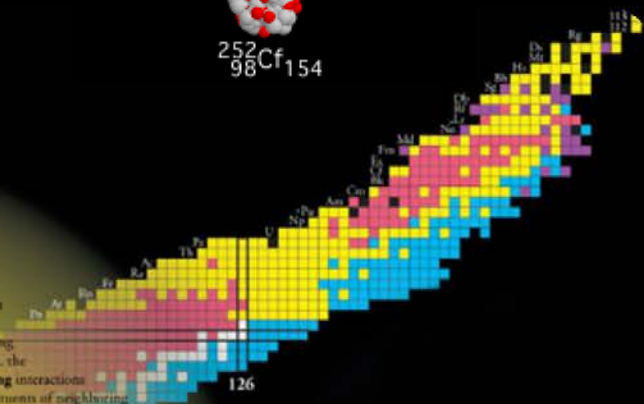
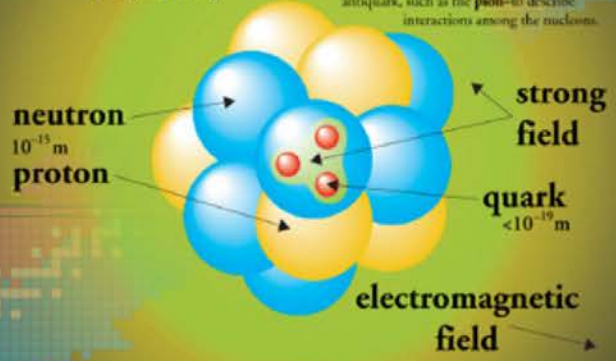
1. Coulomb excitation
2.  $\alpha$ -transfer reaction
3. electron spectroscopy
4. K-isomerism
5. transient magnetic field
6. spectroscopy of fission fragments



# The Nucleus

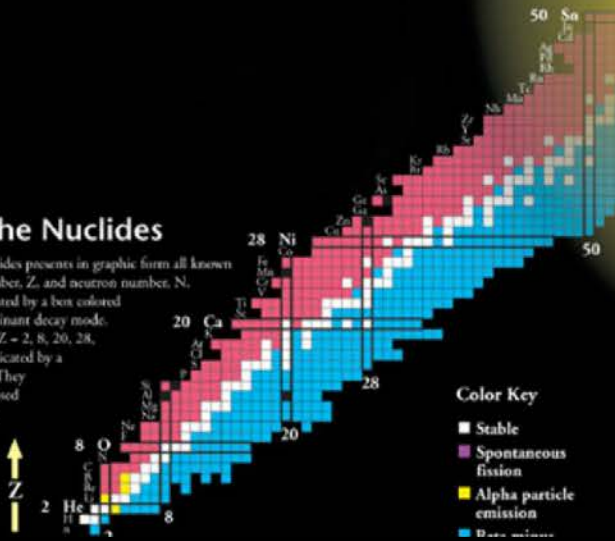
$(1-10) \times 10^{-15} \text{ m}$

At the center of the atom is a nucleus formed from **nucleons**-protons and neutrons. Each nucleon is made from three **quarks** held together by their strong interactions, which are mediated by **gluons**. In turn, the nucleus is held together by the **strong interactions** between the gluon and quark constituents of neighboring nucleons. Nuclear physicists often use the exchange of **mesons**-particles which consist of a quark and an antiquark, such as the **pion**-to describe interactions among the nucleons.

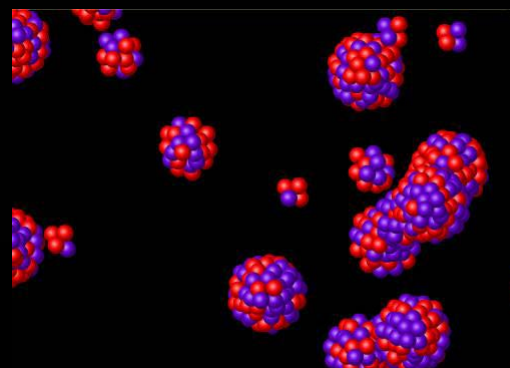


## Chart of the Nuclides

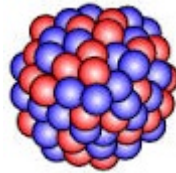
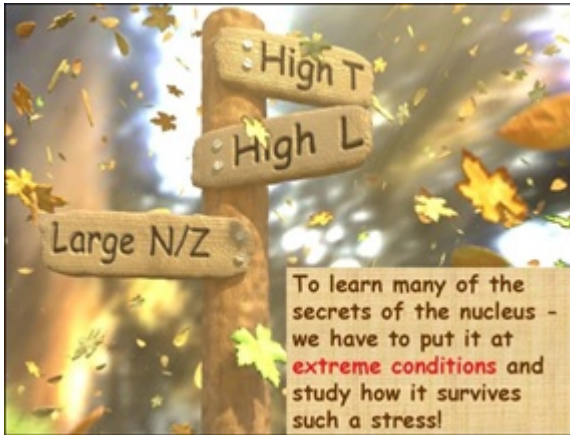
The Chart of the Nuclides presents in graphic form all known nuclei with atomic number, Z, and neutron number, N. Each nuclide is represented by a box colored according to its predominant decay mode. **Magic numbers** (N or Z = 2, 8, 20, 28, 50, 82 and 126) are indicated by a rectangle on the chart. They correspond to major closed shells and those regions of greater nuclear binding energy.



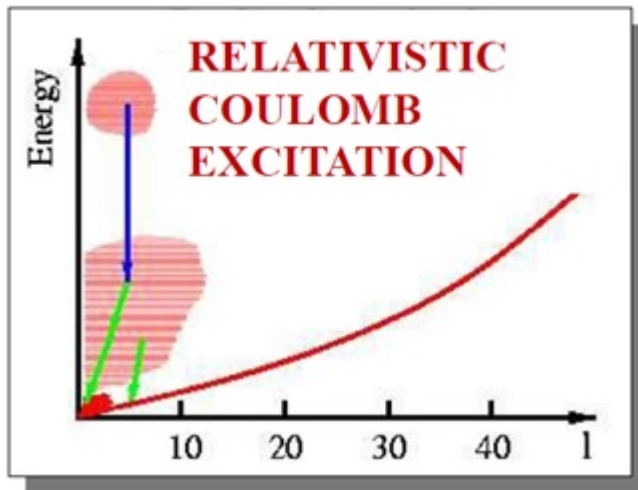
heavy ion nuclear reactions



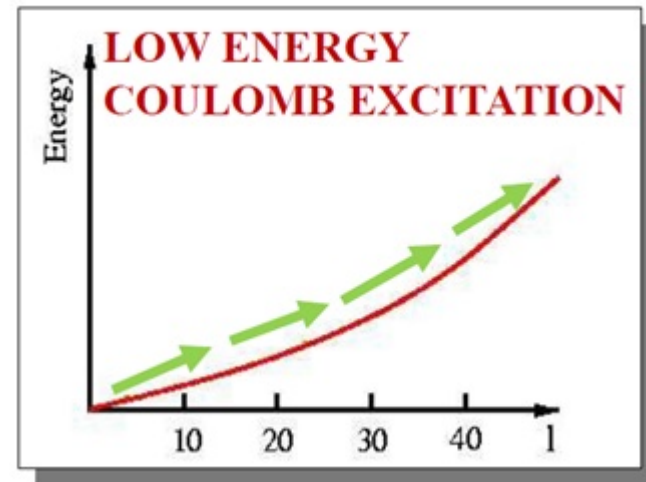
# Heavy ion nuclear reactions



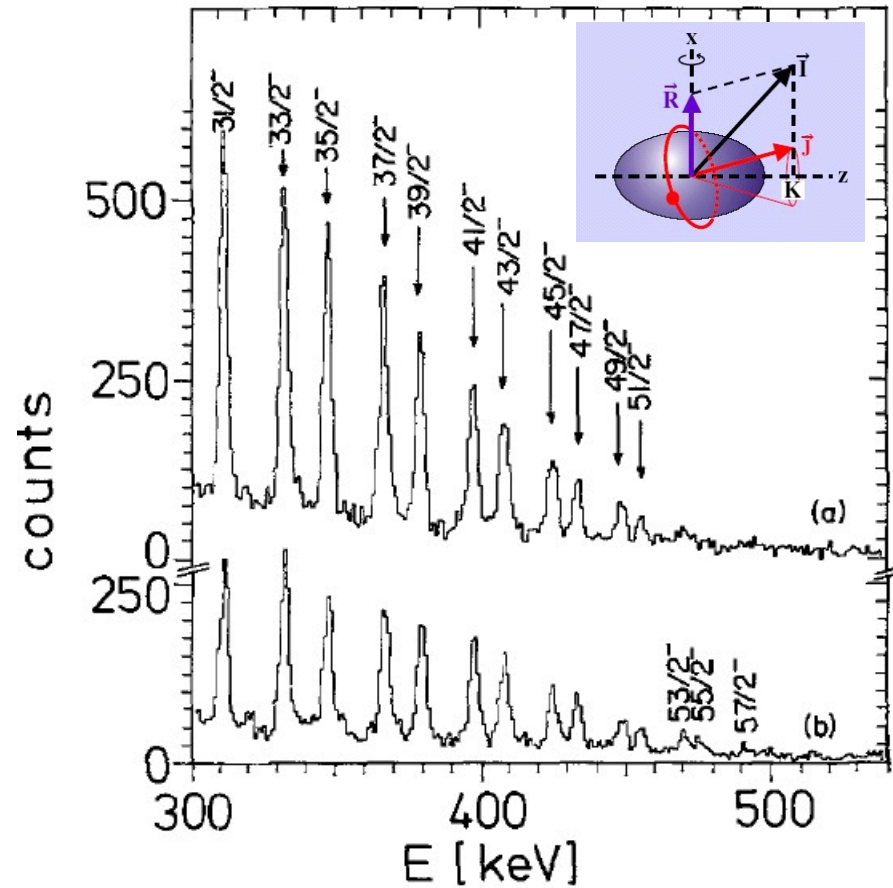
## SIS-18



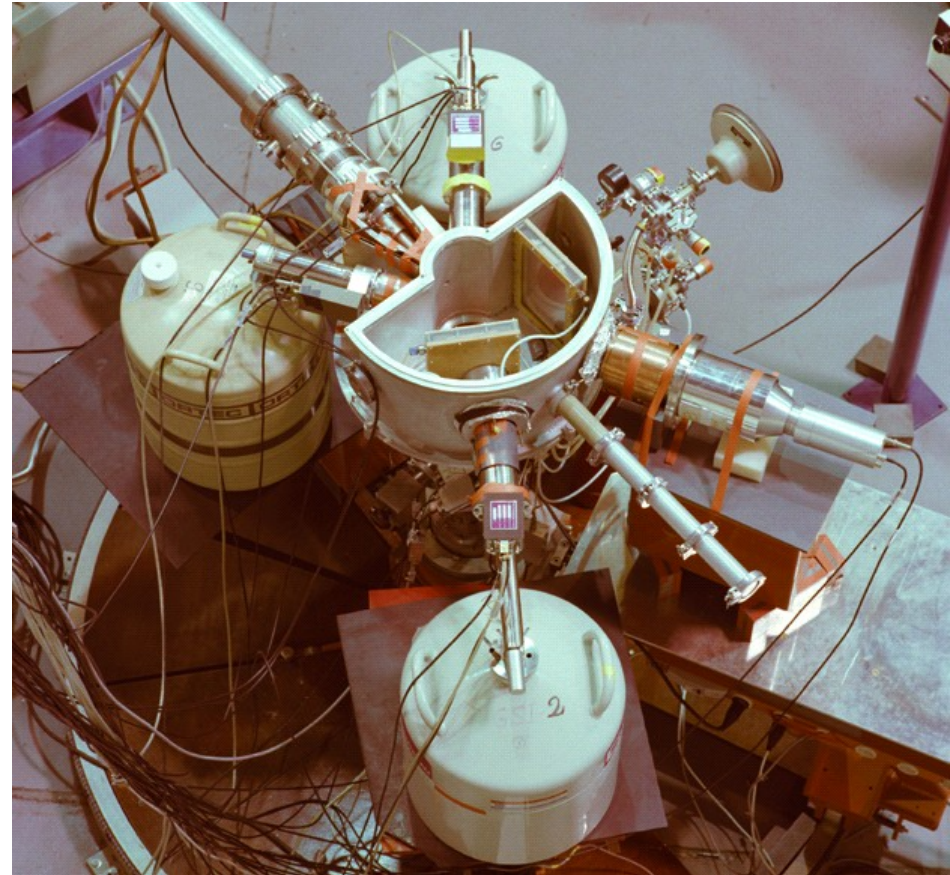
## UNILAC



# First Coulomb excitation experiment at UNILAC 1980



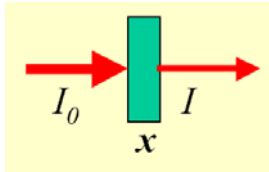
$^{208}\text{Pb} (5.3\text{MeV/u}) \rightarrow ^{235}\text{U}$



Doppler-corrected  $\gamma$ -ray spectrum for  $^{235}\text{U}$

$i_{13/2}$  proton and  $j_{15/2}$  neutron alignment in  $^{235}\text{U}$  and  $^{237}\text{Np}$

# Count rate estimate for UNILAC experiments




$$\begin{aligned} \text{Reaction rate [s}^{-1}] &= \text{luminosity} \cdot \text{cross section [cm}^2] \\ &= \text{projectiles [s}^{-1}] \cdot \text{target nuclei [cm}^{-2}] \cdot \text{cross section [cm}^2] \end{aligned}$$

accelerator current: 1 pA consists of  $6 \cdot 10^9$  projectiles  $[\text{s}^{-1}]$

