

# relativistic nuclear collisions from FAIR to LHC energies and the phase structure of QCD

- introduction and perspective
- the hadron resonance gas
- (u,d,s) hadron production, Lattice QCD and the QCD phase structure
- quarkonia and heavy quark hadrons – window to understand deconfinement
- outlook

TGSW 2017 workshop

Tsukuba, Japan  
Sep. 25 - 27, 2017



UNIVERSITÄT  
HEIDELBERG  
ZUKUNFT  
SEIT 1386



phenomenology results obtained in collaboration with  
Anton Andronic,  
Krzysztof Redlich, and Johanna Stachel

hadron production data from the ALICE collaboration  
at the CERN LHC  
see, e.g., M. Floris,  
Nucl.Phys. A931 (2014) 103-112  
and references there

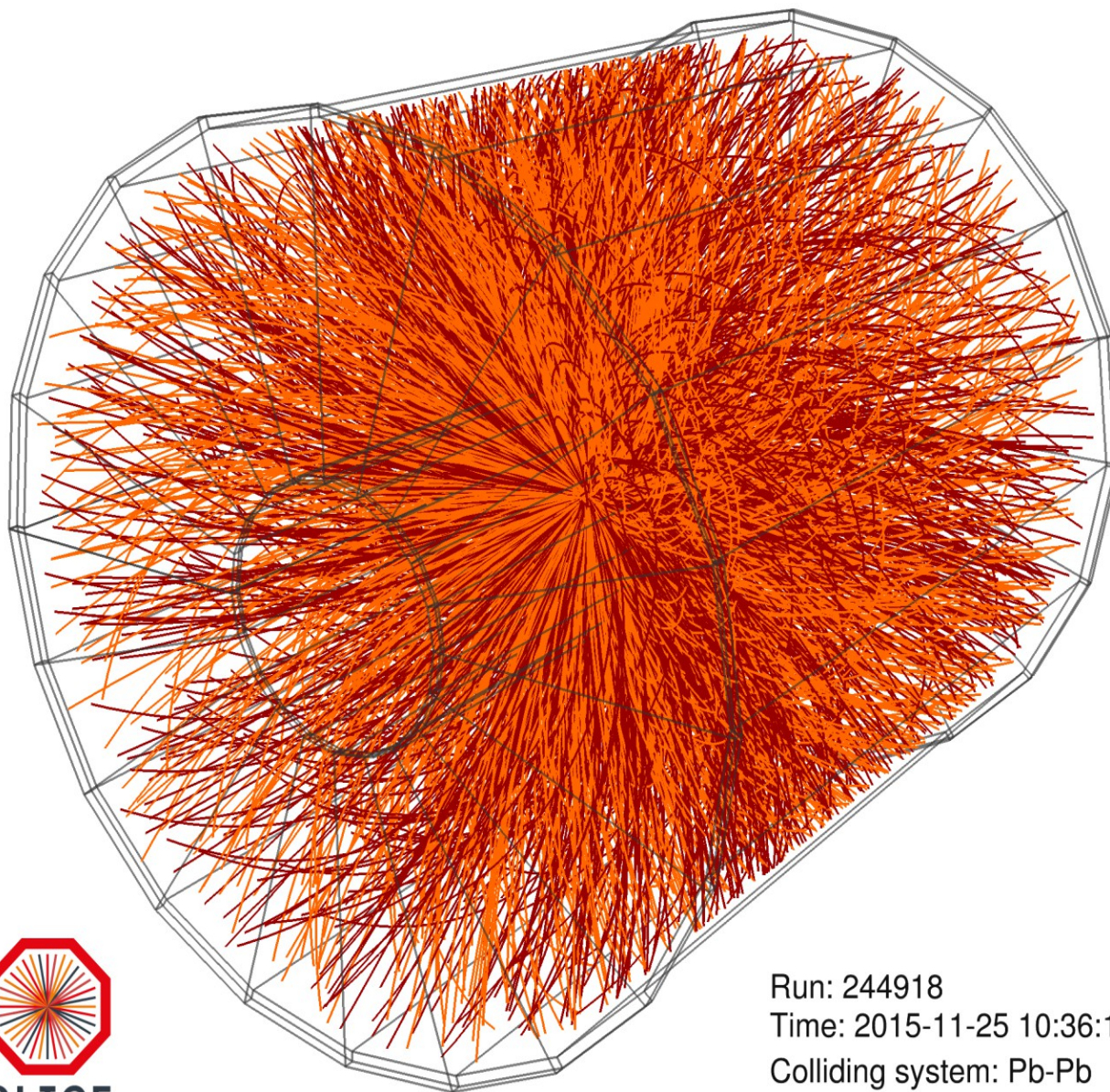
# first PbPb collisions at LHC at $\sqrt{s} = 5.02$ A TeV

Run1: 3 data taking campaigns  
pp, pPb, Pb—Pb  
> 135 publications

Run2 has started with 13 TeV pp  
Pb—Pb run  
in November 2015

Now running with 13 TeV pp

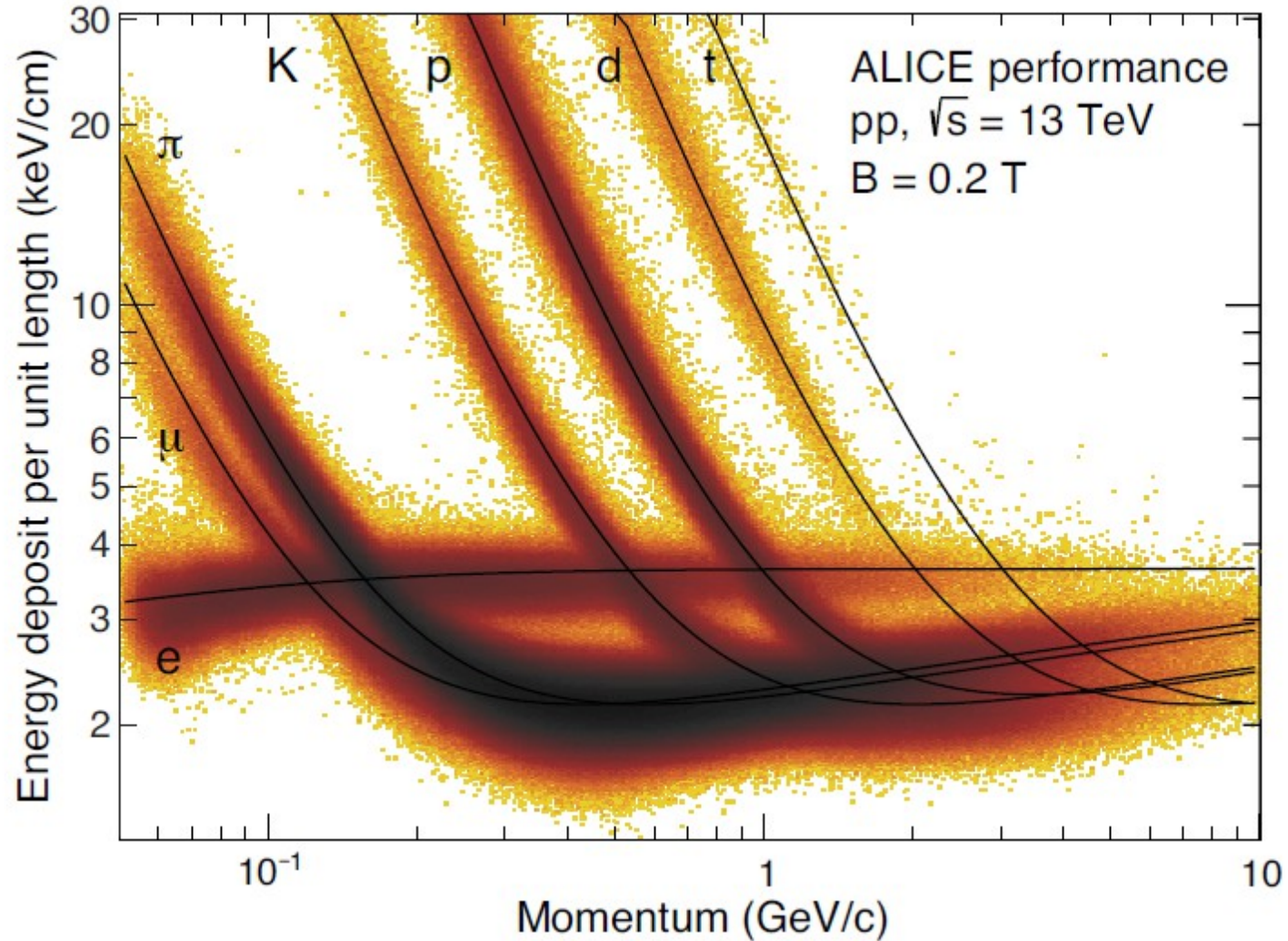
Nov. 2016: pPb 5 TeV



Run: 244918  
Time: 2015-11-25 10:36:18  
Colliding system: Pb-Pb  
Collision energy: 5.02 TeV