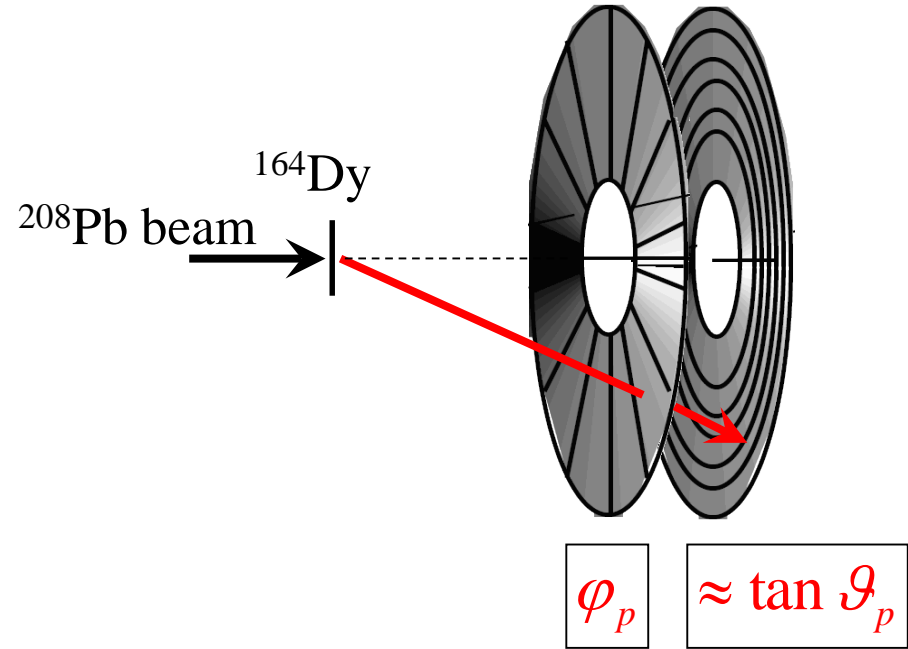
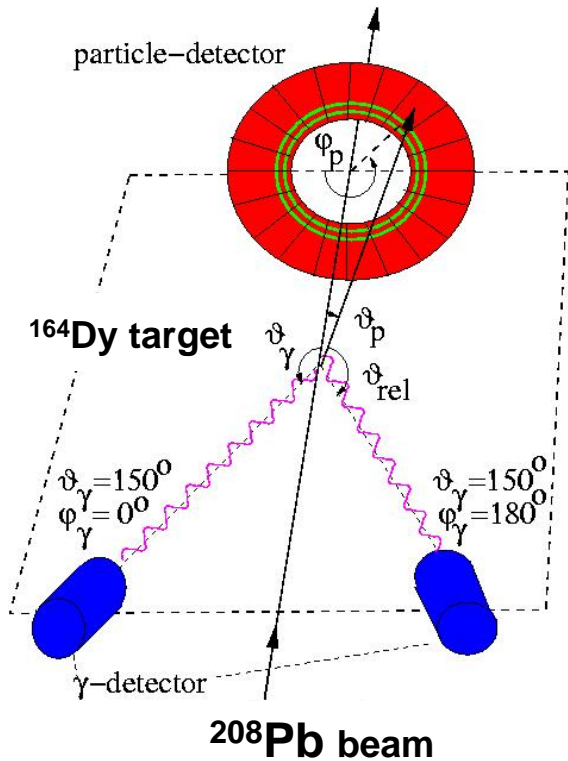
$$\text{target thickness: } 1 \text{ mg/cm}^2 \quad \frac{6 \cdot 10^{23} \cdot 10^{-3} [\text{g/cm}^2]}{A_{\text{target}} [\text{g}]} = \text{target nuclei [cm}^{-2}]$$

$A_{\text{target}}$	target nuclei	projectiles	luminosity $[\text{s}^{-1} \text{ cm}^{-2}]$
200	$3 \cdot 10^{18} [\text{cm}^{-2}]$	$6 \cdot 10^9 [\text{s}^{-1}]$	$18 \cdot 10^{27} [\text{s}^{-1} \text{ cm}^{-2}]$
100	$6 \cdot 10^{18} [\text{cm}^{-2}]$	"	$36 \cdot 10^{27} [\text{s}^{-1} \text{ cm}^{-2}]$
50	$12 \cdot 10^{18} [\text{cm}^{-2}]$	"	$72 \cdot 10^{27} [\text{s}^{-1} \text{ cm}^{-2}]$

beam structure: 50 Hz  duty factor: 25%

present beam structure: 10 Hz  duty factor: 3%

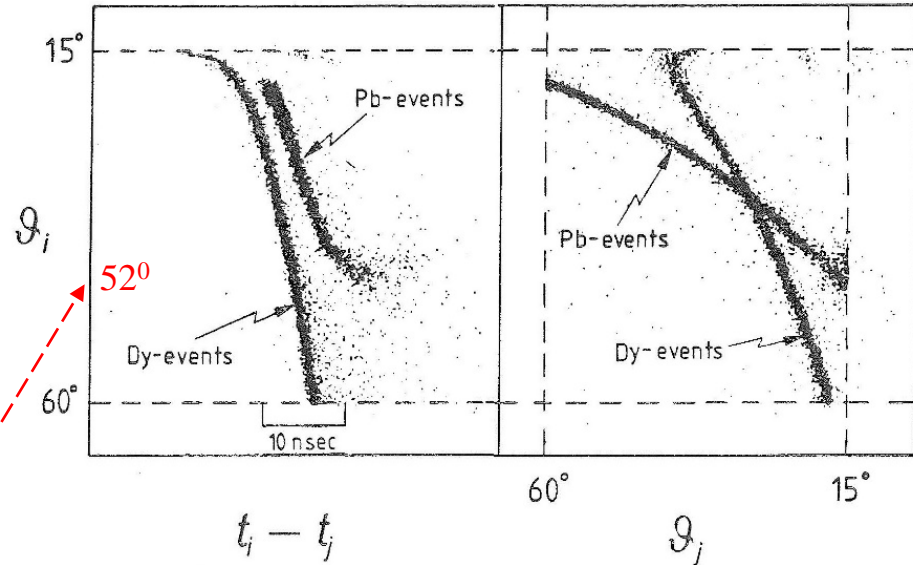
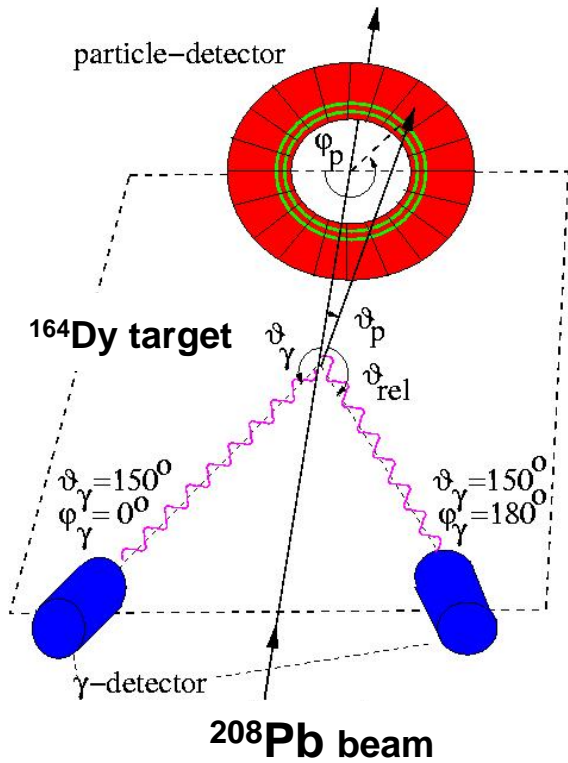
# Coulomb excitation: particle identification



$V_0 \sim 500$  V  
 $p = 5\text{-}10$  Torr  
 gap  $\sim 3$  mm (anode-cathode)

distance target – PPAC: **11 cm**

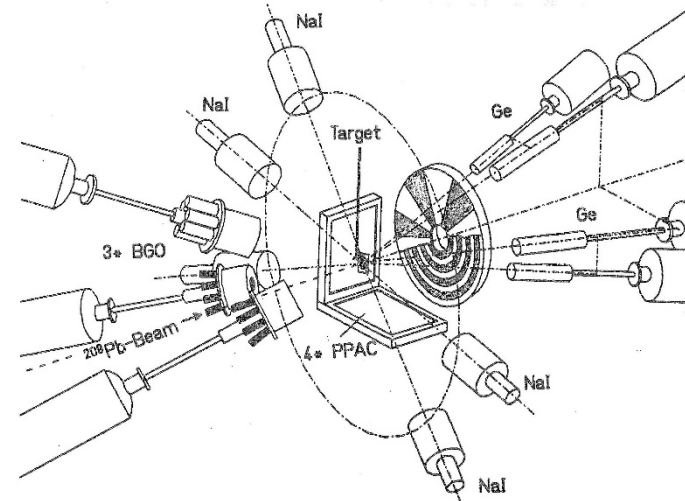
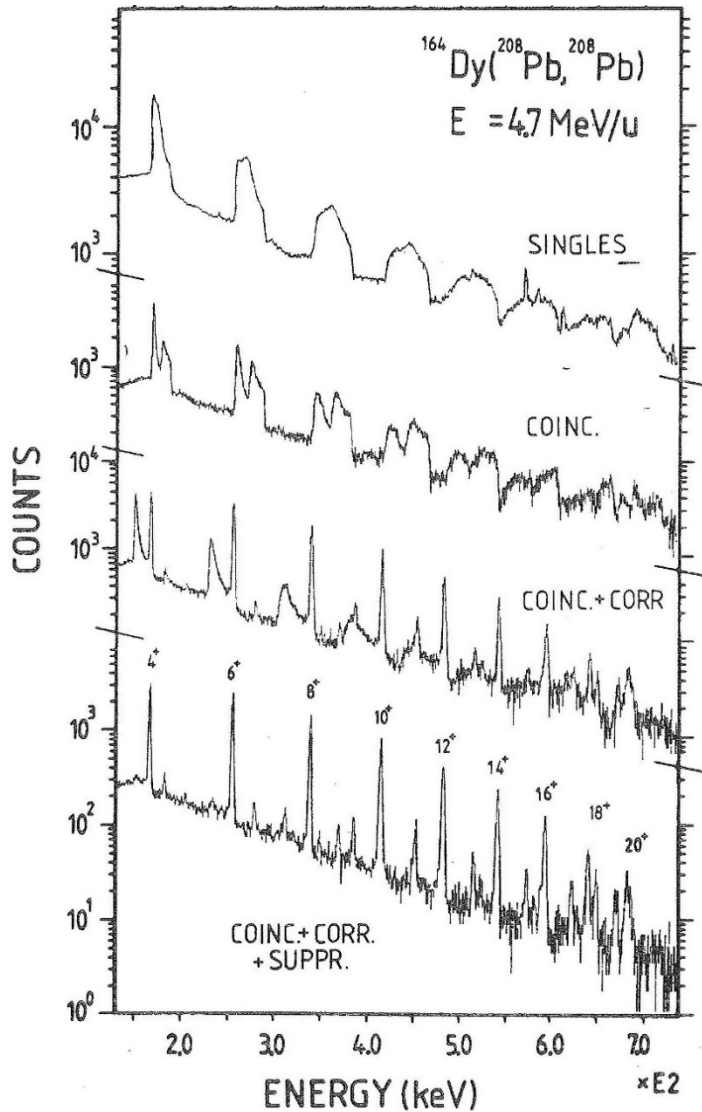
# Coulomb excitation: particle identification



$$\text{max. scattering angle} = \text{arc sin} \frac{A_2}{A_1}$$

distance target – PPAC: **11 cm**

# Doppler shift correction $^{208}\text{Pb} + ^{164}\text{Dy}$ at 978 MeV



$^{164}\text{Dy}$  target nucleus measured with PPAC ( $^{164}\text{Dy}$  target excitation)

index 1  $\equiv$  projectile ( $^{208}\text{Pb}$ )      index 2  $\equiv$  target nucleus ( $^{164}\text{Dy}$ )

$$v_{cm} = 0.04634 \cdot (1 + A_2 / A_1)^{-1} \sqrt{E_{lab} / A_1} \quad (=0.02746)$$

$$v_2 = 2 \cdot v_{cm} \cdot \cos \mathcal{G}_2$$

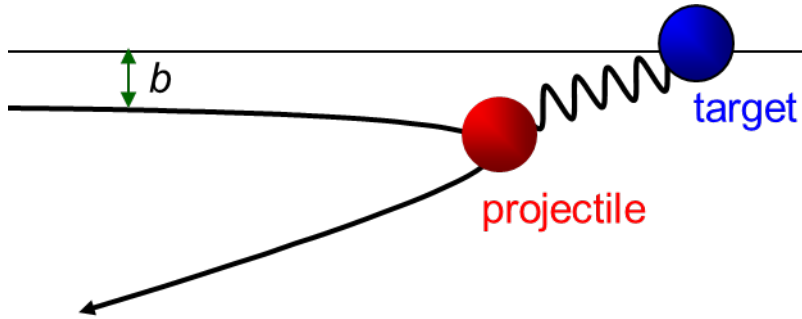
$$\cos \mathcal{G}_{\gamma 2} = \cos \mathcal{G}_\gamma \cdot \cos \mathcal{G}_2 + \sin \mathcal{G}_\gamma \cdot \sin \mathcal{G}_2 \cdot \cos(\varphi_\gamma - \varphi_2)$$

$$\cos(\varphi_\gamma - \varphi_2) = \cos \varphi_\gamma \cdot \cos \varphi_2 + \sin \varphi_\gamma \cdot \sin \varphi_2$$

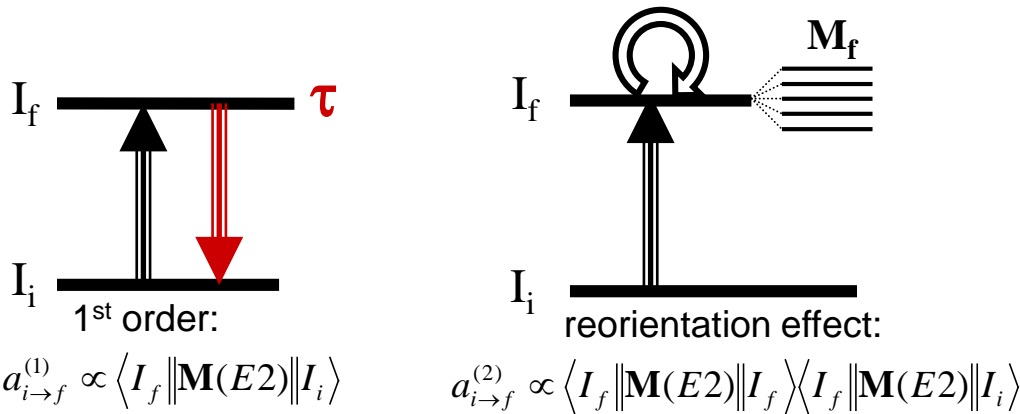
$$\frac{E_{\gamma 0}}{E_\gamma} = \frac{1 - v_2 \cdot \cos \mathcal{G}_{\gamma 2}}{\sqrt{1 - v_2^2}}$$



# The reorientation effect at backward angles

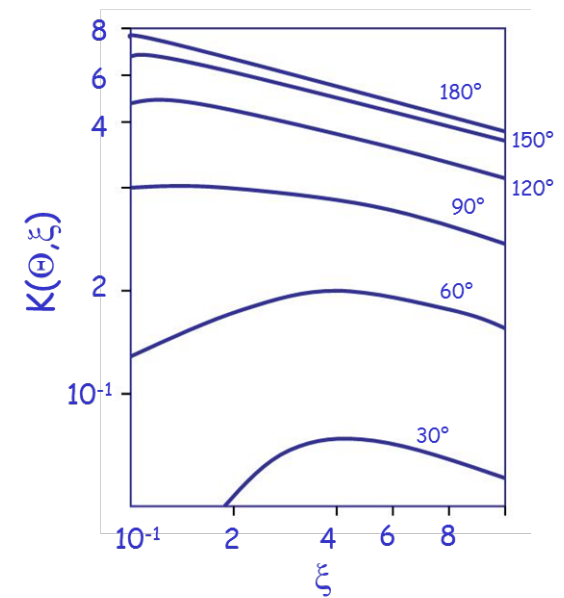


The excitation cross section is a direct measure of the  $E\lambda$  matrix elements.



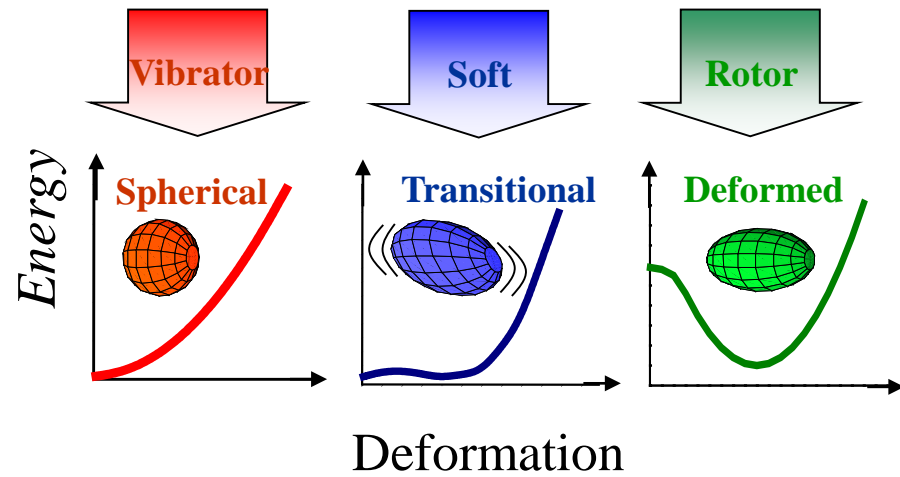
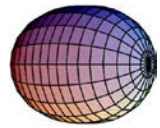
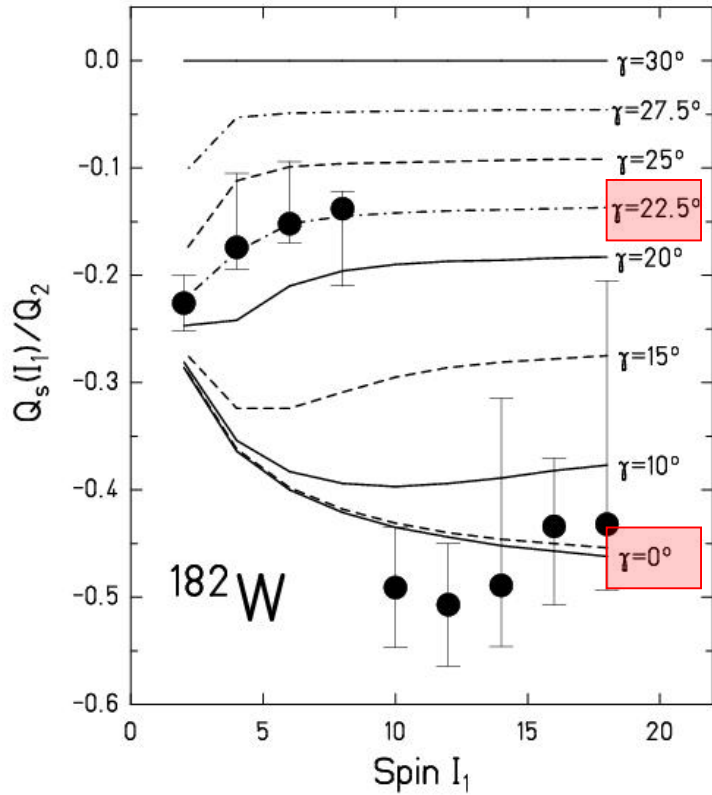
$$Q_s(2^+) = -\sqrt{\frac{2\pi}{7} \frac{4}{5}} \cdot \langle 2 \| M(E2) \| 2 \rangle$$

$$P_{0 \rightarrow 2}^{(2)}(\theta, \xi) = P_{0 \rightarrow 2}^{(1)}(\theta, \xi) \cdot \left[ 1 + \sqrt{\frac{7}{2\pi}} \frac{5}{4} \cdot \frac{A_p}{Z_p} \cdot \frac{\Delta E}{1 + A_p/A_t} \cdot Q_s(2) \cdot K(\theta, \xi) \right]$$



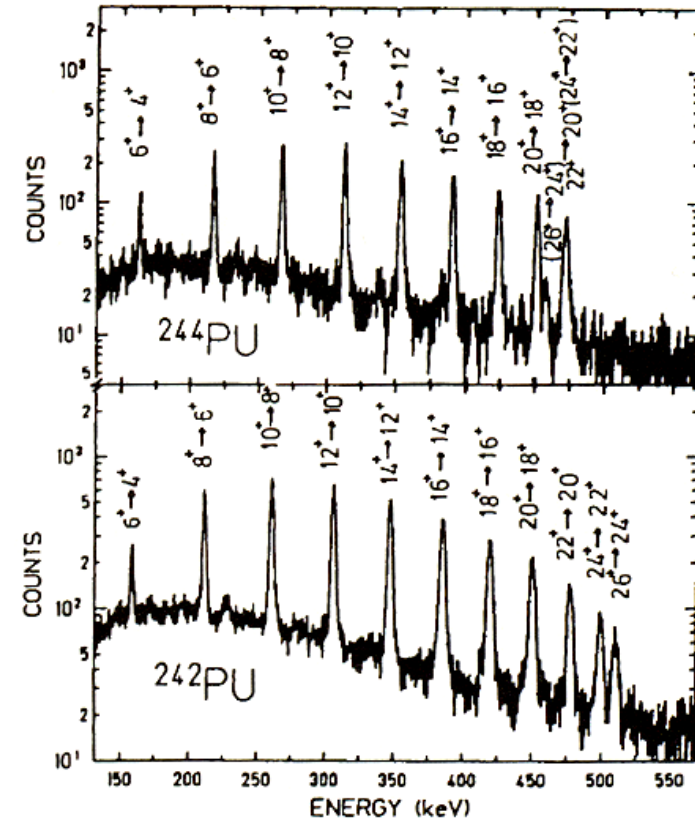
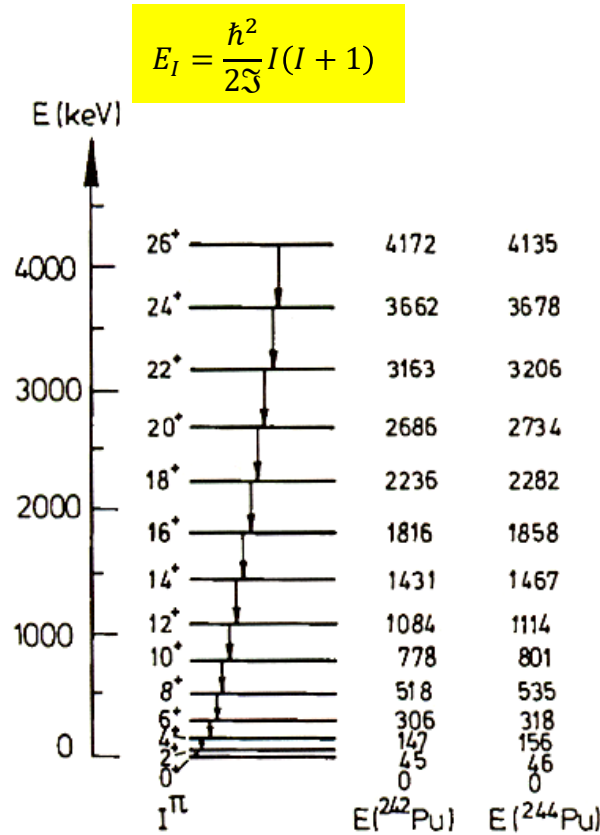
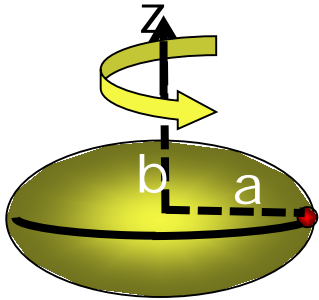
# Quadrupole deformation in $^{182,184,186}\text{W}$

<b>W176</b> 2.5 h 0+	<b>W177</b> 135 m (1/2-)	<b>W178</b> 21.6 d 0+	<b>W179</b> 37.05 m (7/2-)*	<b>W180</b> 0+	<b>W181</b> 121.2 d 9/2+	<b>W182</b> 0+	<b>W183</b> 1.1E+17 y 1/2-*	<b>W184</b> 3E+17 y 0+	<b>W185</b> 75.1 d 3/2-*	<b>W186</b> 0+	<b>W187</b> 23.72 h 3/2-	<b>W188</b> 69.4 d 0+	<b>W189</b> 11.5 m (3/2-)	<b>W190</b> 30.0 m 0+
EC	EC	EC	EC	0.13	EC	26.3	14.3	30.67	$\beta^-$	28.6	$\beta^-$	$\beta^-$	$\beta^-$	$\beta^-$
<b>Ta175</b> 10.5 h 7/2+	<b>Ta176</b> 8.09 h (1)-*	<b>Ta177</b> 56.56 h 7/2+	<b>Ta178</b> 9.31 m 1+	<b>Ta179</b> 1.82 y 7/2+*	<b>Ta180</b> 8.152 h 1+ EC, $\beta^-$ <sub>0.012</sub> *	<b>Ta181</b> 7/2+	<b>Ta182</b> 114.43 d 3-*	<b>Ta183</b> 5.1 d 7/2+	<b>Ta184</b> 8.7 h (5-)	<b>Ta185</b> 49.4 m (7/2+)	<b>Ta186</b> 10.5 m 2,3	<b>Ta187</b>	<b>Ta188</b>	116
EC	EC	EC	EC	EC	99.988	$\beta^-$	$\beta^-$	$\beta^-$	$\beta^-$	$\beta^-$	$\beta^-$			
<b>Hf174</b> 2.0E15 y 0+	<b>Hf175</b> 70 d 5/2-	<b>Hf176</b>	<b>Hf177</b>	<b>Hf178</b>	<b>Hf179</b>	<b>Hf180</b>	<b>Hf181</b> 42.39 d 1/2-	<b>Hf182</b> 9E6 y 0+*	<b>Hf183</b> 1.067 h (3/2-)	<b>Hf184</b> 4.12 h 0+	<b>Hf185</b> 3.5 m	<b>Hf186</b> 0+		
$\alpha$ 0.162	EC	5.206	18.606	27.297	13.629	35.100	$\beta^-$	$\beta^-$	$\beta^-$	$\beta^-$	$\beta^-$			



R. Kulesa et al., Phys. Lett. B218 (1989), 421

# Alignment of $i_{13/2}$ protons in $^{242,244}\text{Pu}$



$E_\gamma = E_I - E_{I-2} = \frac{\hbar^2}{2\mathfrak{S}} (4I - 2)$

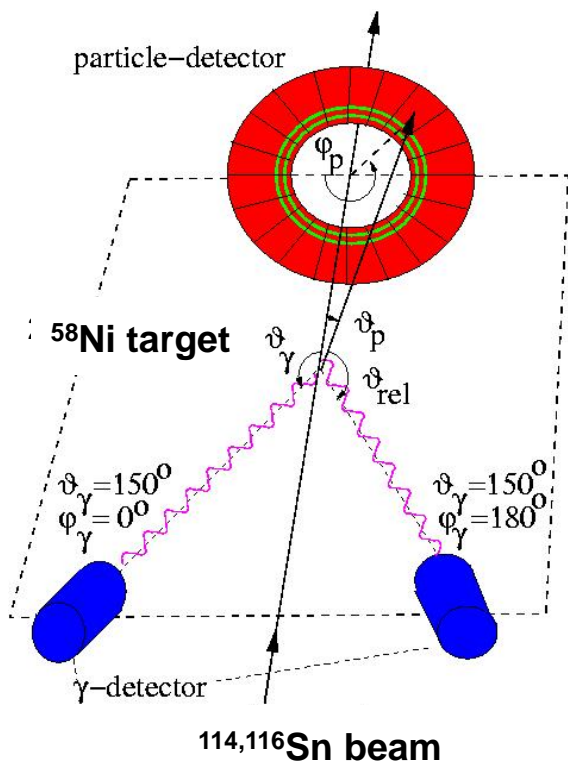
$\mathfrak{S} = \frac{2}{5} A \cdot M \cdot R_0^2 \cdot \beta^2$

$B(E2; I \rightarrow I-2) = \frac{15}{32\pi} \frac{I(I+1)}{(2I-1)(2I+1)} \cdot Q_2$