# particle identification with the ALICE TPC

from 50 MeV to 50 GeV



# **hadron production and the QCD phase boundary**

## **part 1: the hadron resonance gas**

# duality between hadrons and quarks/gluons (I)

Z: full QCD partition function

all thermodynamic quantities derive from QCD partition functions

for the pressure we get:

$$\frac{p}{T^4} = \frac{1}{T^3} \frac{\partial \ln Z(V, T, \mu)}{\partial V}$$

comparison of trace anomaly from LQCD

Phys.Rev. D90 (2014) 094503

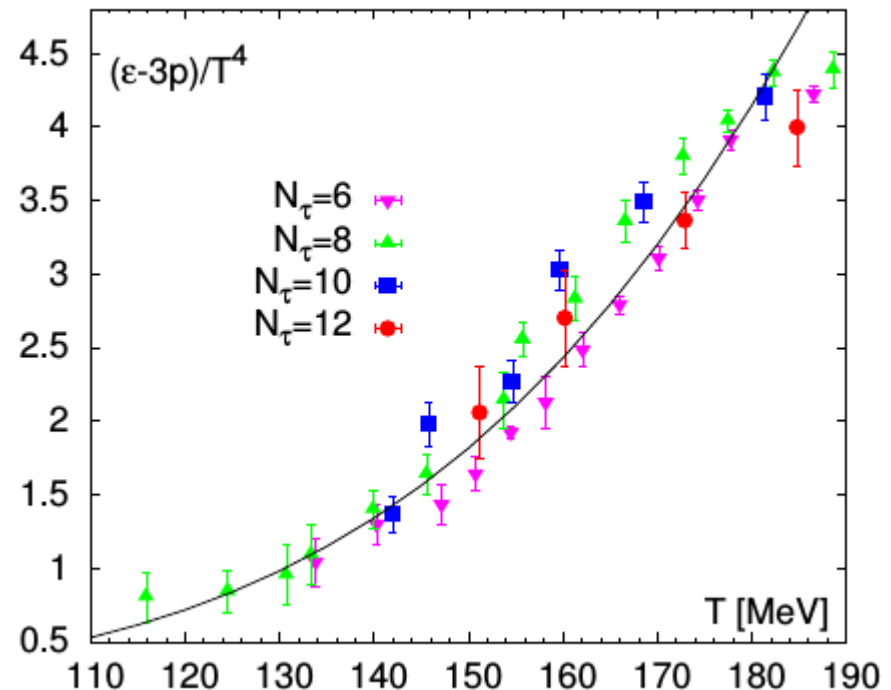
HOTQCD coll.

with hadron resonance gas prediction

(solid line)

LQCD: full dynamical quarks with realistic

pion mass

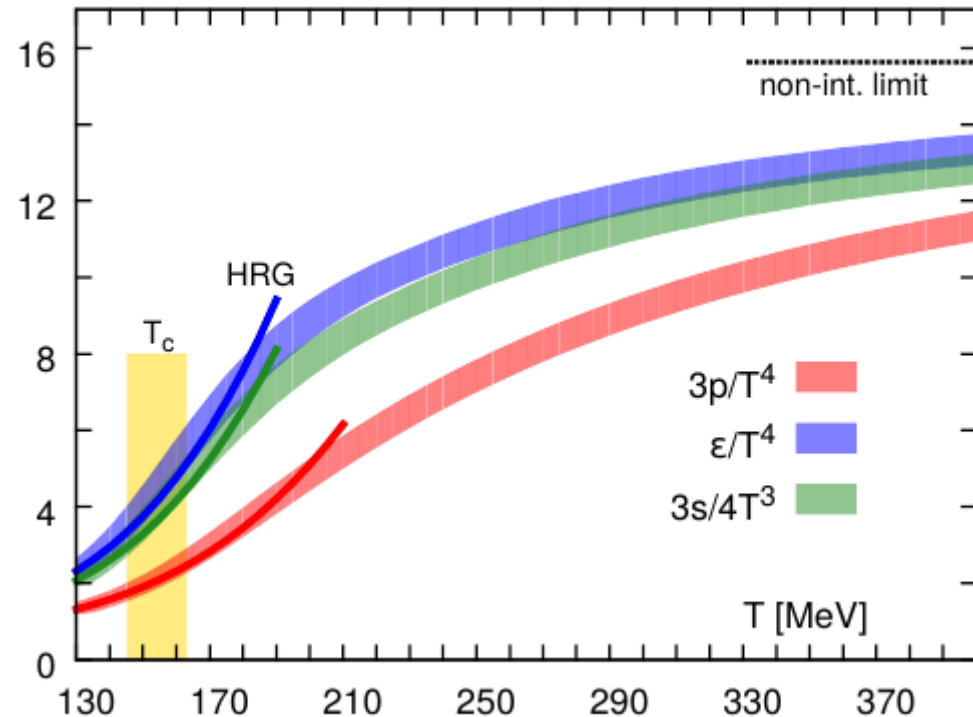


# duality between hadrons and quarks/gluons (II)

comparison of equation of state from  
LQCD  
Phys.Rev. D90 (2014) 094503  
HOTQCD coll.

with hadron resonance gas predictions  
(colored lines)

essentially the same results also from  
Wuppertal-Budapest coll.  
Phys.Lett. B730 (2014) 99-104



↑ pseudo-critical  
temperature

$$T_c = (154 \pm 9) \text{ MeV}$$

$$\epsilon_{\text{crit}} = (340 \pm 45) \text{ MeV/fm}^3$$

$$\epsilon_{\text{nucl}} = 450 \text{ MeV/fm}^3$$

# duality between hadrons and quarks/gluons (III)

in the dilute limit  $T < 165$  MeV:

$$\ln Z(T, V, \mu) \approx \sum_{i \in \text{mesons}} \ln \mathcal{Z}_{M_i}^M(T, V, \mu_Q, \mu_S) + \sum_{i \in \text{baryons}} \ln \mathcal{Z}_{M_i}^B(T, V, \mu_b, \mu_Q, \mu_S)$$

where the partition function of the hadron resonance model is expressed in mesonic and baryonic components. The chemical potential  $\mu$  reflects then the baryonic, charge, and strangeness components  $\mu = (\mu_b, \mu_Q, \mu_S)$ .



# thermal model of particle production and QCD

partition function  $Z(T,V)$  contains sum over the full hadronic mass spectrum and is fully calculable in QCD

for each particle  $i$ , the statistical operator is:

$$\ln Z_i = \frac{V g_i}{2\pi^2} \int_0^\infty \pm p^2 dp \ln[1 \pm \exp(-(E_i - \mu_i)/T)]$$

particle densities are then calculated according to:

$$n_i = N_i/V = -\frac{T}{V} \frac{\partial \ln Z_i}{\partial \mu} = \frac{g_i}{2\pi^2} \int_0^\infty \frac{p^2 dp}{\exp[(E_i - \mu_i)/T] \pm 1}$$

from analysis of all available nuclear collision data we now know the energy dependence of the parameters  $T$ ,  $\mu_b$ , and  $V$  over an energy range from threshold to LHC energy and can confidently extrapolate to even higher energies

in practice, we use the full experimental hadronic mass spectrum from the PDG compilation (vacuum masses) to compute the 'primordial yield'

comparison with measured hadron yields needs evaluation of all strong decays

# implementation

$$n_i = N_i/V = -\frac{T}{V} \frac{\partial \ln Z_i}{\partial \mu} = \frac{g_i}{2\pi^2} \int_0^\infty \frac{p^2 dp}{\exp[(E_i - \mu_i)/T] \pm 1}$$

Latest PDG hadron mass spectrum ...quasi-complete up to  $m=2$  GeV;  
our code: 555 species (including fragments, charm and bottom hadrons)

for resonances, the width is considered in calculations

$$\text{Minimize: } \chi^2 = \sum_i \frac{(N_i^{exp} - N_i^{therm})^2}{\sigma_i^2}$$

$N_i$  hadron yield,  $\sigma_i$  experimental uncertainty (stat.+syst.)

$$\Rightarrow (T, \mu_B, V)$$

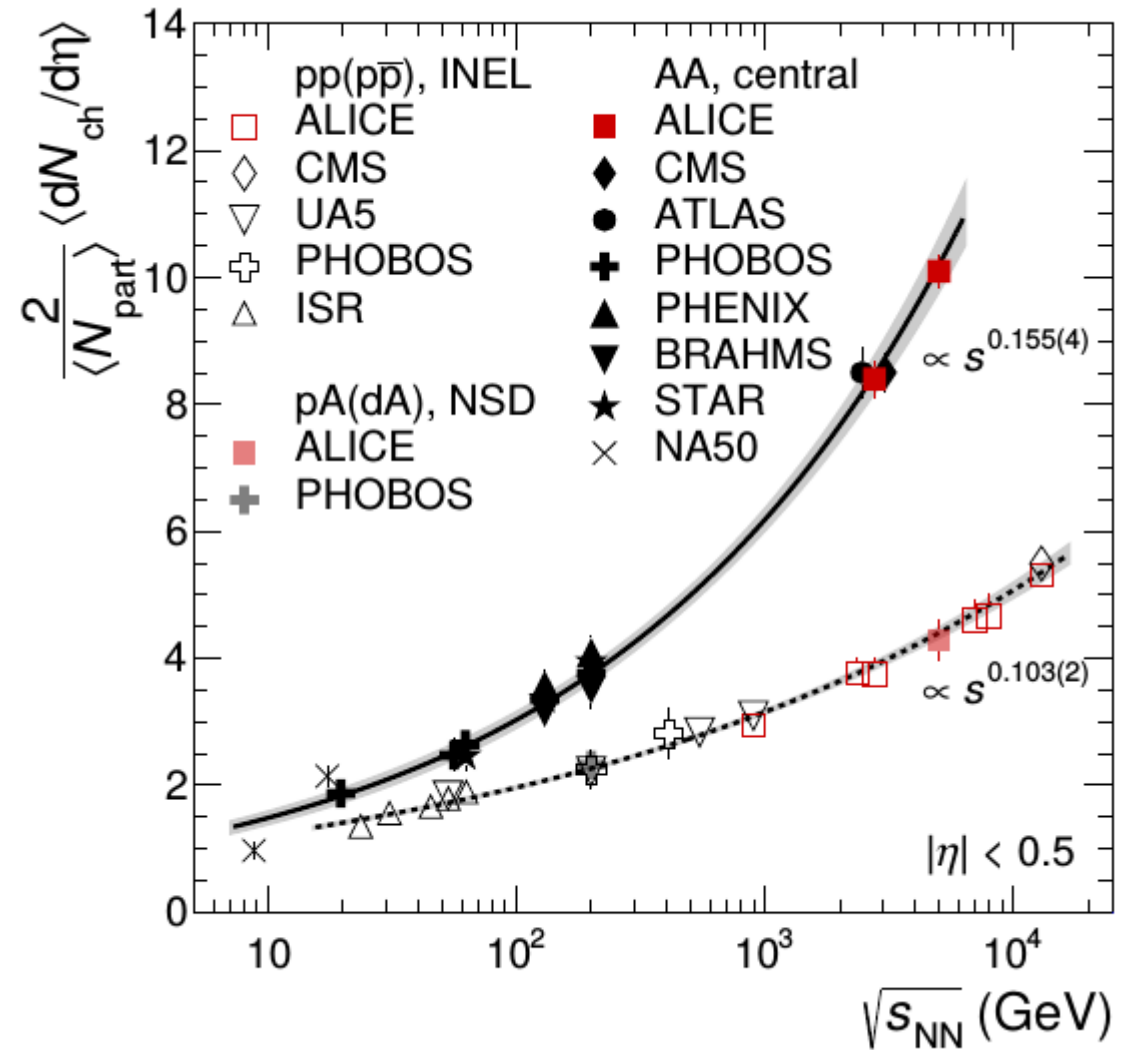
canonical treatment whenever needed (small abundances)

# energy dependence of hadron production in central Pb-Pb (Au-Au) collisions

total number of hadrons produced

2.76 TeV  $N_{\text{had}} = 25800$

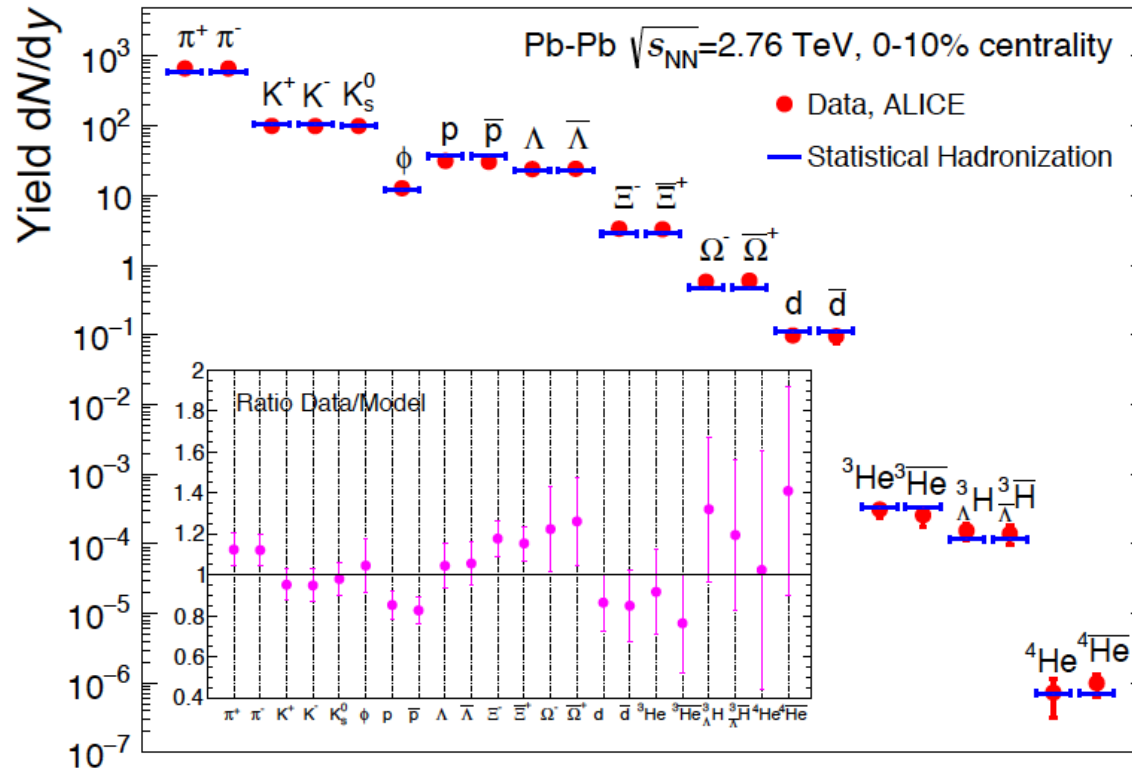
5.02 TeV  $N_{\text{had}} = 32300$



data from LHC run1 and run2

ALICE coll., Phys.Rev.Lett. 116 (2016) no.22, 222302

# July 2017 update: excellent description of ALICE@LHC data



fit includes loosely bound systems such as deuteron and hypertriton  
 hypertriton is bound-state of ( $\Lambda$ ,p,n),  $\Lambda$  separation energy about 130 keV  
 size about 10 fm, the **ultimate halo nucleus**,  
 produced at  $T=156$  MeV. close to an Efimov state

# Quark Model Spectroscopy

Why does the quark model work so well?

Why do M and B body plans dominate?

Why don't multibaryons make one big bag?

**hypothesis:**  
**all nuclei and hyper-nuclei are formed as compact multi-quark states at the phase boundary. Then slow time evolution into hadronic representation.**

Andronic, pbm, Redlich, Stachel, in preparation

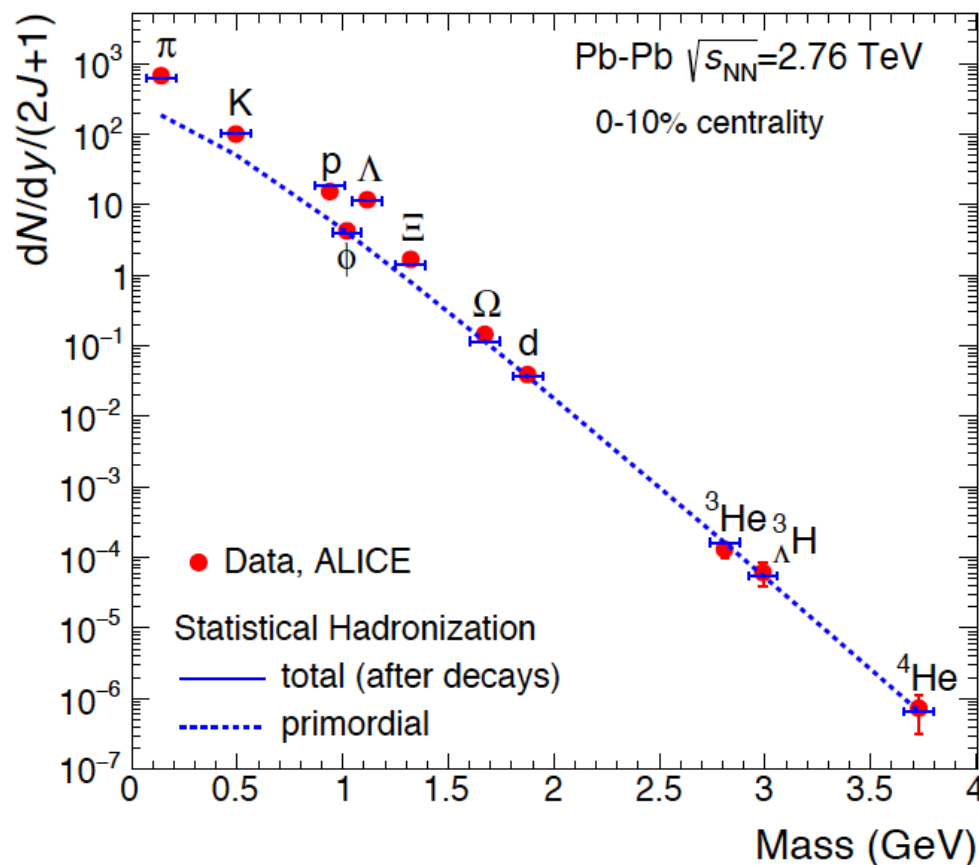
**How can this be tested?**

precision measurement of spectra and flow pattern for light nuclei and hyper-nuclei