$Q_2 = \frac{3ZR_0^2}{\sqrt{5}\pi} \cdot \beta$

❖ analysis with GOSIA code

# Coulomb excitation of $^{114}\text{Sn}$ projectile excitation



**natural abundance of  $^{114}\text{Sn}$ : 0.65%**

$^{114,116}\text{Sn} \rightarrow ^{58}\text{Ni}$  at 3.6 MeV/u

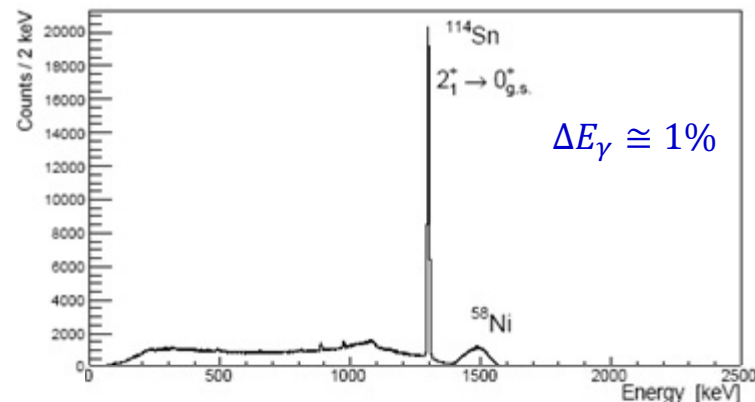
$$E_x = 1300, 1294 \text{ MeV}$$

$$B(E2) \uparrow = 0.25(5), 0.209(5) e^2 b^2$$

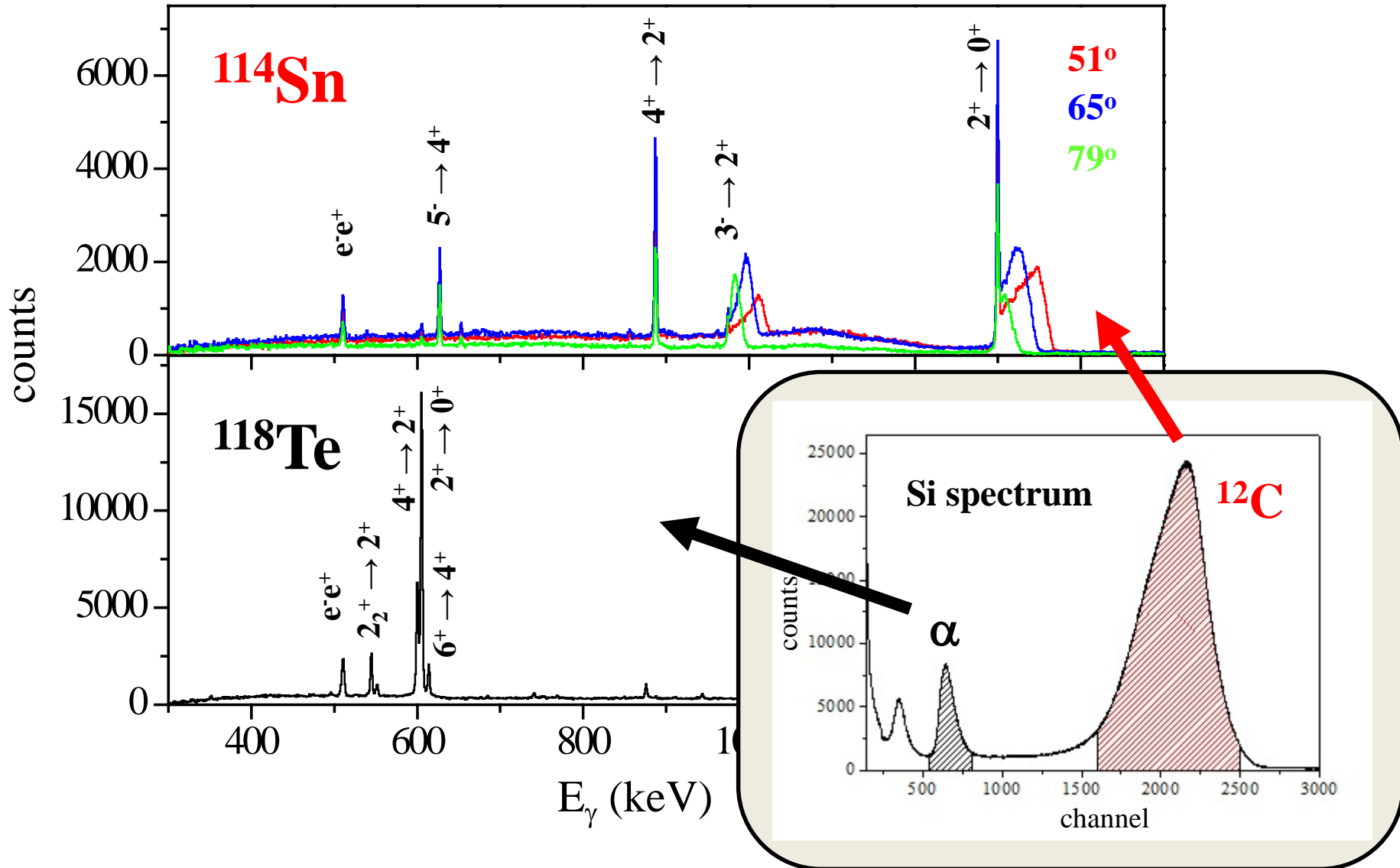
$\gamma$ -efficiency = 0.005  
 accelerator duty factor = 10%

beam intensity = 1 pA  
 target thickness = 1 mg/cm<sup>2</sup>

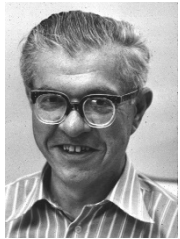
**py-rate (Sn) = 1/s**



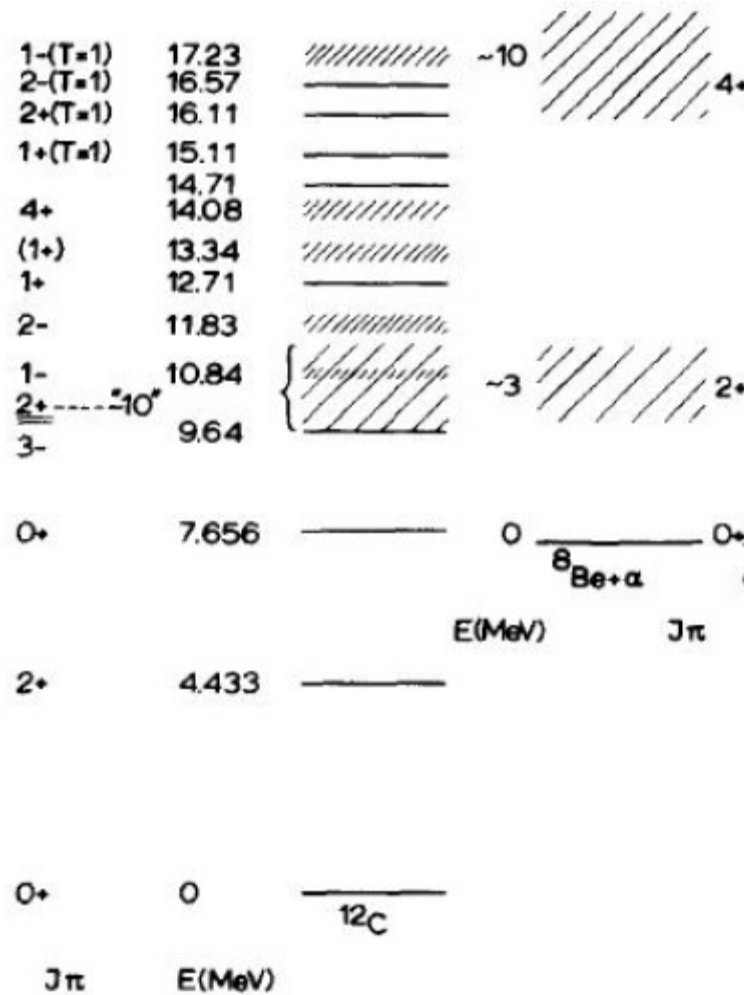
# $\alpha$ -transfer reactions



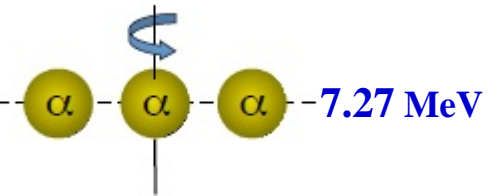
# $\alpha$ -clustering in $^{12}\text{C}$



Fred Hoyle 1953

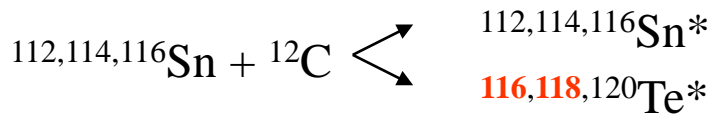


Haruhiko Morinaga  
1956



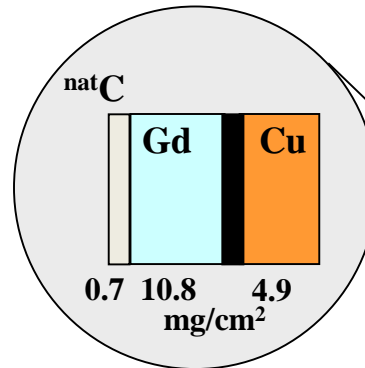
2.4 MeV per bound

# $\alpha$ -transfer experiment



$$456 \text{ MeV} \rightarrow \theta_{1/4}^{cm} = 115.5^\circ$$

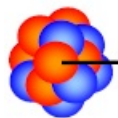
$$\zeta_{1/4}^{lab}({}^{12}_6\text{C}) = 32.2^\circ$$



4 Euroball Cluster at  $\pm 65^\circ$

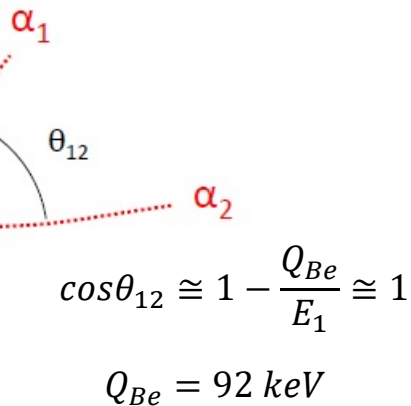
delayed breakup

$${}^8\text{Be } 0^+ \tau \sim 10^{-15} \text{ s}$$



target

${}^{12}\text{C}$  projectile

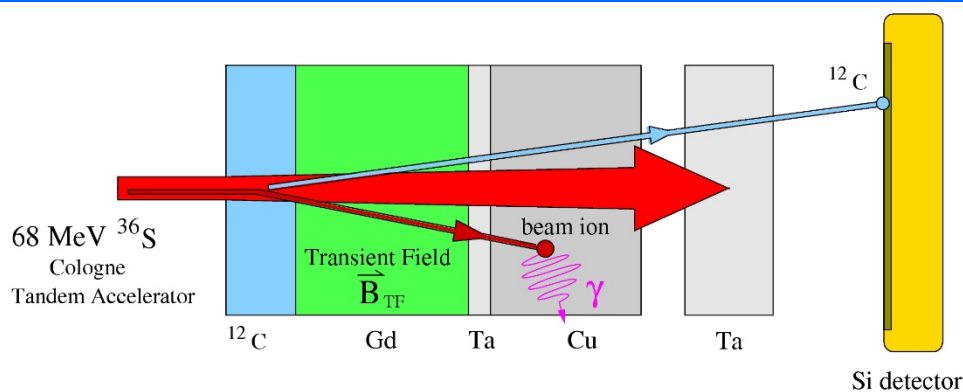


$$E_{rel} = \frac{m_2 E_1 + m_1 E_2 - 2\sqrt{m_1 E_1 m_2 E_2} \cdot \cos\theta_{12}}{m_1 + m_2}$$

${}^{112,114,116}\text{Sn}$   
 @ 4 MeV/u

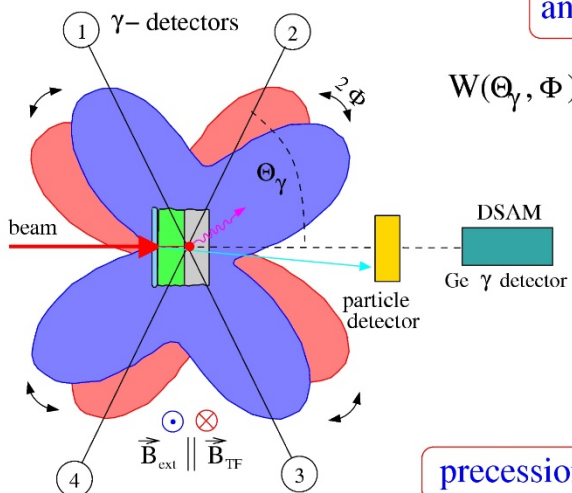
recoil detection  
 $23^\circ \leq \Theta \leq 38^\circ$

# Transient magnetic fields g-factor measurement



angular correlation

$$W(\Theta_\gamma, \Phi) = \sum_{k=0,2,4,\dots}^{k_{\text{max}}} Q_k \cdot A_k \cdot P_k(\cos(\Theta_\gamma \pm \Phi))$$

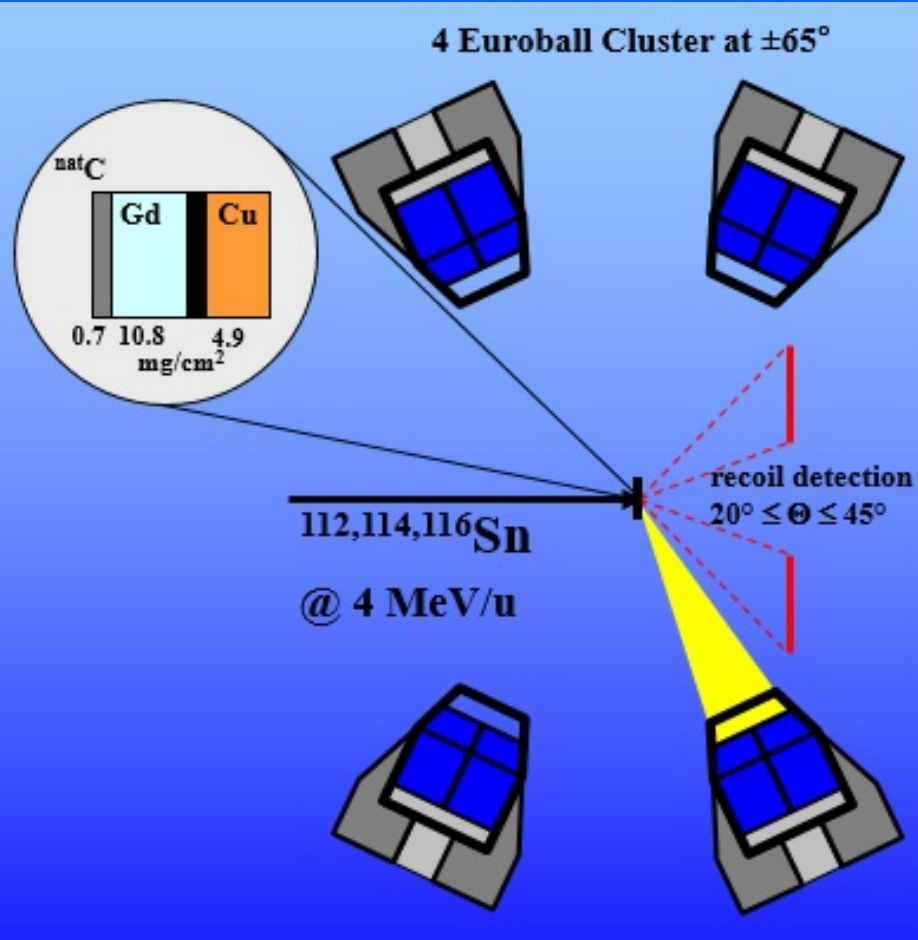


double ratio:

$$\text{DR}(1/4) = \frac{N_{1\uparrow} \cdot N_{4\downarrow}}{N_{1\downarrow} \cdot N_{4\uparrow}}$$

precession angle

$$\Phi = \frac{\sqrt{\text{DR}} - 1}{\sqrt{\text{DR}} + 1} \bigg/ \frac{1}{W} \cdot \frac{dW}{d\Theta} \bigg|_{\Theta_\gamma} = g \frac{\mu_N}{\hbar} \int_{t_{\text{in}}}^{t_{\text{out}}} B_{\text{TF}}(v_{\text{ion}}) e^{-t/\tau} dt$$