**a major new opportunity for ALICE Run3  
and for CBM/NICA/JPARC/NA61**

# excellent agreement over 9 orders of magnitude

agreement over 9  
orders of  
magnitude with  
QCD statistical  
operator  
prediction



yield of light nuclei predicted in: pbm, J. Stachel, J.Phys. G28 (2002) 1971-1976,  
J.Phys. G21 (1995) L17-L20

# a note on the chemical freeze-out temperature

$$T_{\text{chem}} = 156.5 \pm 1.5 \text{ MeV from fit to all particles}$$

there is an additional uncertainty because of the poorly known hadronic mass spectrum for masses  $> 2 \text{ GeV}$

for d,  $^3\text{He}$ , hypertriton and alpha, there is very little feeding from heavier states and none from high mass states in the hadronic mass spectrum, for these particles the temperature  $T_{\text{nuc}}$  can be determined 'on the back of an envelope' :

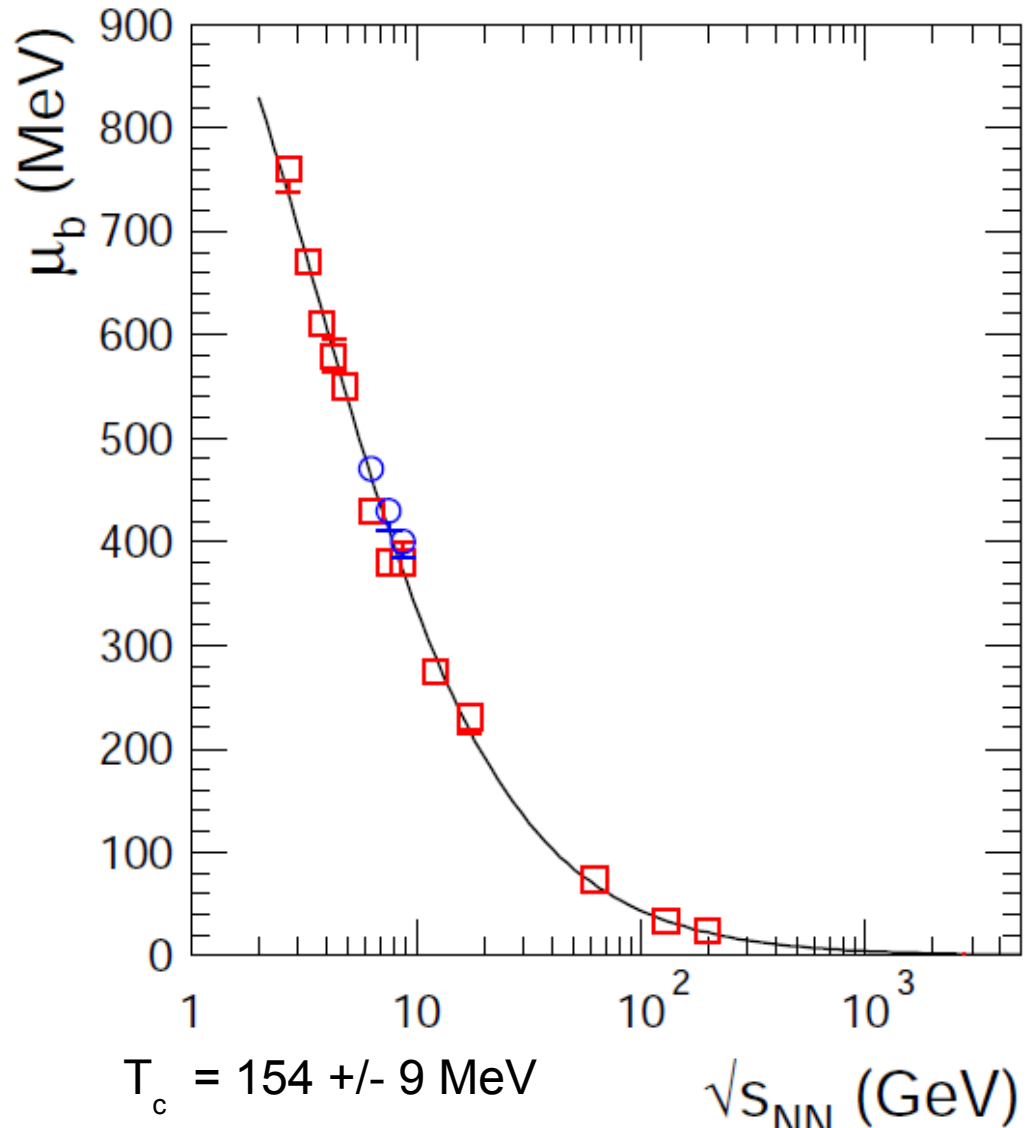
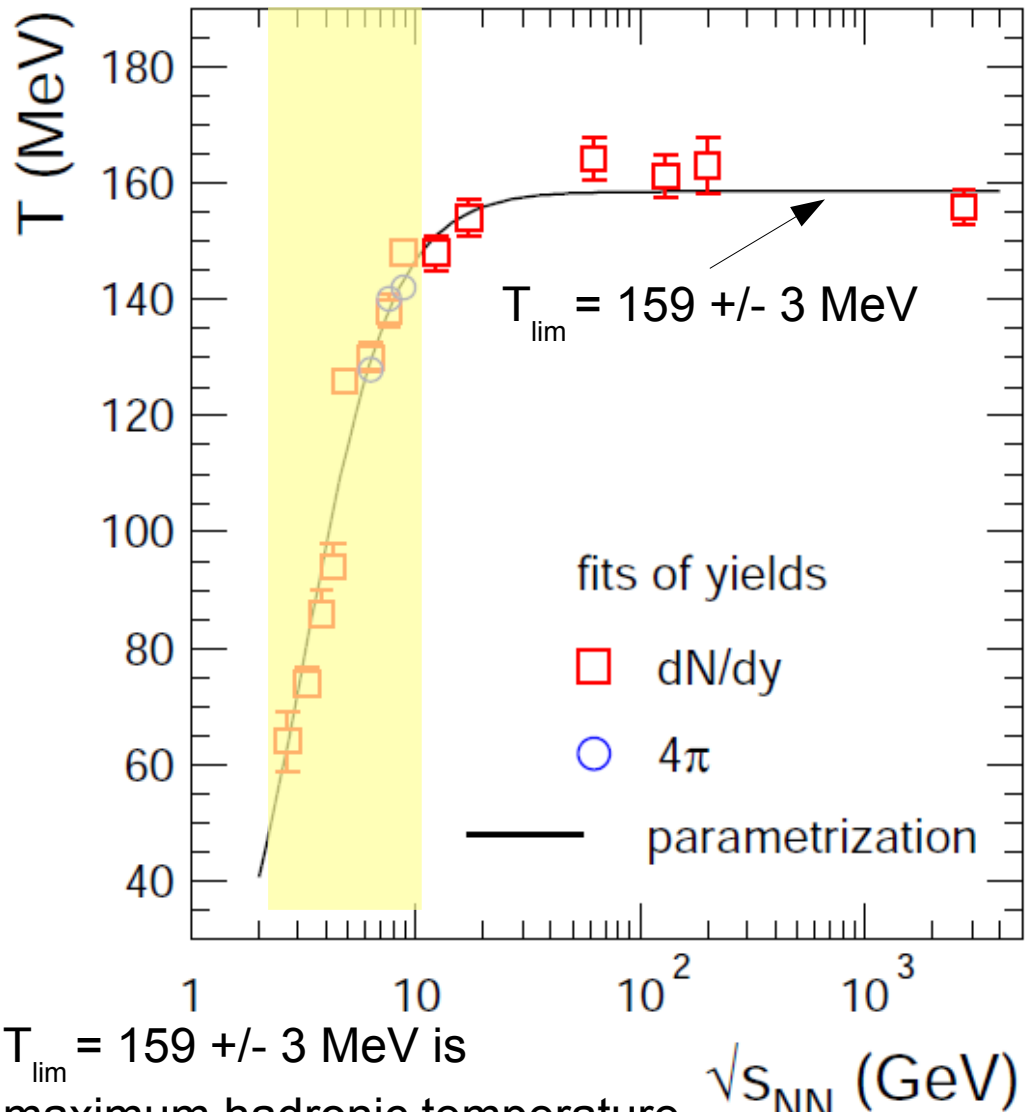
$$T_{\text{nuc}} = 154 \pm 5 \text{ MeV, independent of hadronic mass spectrum}$$



# energy dependence of temperature and baryo-chemical potential

energy range from SPS down to threshold (FAIR)

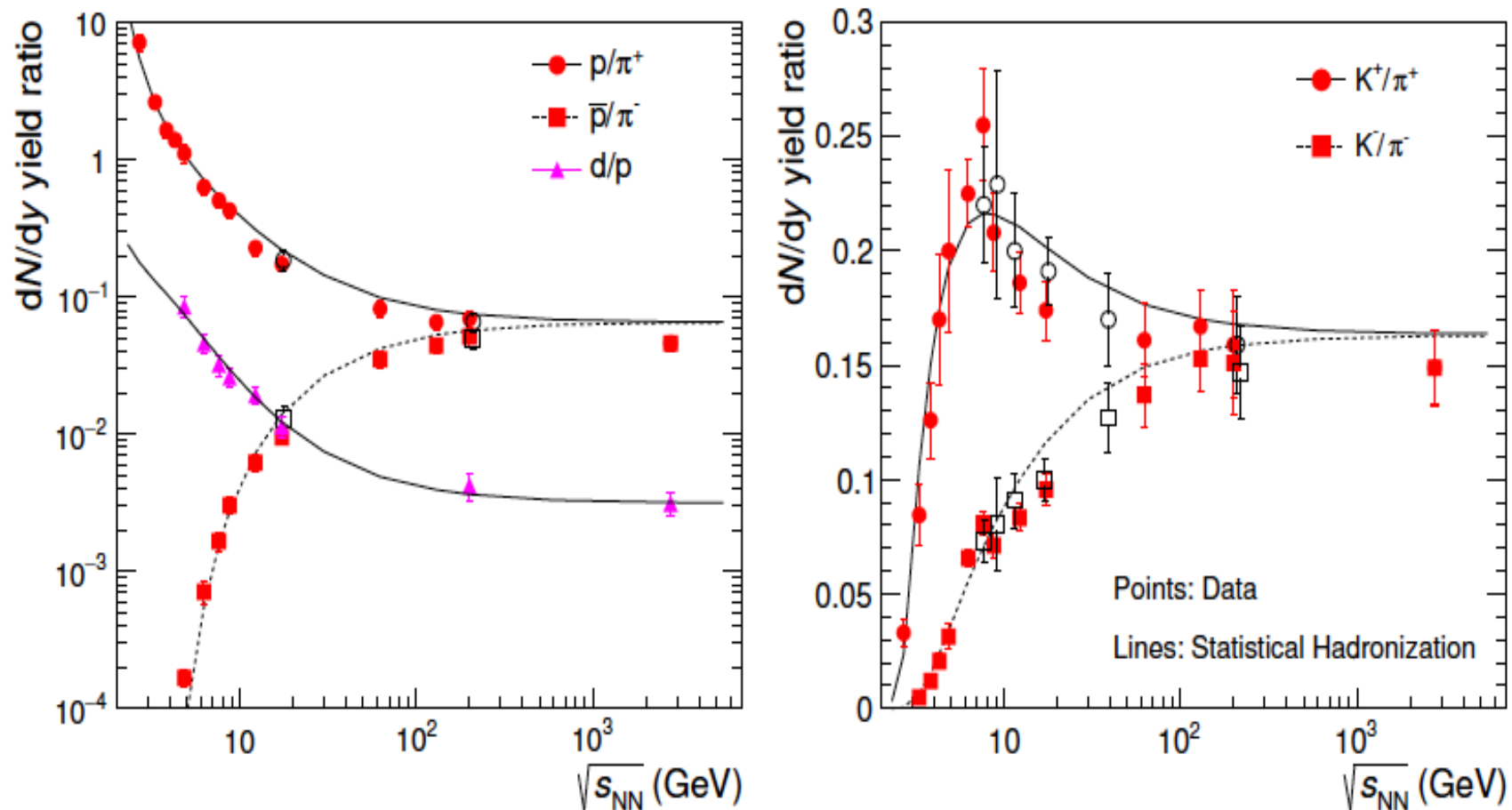
is phase boundary ever reached for  $\sqrt{s_{NN}} < 10$  GeV?



$T_{lim} = 159 \pm 3$  MeV is maximum hadronic temperature

$T_c = 154 \pm 9$  MeV from lattice

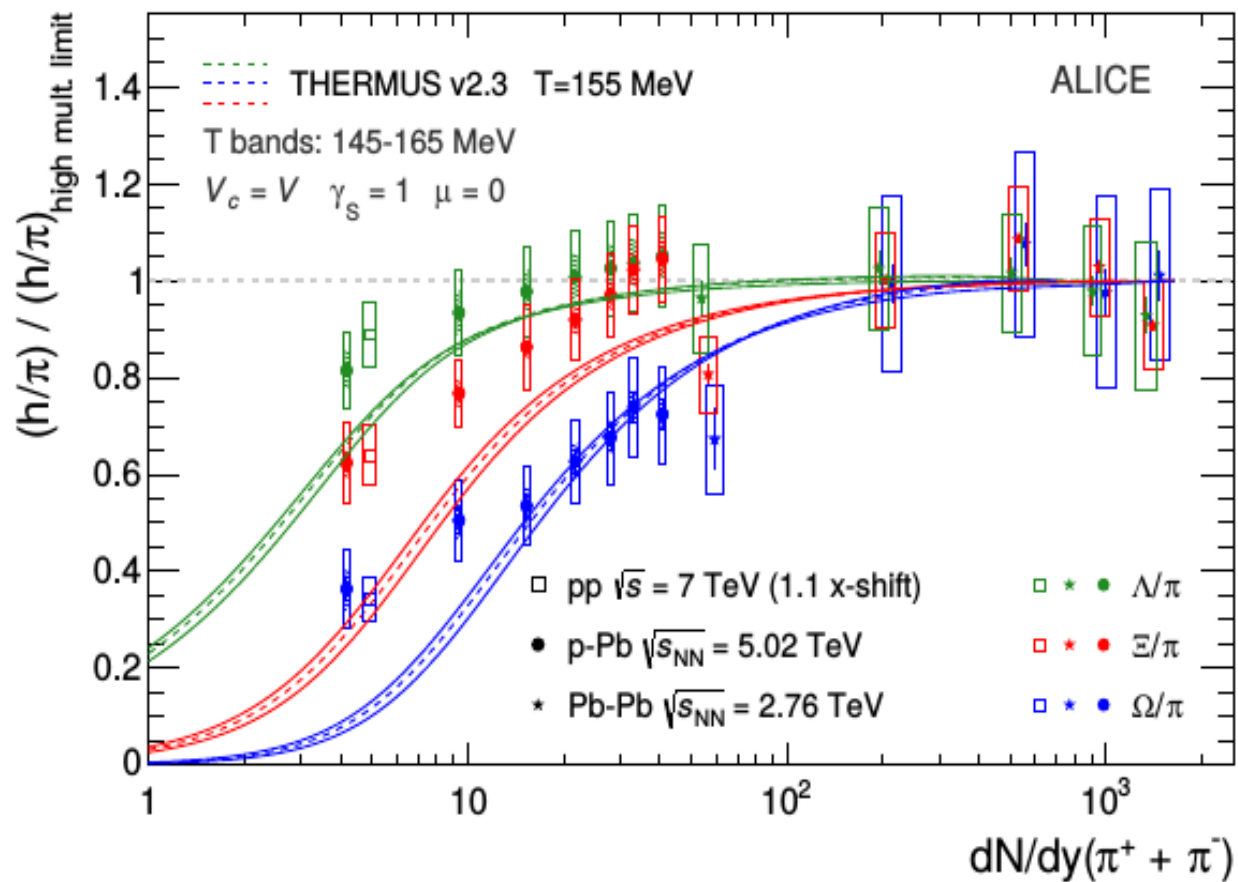
# energy dependence of hadron production described quantitatively



together with known energy dependence of charged hadron production in Pb-Pb collisions we can predict yield of all hadrons at all energies with < 10% accuracy