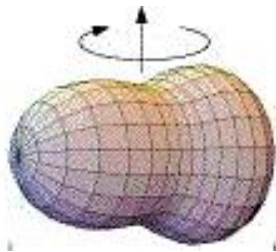


# Space inversion invariance: octupole deformed nucleus $^{226}\text{Ra}$

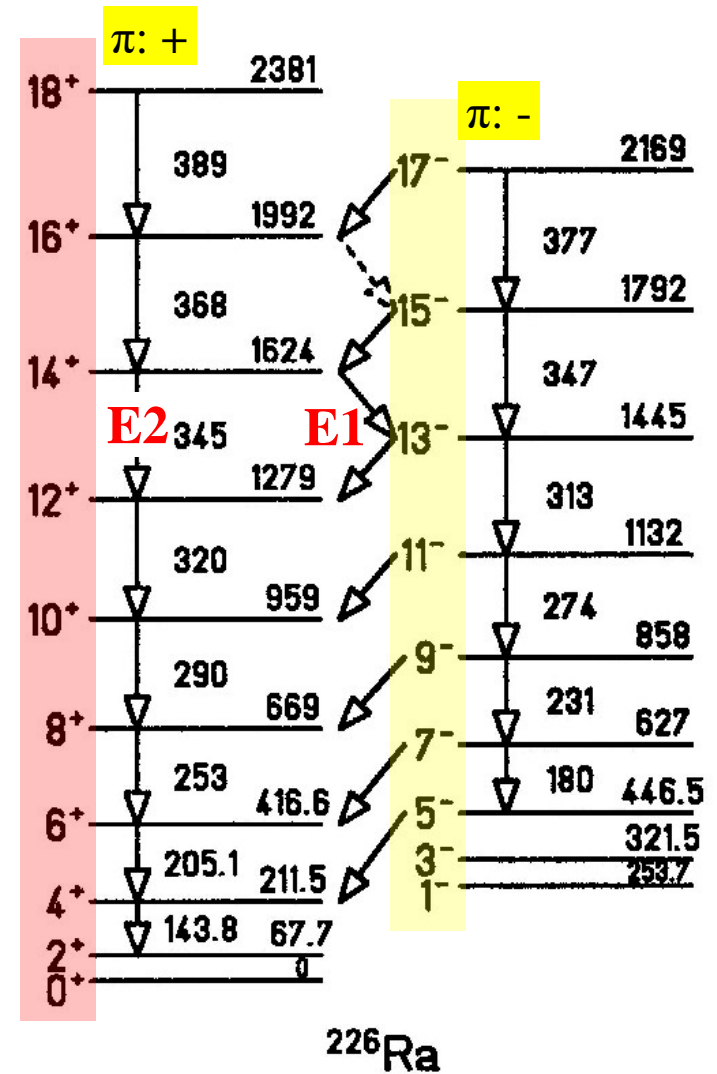
$$|\Psi\rangle = |\text{shape}\rangle$$

$$P|\Psi\rangle = |\text{shape}\rangle$$

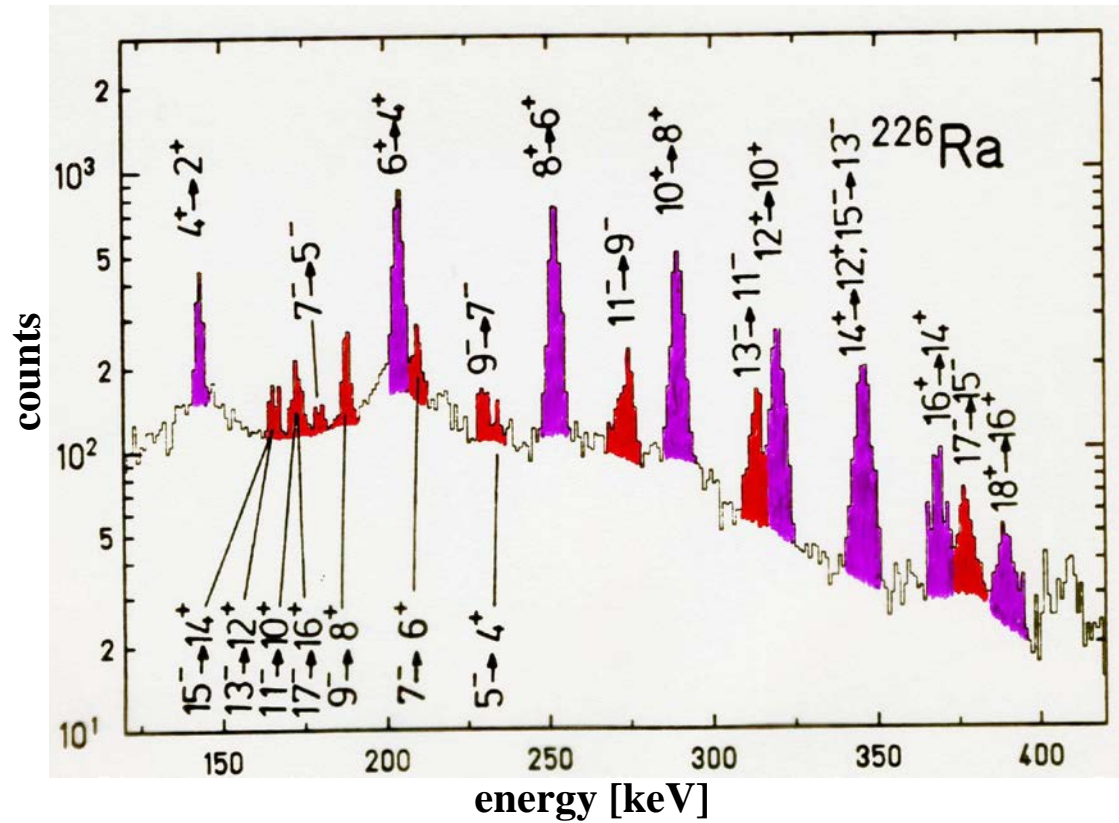
$$P|\Psi\rangle \neq |\Psi\rangle$$



rotation



# Coulomb excitation of $^{226}\text{Ra}$



$^{208}\text{Pb} \rightarrow ^{226}\text{Ra}$

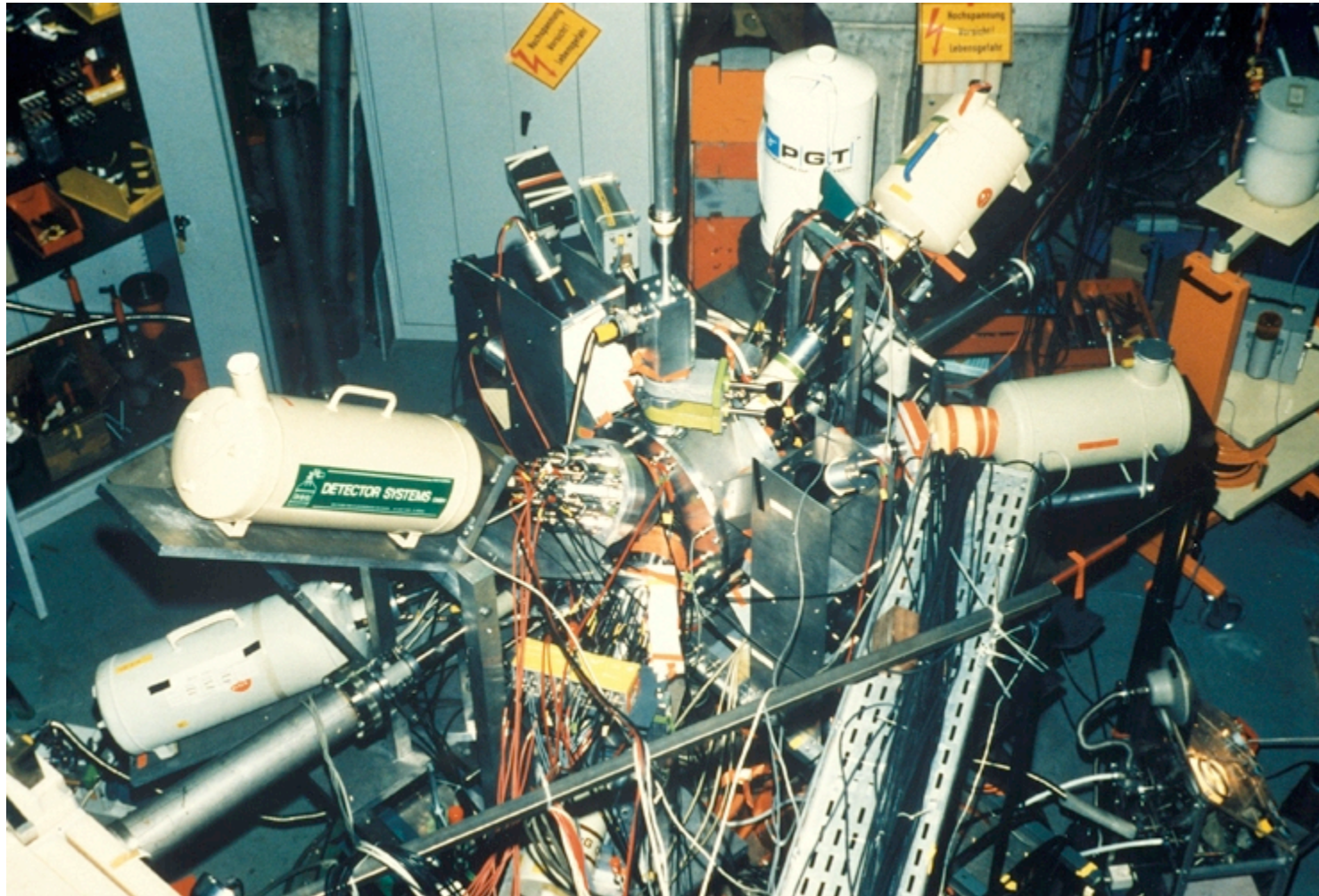
$E_{\text{lab}} = 4.7 \text{ A MeV}$

$15^\circ \leq \theta_{\text{lab}} \leq 45^\circ$

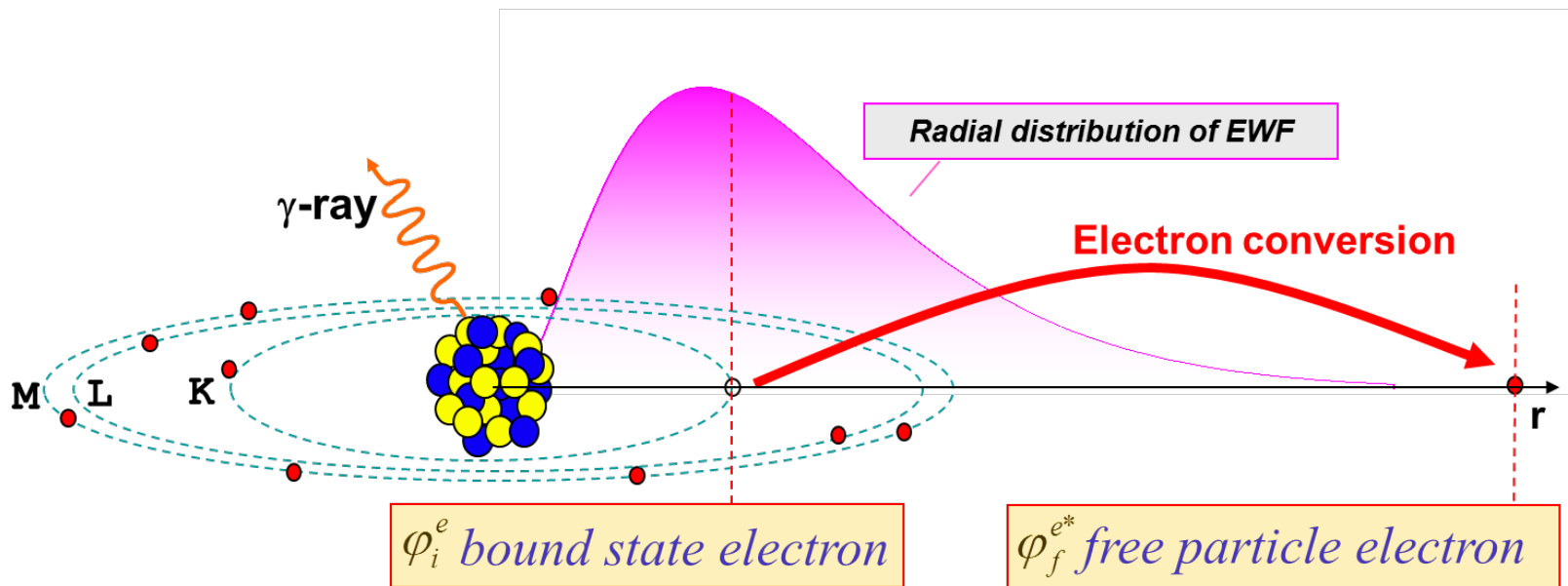
$0^\circ \leq \phi_{\text{lab}} \leq 360^\circ$

**$^{226}\text{Ra}$  target broken after 8 hours**

# Coulomb excitation of $^{226}\text{Ra}$ 1992



# Conversion electrons



- ❖ For an electromagnetic transition internal conversion can occur instead of emission of gamma radiation. In this case the transition energy  $Q = E_\gamma$  will be transferred to an electron of the atomic shell.

$$T_e = E_\gamma - B_e$$

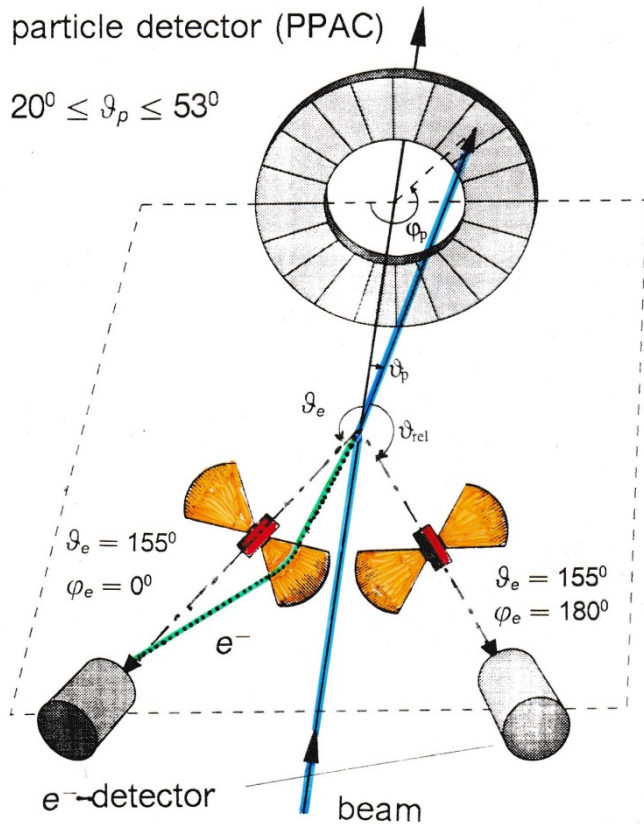
$T_e$ : kinetic energy of the electron  
 $B_e$ : binding energy of the electron

internal conversion is important for:

- heavy nuclei  $\sim Z^3$
- high multiplicities  $El$  or  $Ml$
- small transition energies

$$\alpha_k(El) \propto Z^3 \left( \frac{L}{L+1} \right) \left( \frac{2m_e c^2}{E} \right)^{L+5/2}$$

# Electron spectroscopy with Mini-Orange devices



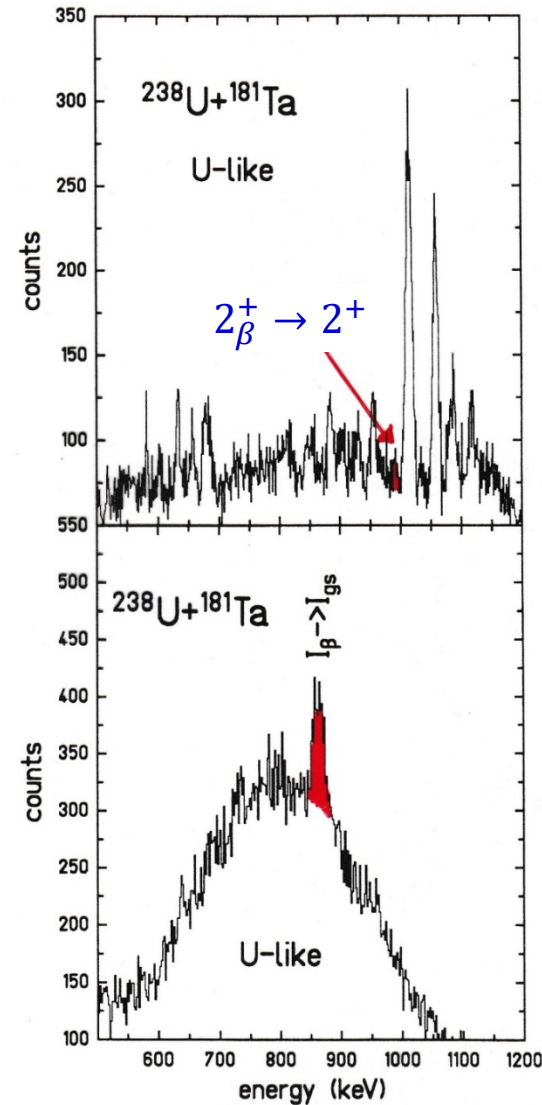
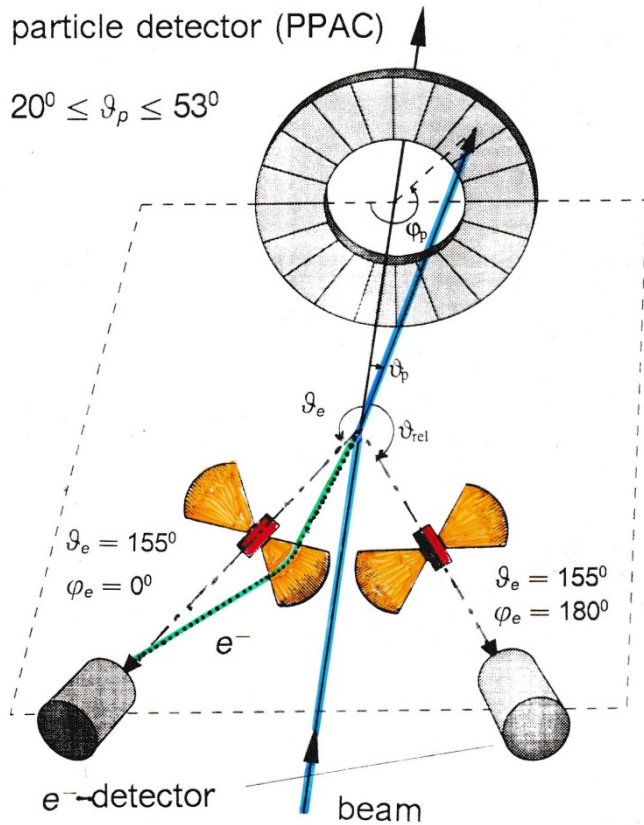
$\Delta\vartheta_e = 20^\circ$   
 target – Mini-Orange: 19 cm  
 Mini-Orange – Si detector: 6 cm

Doppler correction for projectile excitation:

$$T_e^* = \gamma \cdot T_e \cdot \left\{ 1 - \beta_1 \cdot \sqrt{1 + 2m_e c^2 / T_e} \cdot \cos\theta_{e1} \right\} + m_e c^2 \cdot (\gamma - 1)$$

$$\cos\theta_{e1} = \cos\vartheta_1 \cos\vartheta_e + \sin\vartheta_1 \sin\vartheta_e \cos(\varphi_e - \varphi_1)$$

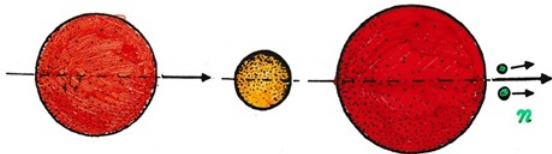
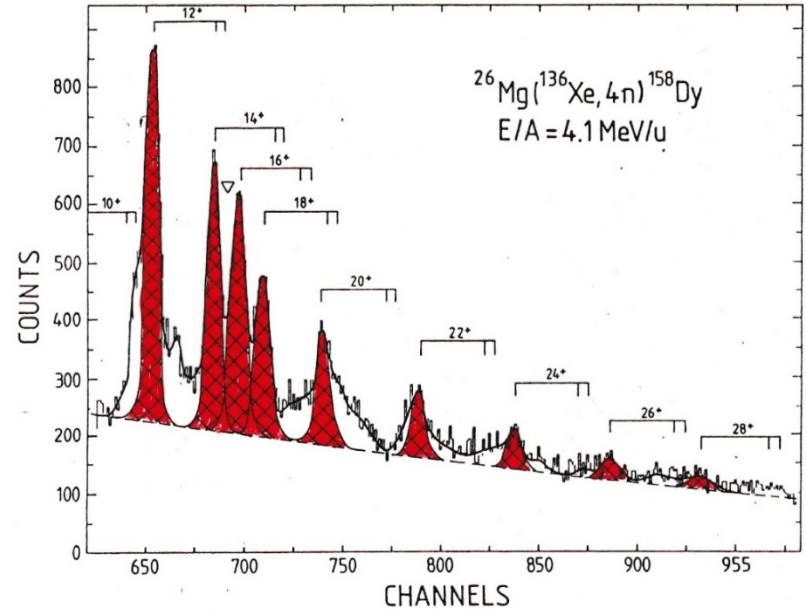
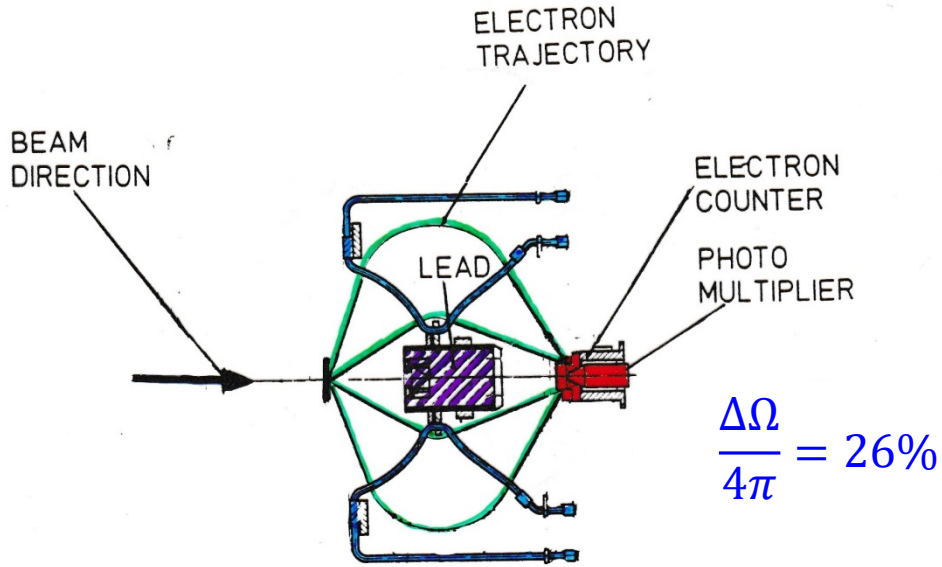
# Doppler-corrected e<sup>-</sup> and γ-ray spectra



γ-ray spectrum

e<sup>-</sup> spectrum

# Electron spectroscopy



$$\vartheta_c = 0^0$$

$$\beta_c = \beta_{cm} = 0.079$$

resolution of the spectrometer  
including Doppler correction  
as calculated for a point source

$$\left(\frac{\Delta p}{p}\right)_e / \%$$

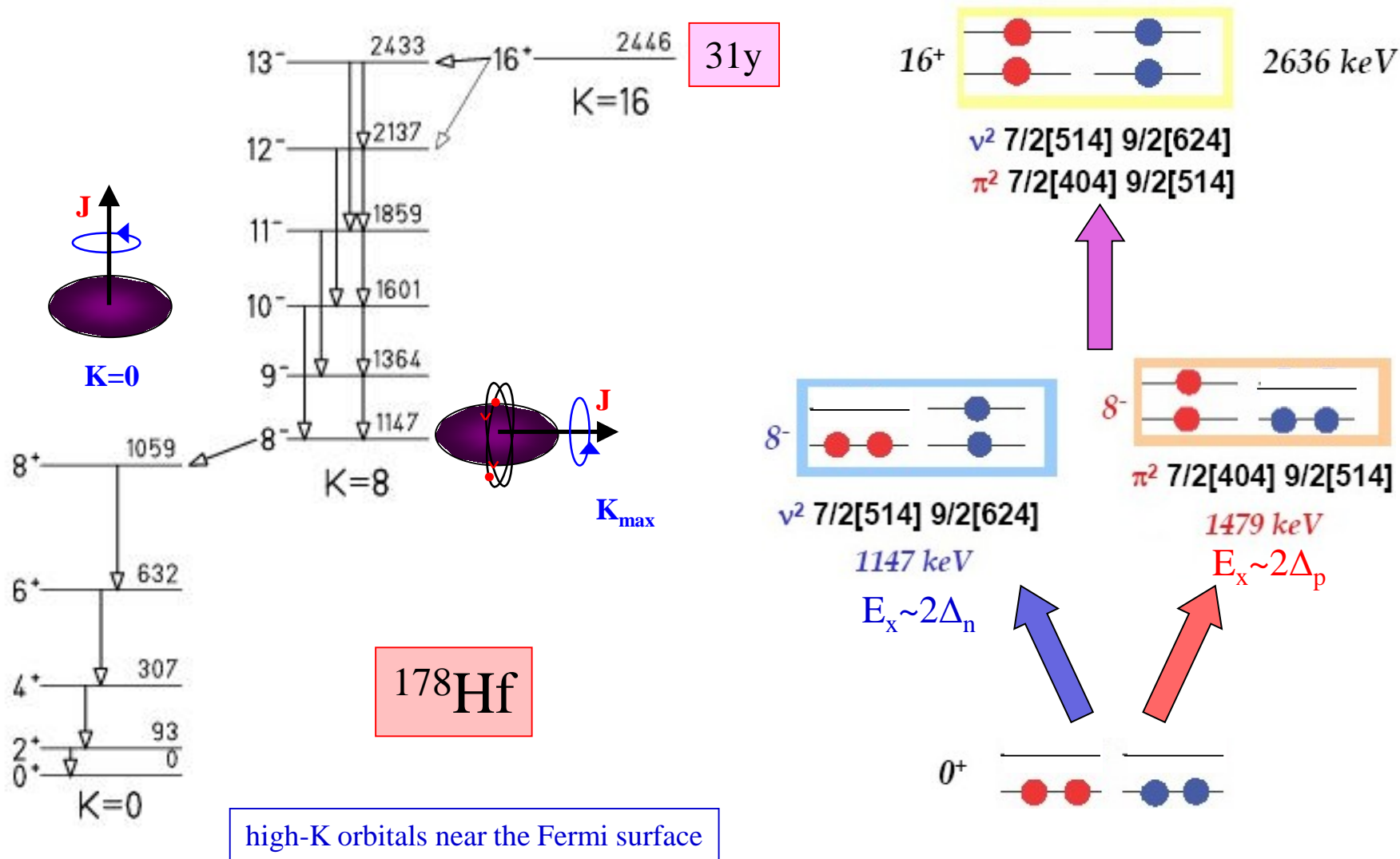
0.4

scattering in the target (i) 0.004  
beam optics (ii) 0.11  
evaporation of neutrons (iii) 0.09  
energy loss in the target (iv) 0.31  
energy straggling of the projectiles (v) 0.006