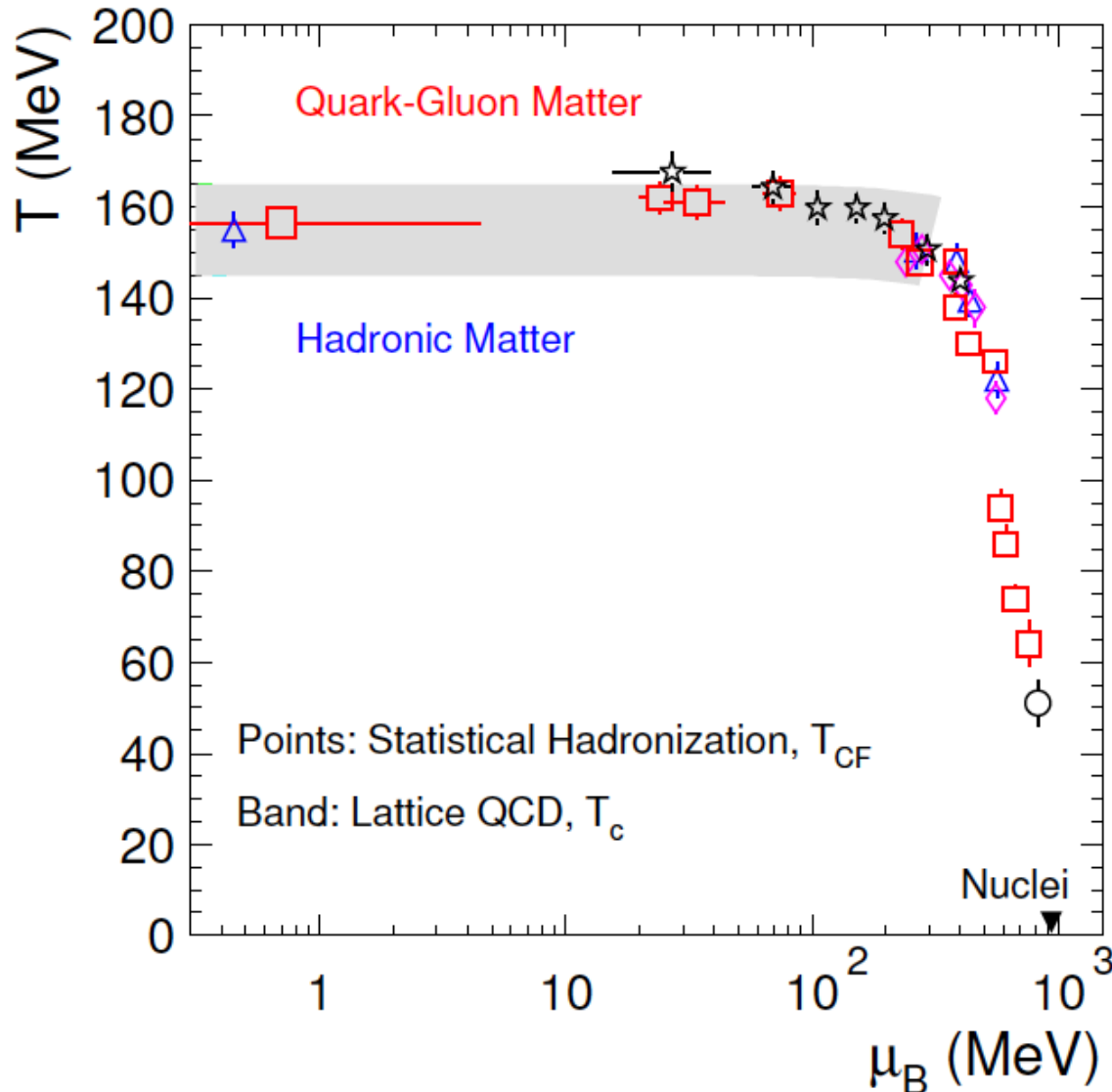
no new physics needed to describe  $K^+/\pi^+$  ratio including the 'horn'

# is multiplicity dependence described by canonical thermodynamics?



main features, but not details, are captured well – needs further study  
 arXiv:1512.07227 ALICE

# the QGP phase diagram, LQCD, and hadron production data



quantitative agreement of chemical freeze-out parameters with LQCD predictions for baryochemical potential  $< 300$  MeV

# charmonium as a probe for the properties of the QGP

the original idea: (Matsui and Satz 1986) implant charmonia into the QGP and observe their modification, in terms of suppressed production in nucleus-nucleus collisions with or without plasma formation – **sequential melting**

new insight (pbm, Stachel 2000) QGP screens all charmonia, but charmonium production takes place at the phase boundary, enhanced production at colliders – **signal for deconfined, thermalized charm quarks production probability scales with  $N(c\bar{c})^2$**

reviews: L. Kluberg and H. Satz, arXiv:0901.3831

pbm and J. Stachel, arXiv:0901.2500

both published in Landoldt-Boernstein Review, R. Stock, editor, Springer 2010

nearly simultaneous: Thews, Schroeder, Rafelski 2001

formation and destruction of charmonia inside the QGP

n.b. at collider energies there is a complete separation of time scales

$$t_{\text{coll}} \ll t_{\text{QGP}} < t_{\text{Jpsi}}$$

implanting charmonia into QGP is an inappropriate notion

this issue was already anticipated by Blaizot and Ollitrault in 1988

# the idea

heavy quarks are not thermally produced, since their mass  $m \gg T$

at collider energies, heavy quarks are copiously produced through QCD hard scattering

the developing hot fireball formed in the collision thermalizes the heavy quarks

all charmed hadrons and charmonia are deconfined near  $T_c$

the fireball expands and cools until it reaches the phase boundary

there, charmonia are formed with thermal/statistical weights

since charmonium formation scales with  $N(c\bar{c})^2$  and since the charm cross section increases strongly with energy, we expect enhanced charmonium production at collider energy

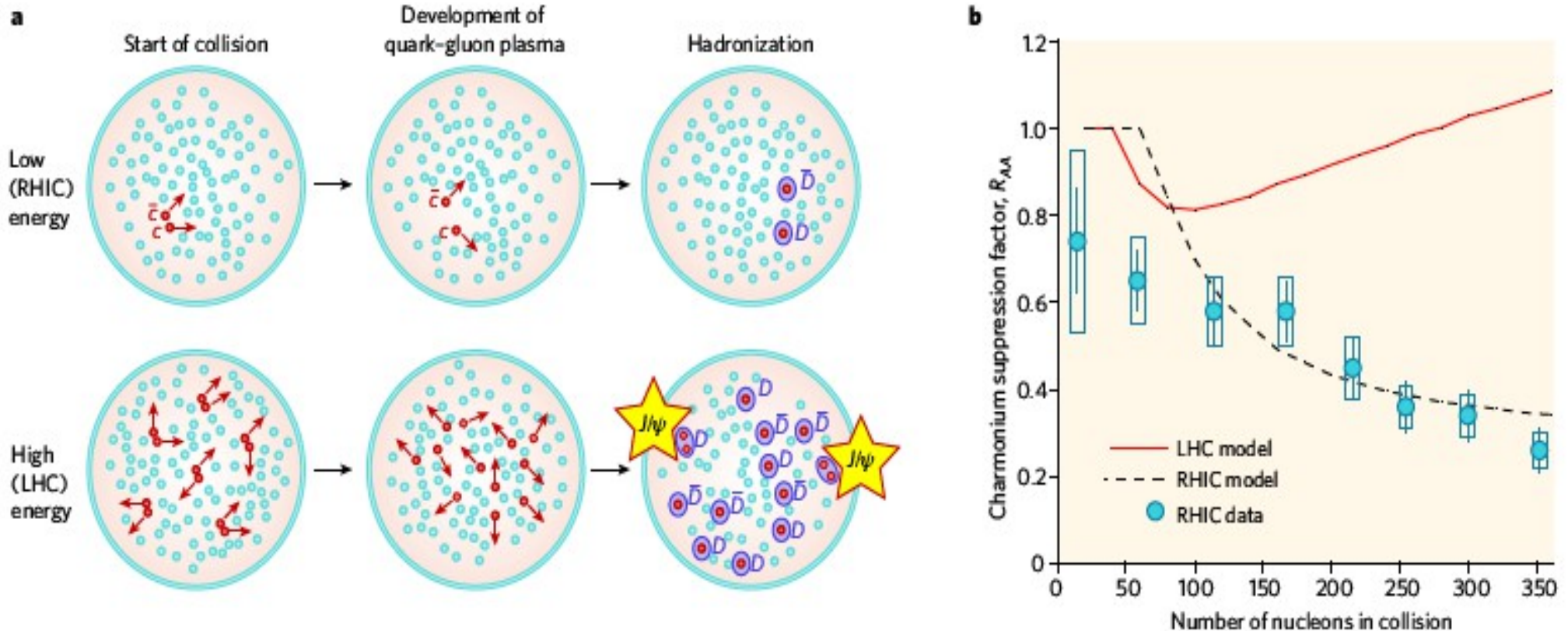
this brings the thermal model into the heavy quark era with a large heavy quark fugacity

note: mass of charm quark is about 300 times heavier than mass of light quarks

# quarkonium as a probe for deconfinement at the LHC

## the statistical (re-)generation picture

P. Braun-Munzinger, J. Stachel, The Quest for the Quark-Gluon Plasma, Nature 448 Issue 7151, (2007) 302-309.

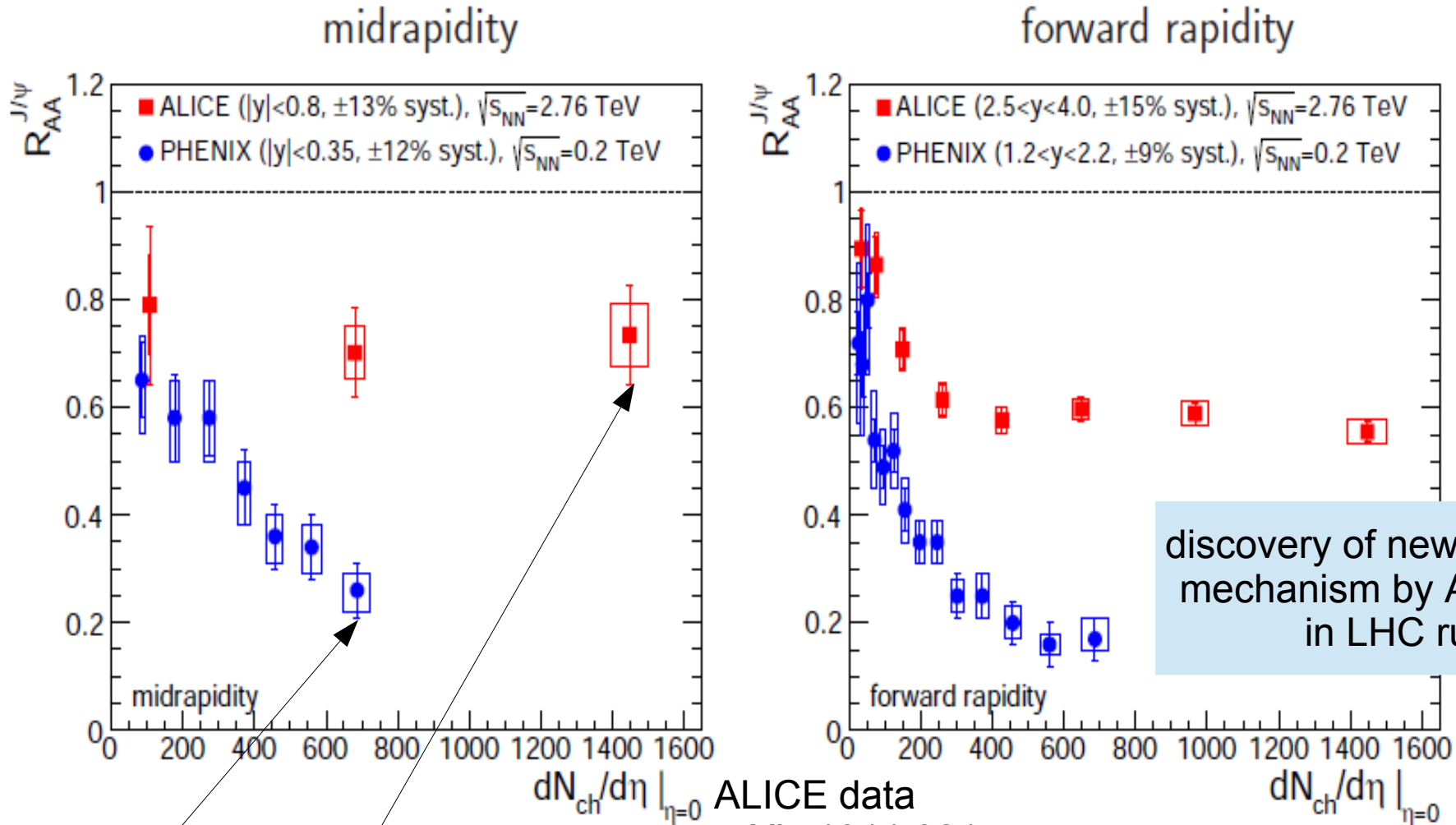


charmonium enhancement as fingerprint of color screening and deconfinement at LHC energy

pbm, Stachel, Phys. Lett. B490 (2000) 196

Andronic, pbm, Redlich, Stachel, Phys. Lett. B652 (2007) 659

# less suppression when increasing the energy density



discovery of new production mechanism by ALICE coll. in LHC run1

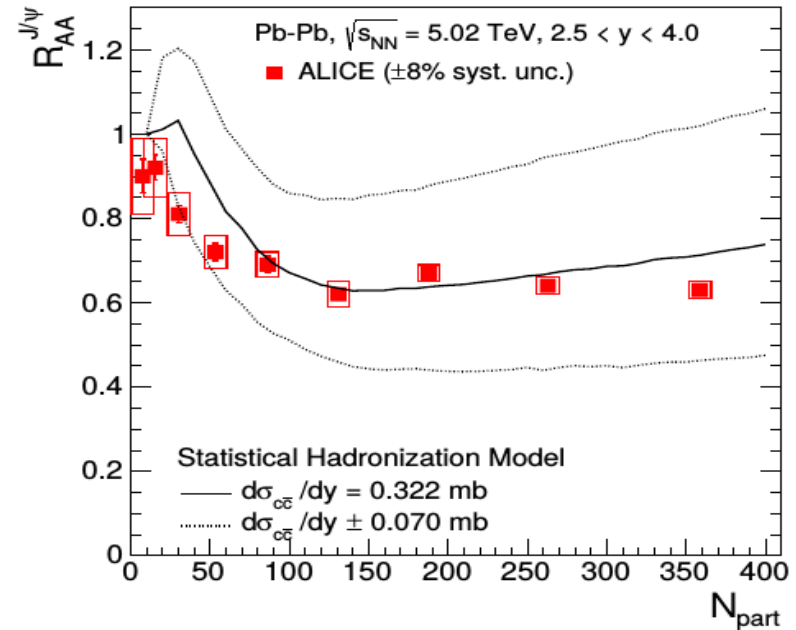
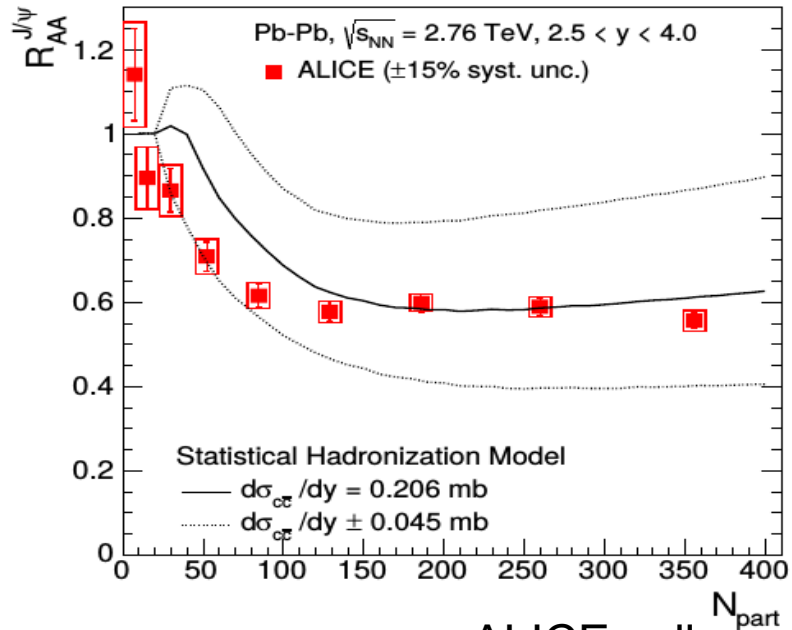
ALICE data  
arXiv:1311.0214  
Phys.Lett. B734 (2014) 314-327

from here to here more than factor of 2 increase in energy density, but  $R_{AA}$  increases by more than a factor of 3