quadratic sum  
experimental resolution

0.53  
0.56 %

# Nuclear structure of $^{178}\text{Hf}$

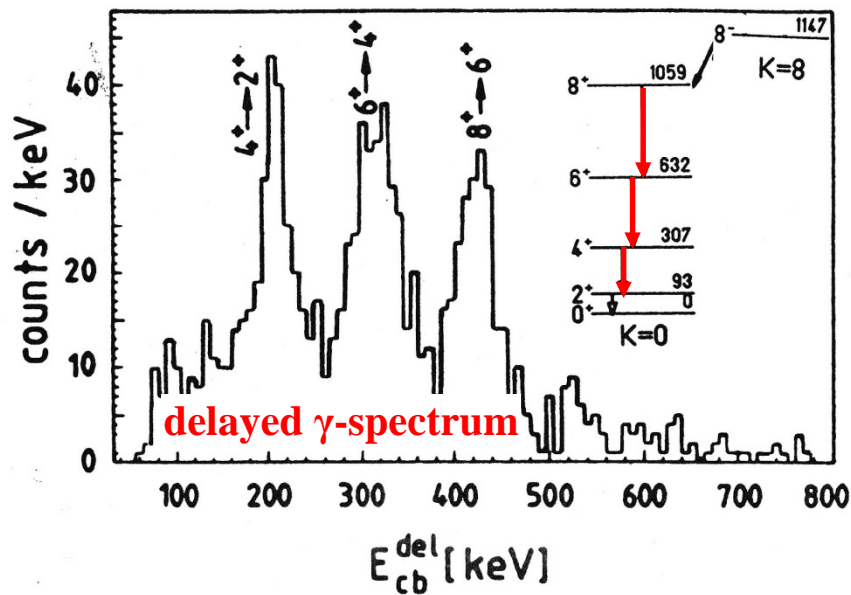


$$\nu: f_{7/2} i_{13/2} \quad \pi: h_{11/2} g_{7/2}$$



# Coulomb excitation of the $K = 8^-$ isomer in $^{178}\text{Hf}$

➤  $^{178}\text{Hf} + ^{130}\text{Te}$  at 560, 590, 620 MeV



4 s  $\rightarrow M_{30} (E3)$

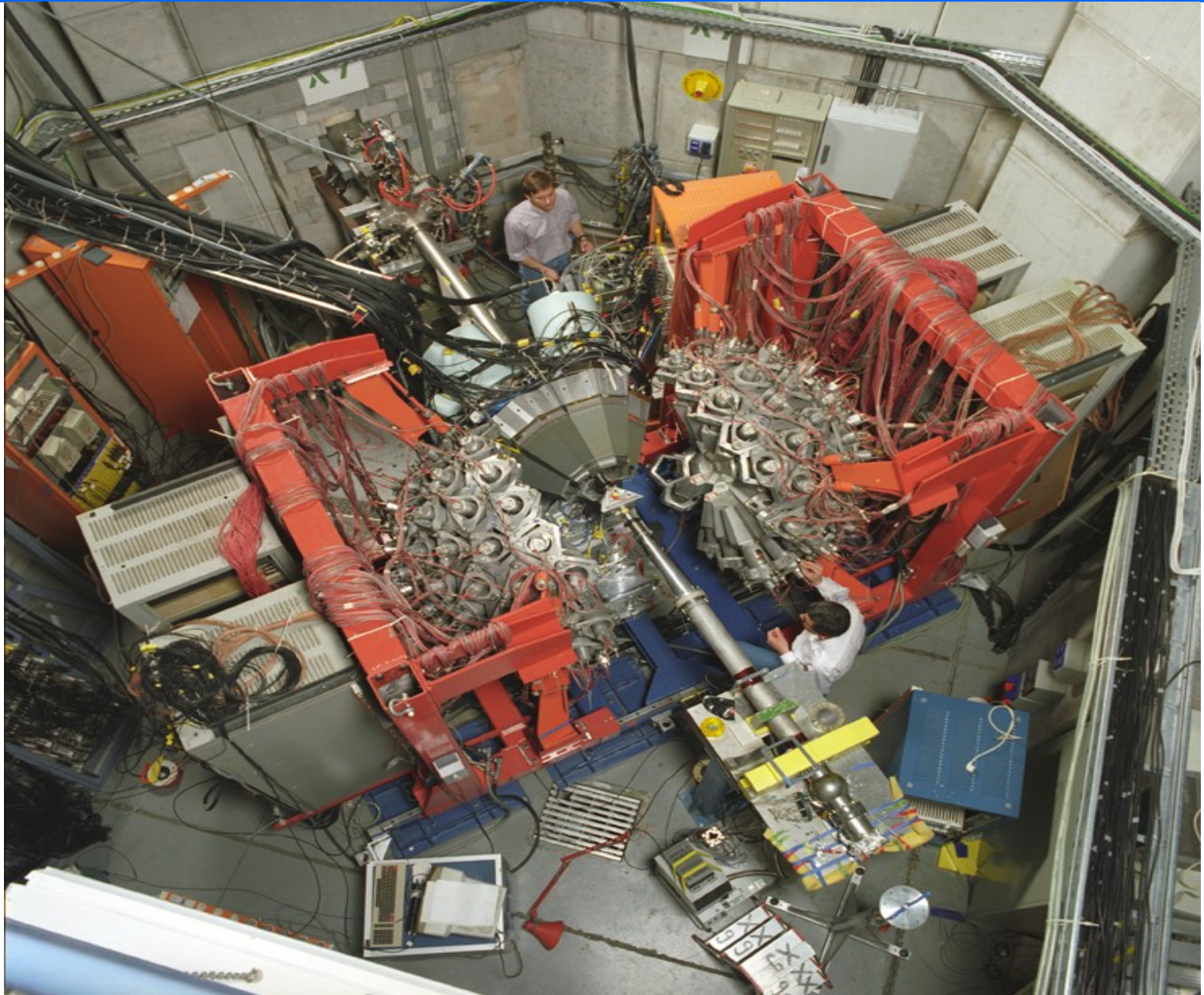


Darmstadt Heidelberg  
Crystal Ball

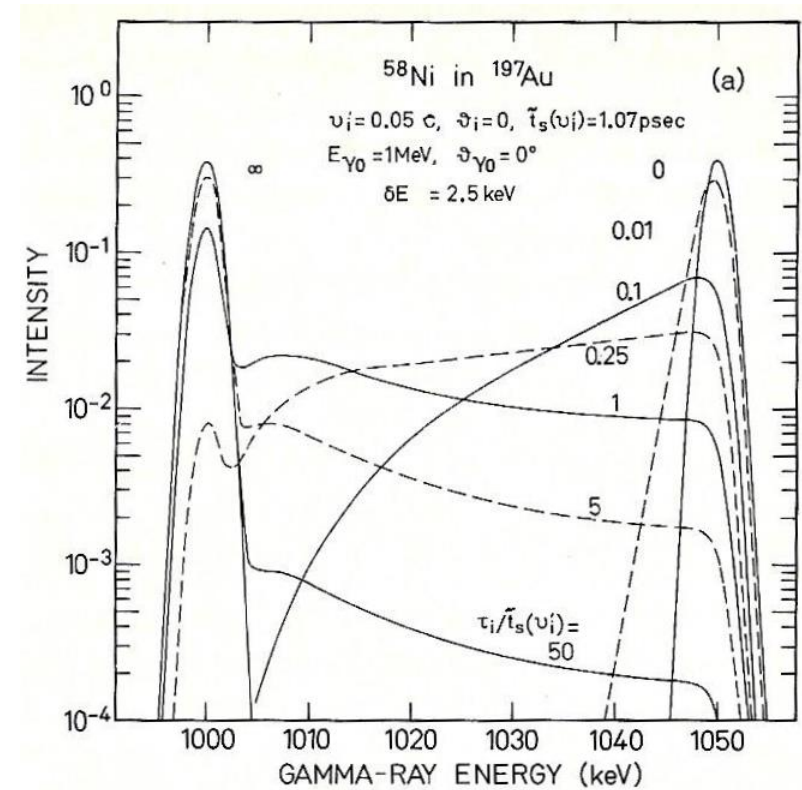
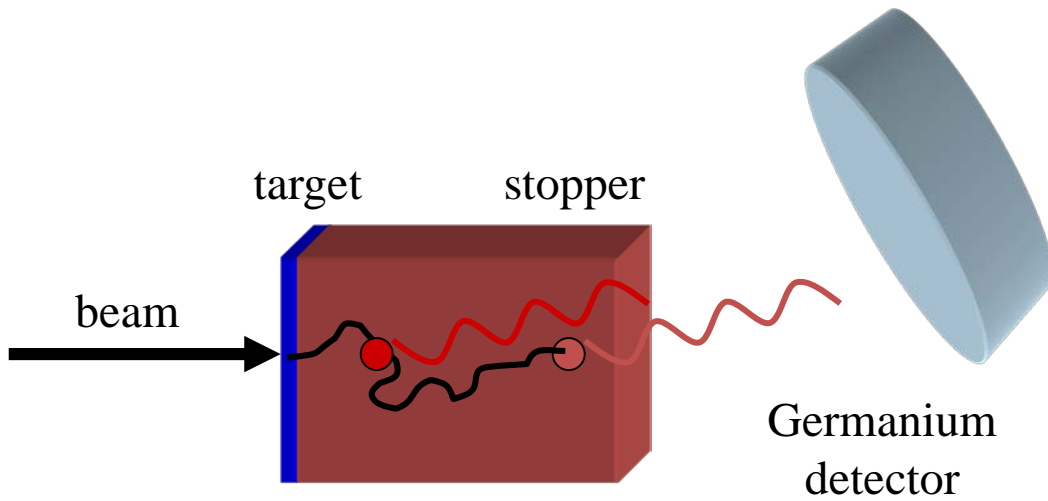
$$\Delta E_{\gamma} = 90 \text{ keV}$$

Delayed  $\gamma$ -ray spectrum of the Crystal Ball with  $850 \text{ keV} \leq E_{sum}^{del} \leq 1100 \text{ keV}$  and  $3 \leq N_{det} \leq 6$ . In addition at least one of the delayed  $\gamma$ -rays must have been detected in one of the Ge-detectors.

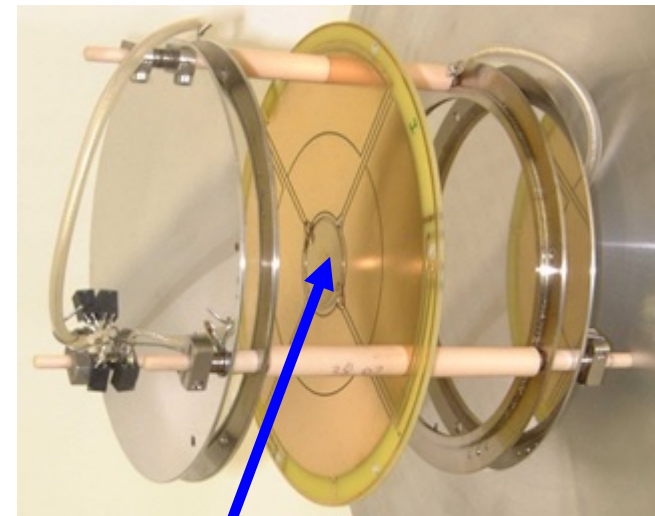
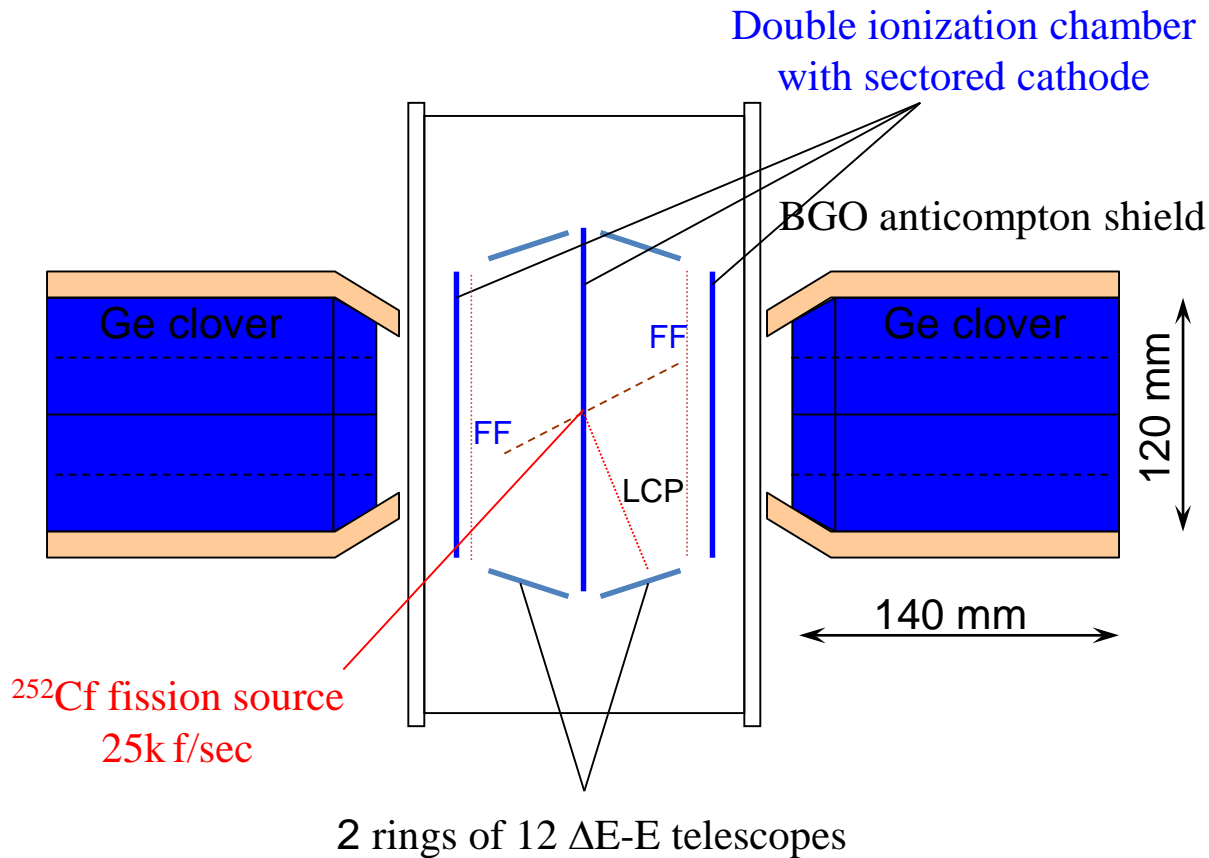
# Darmstadt-Heidelberg Crystal Ball and EUROBALL-3 demonstrator 1993



# Doppler shift attenuation method



# Spectroscopy of binary and ternary fission fragments



$^{252}\text{Cf}$  source (25k f/s)

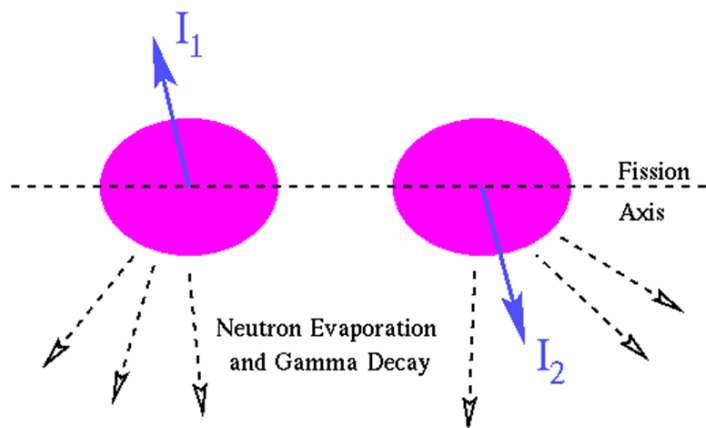
$T_{1/2} = 2.645\text{y}$

$E_{\alpha} = 6.118$  and  $6.076$  MeV

bin. fiss./ $\alpha$ -decay = 1/31

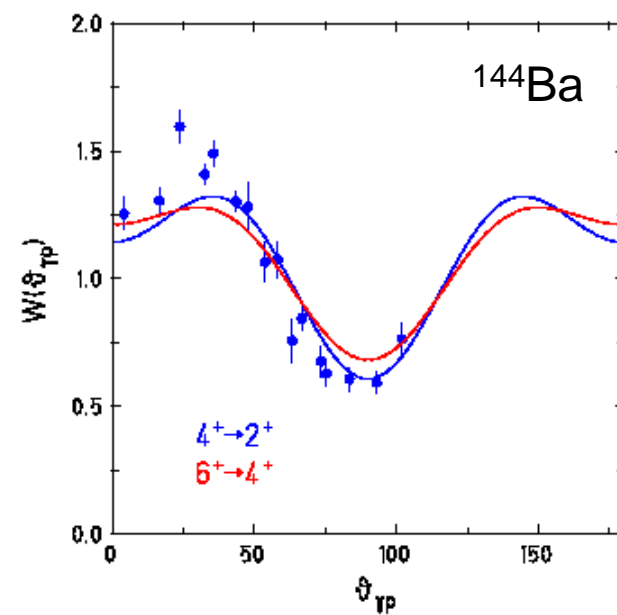
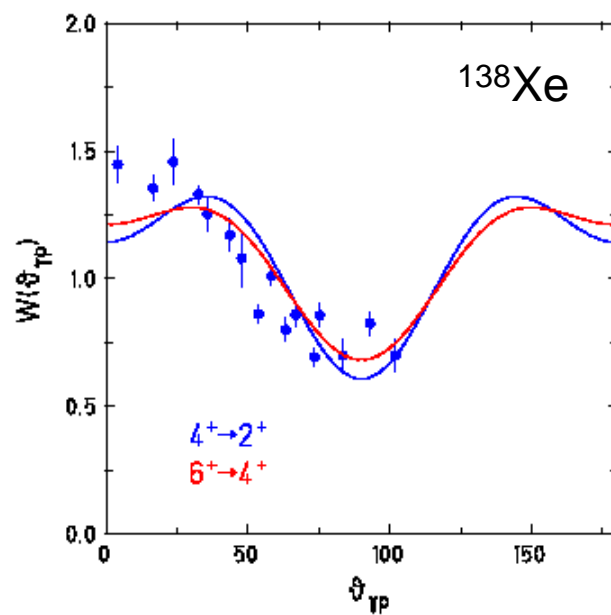
ter. fiss./ $\alpha$ -decay = 1/8308

# 4 $\pi$ twin ionization chamber for fission fragments



The origin of fragment spins and their alignment

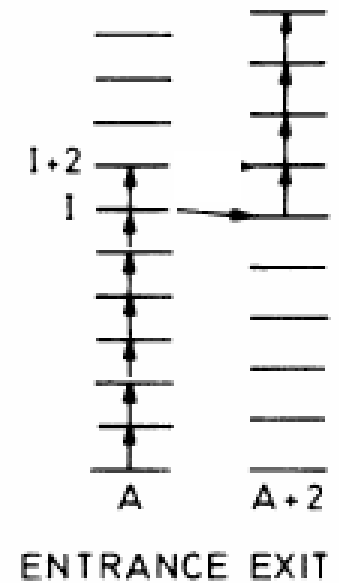
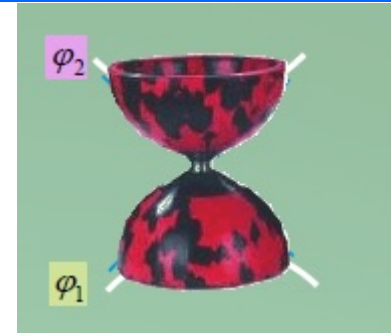
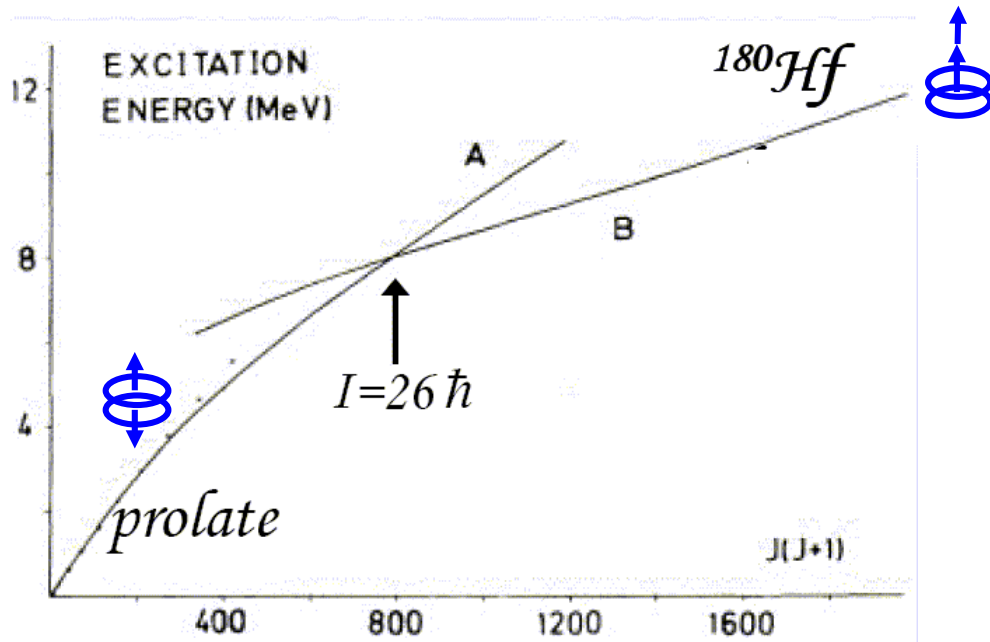
4<sup>+</sup> → 2<sup>+</sup> transitions



# Search for diabolic pair transfer

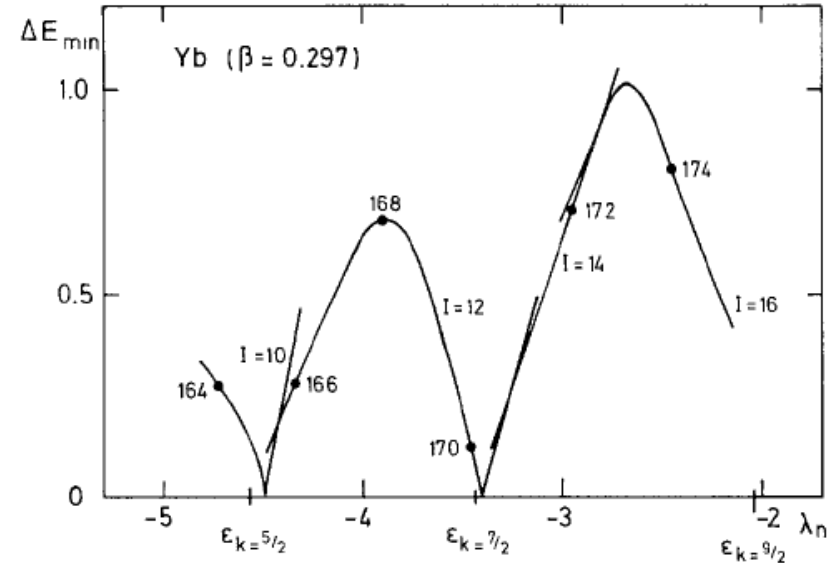
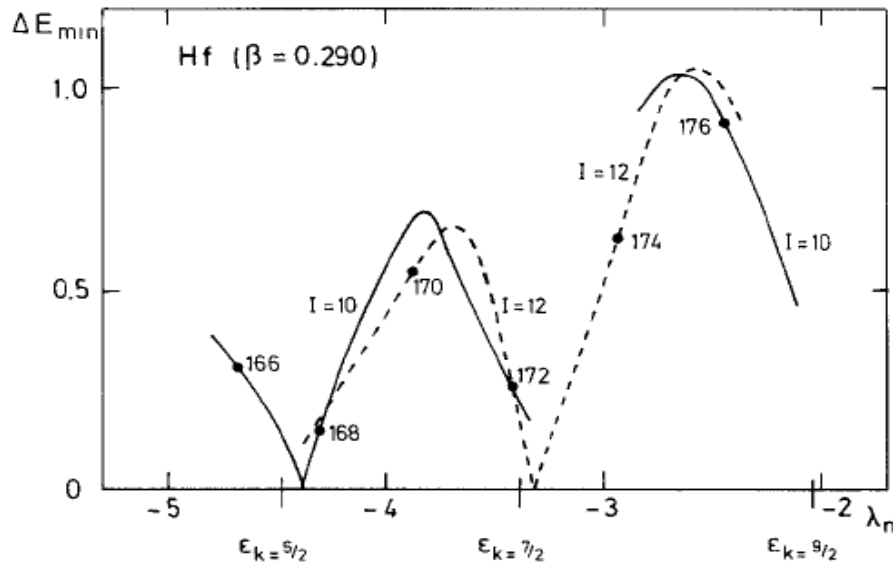
## Nuclear Josephson Effects:

Enhanced transfer of nucleon pairs between two superfluid heavy nuclei in a cold reaction correspond to a super-current



# Proposed systems

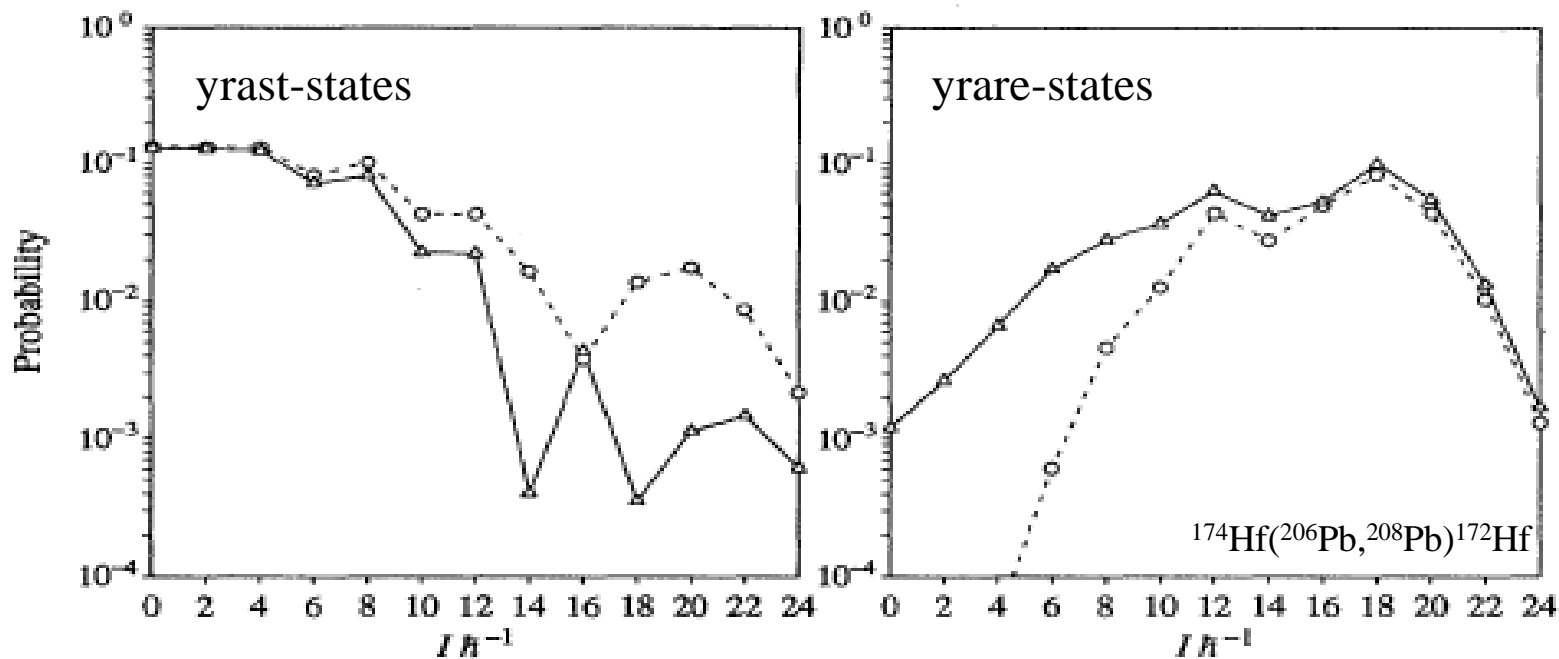
172,174Yb on  $^{206}\text{Pb}$   
174,176Hf on  $^{206}\text{Pb}$



The Hf and Yb-chain : The interaction strength in the level crossing between the ground state band and the s-band characterized by the minimal distance between the yrast band and the first excited band  $\Delta E_{min}$ . Connected lines correspond to minimal distances for the angular momenta  $I=10-16\hbar$ . Full dot symbols indicate the even mass Yb-isotopes. The position of the deformed single-particle energies of the  $\nu i_{13/2}$  levels for the nucleus  $^{166}\text{Yb}$  and  $^{170}\text{Hf}$  are given on the abscissa.

Y. Sun et al, Z. Phys. A339 (1991) 51

# Proposed systems $2n$ -transfer probability as a function of spin



The calculation show the diabolo effect for  $^{206}\text{Pb}$  on  $^{174}\text{Hf}$ . This calculation assumes  $^{174}\text{Hf}$  transfers to  $^{172}\text{Hf}$ . The symbol o's are non diabolo case and  $\Delta$ 's are diabolo cases.

*L F Canto et al PRC 47,2836(1993).*



# Open problems

- ❖ Coulomb excitation of isomeric states in deformed nuclei
- ❖ Nuclear structure of  $^{208}\text{Pb}$
- ❖ Studies in the  $^{100}\text{Sn}$  region (Magda Gorska)
- ❖ Search for diabolic pair transfer at higher angular momentum states
  
- ❖ Mini Orange devices from Johan van Klinken are with Torsten Kröll (TU Darmstadt)
  
- ❖ 10 radioactive targets ( $0.3 \text{ mg/cm}^2$ ) from LMU München stored in Mainz (C. Düllmann)  
 $^{235}\text{U}$  ( $1 \text{ mg} \equiv 80 \text{ Bq}$ ),  $^{237}\text{Np}$  ( $1 \text{ mg} \equiv 26 \text{ kBq}$ ),  $^{242}\text{Pu}$  ( $1 \text{ mg} \equiv 145 \text{ kBq}$ ) (area =  $0.2 \text{ cm}^2$ )  
 $^{226}\text{Ra}$  material