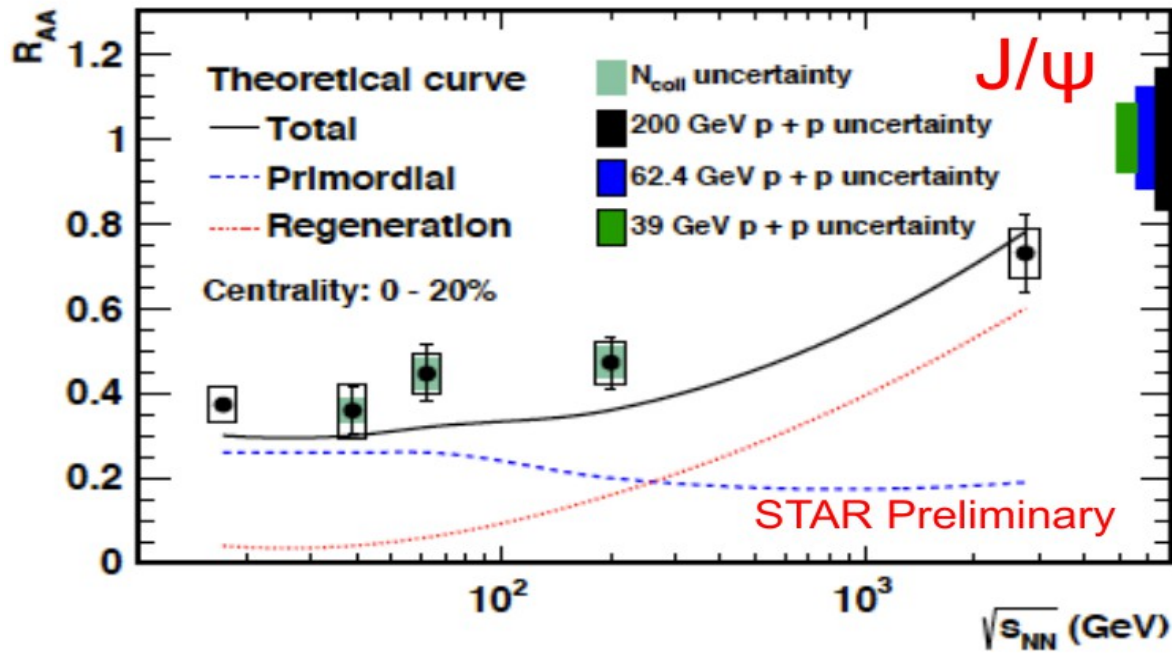
2007 prediction impressively confirmed by LHC data



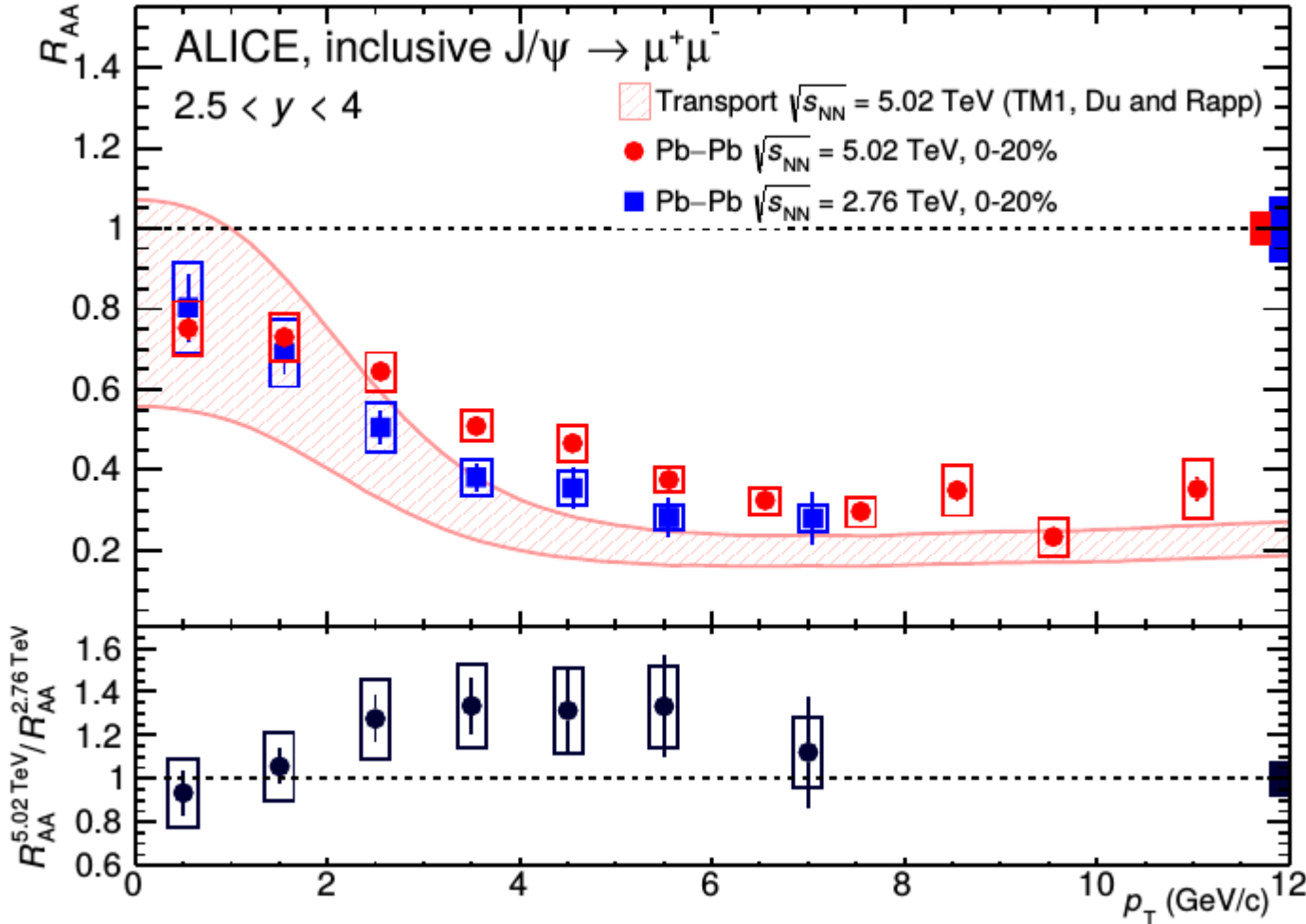
# predictions from 2000/2007 beautifully confirmed by RHIC and LHC data



ALICE coll.,  
 arXiv:1606.08197

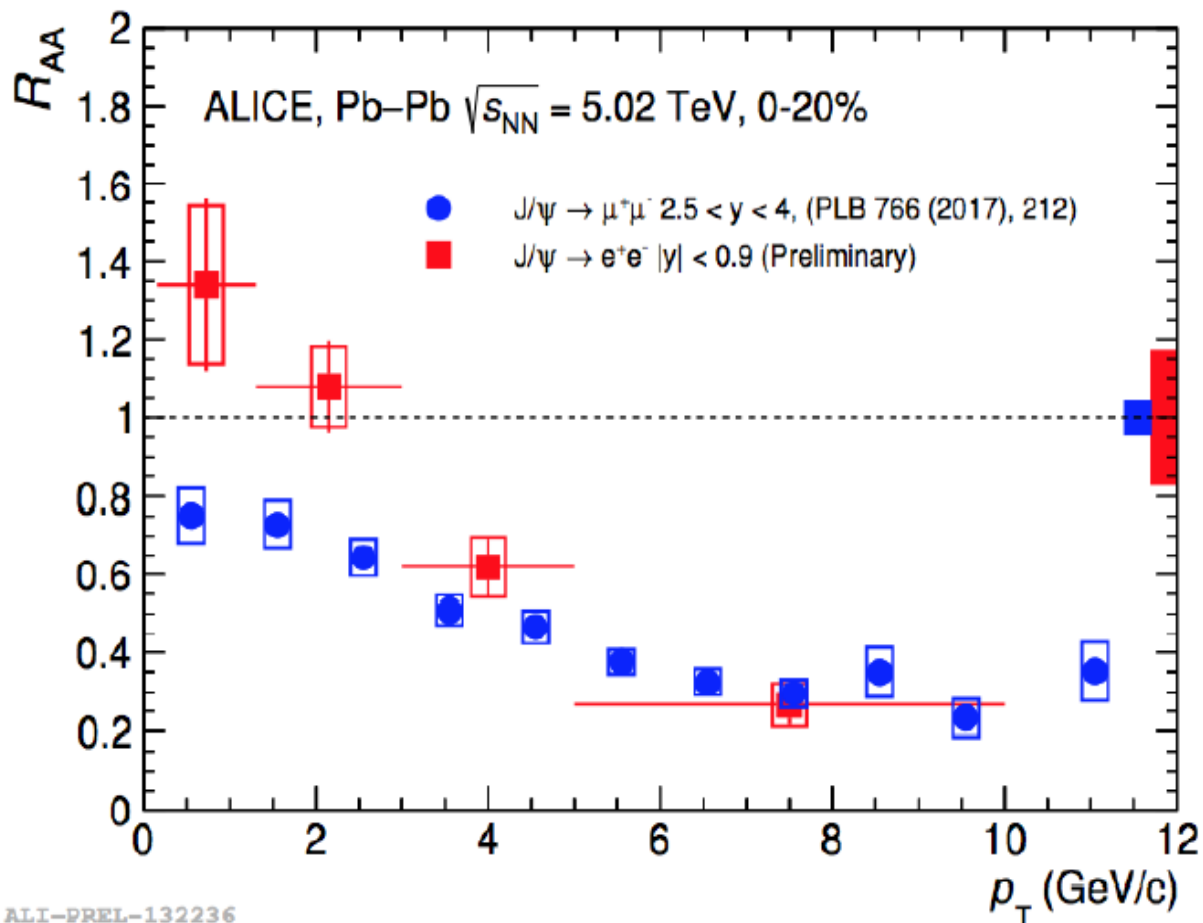


# dependence on transverse momentum (1) forward rapidity



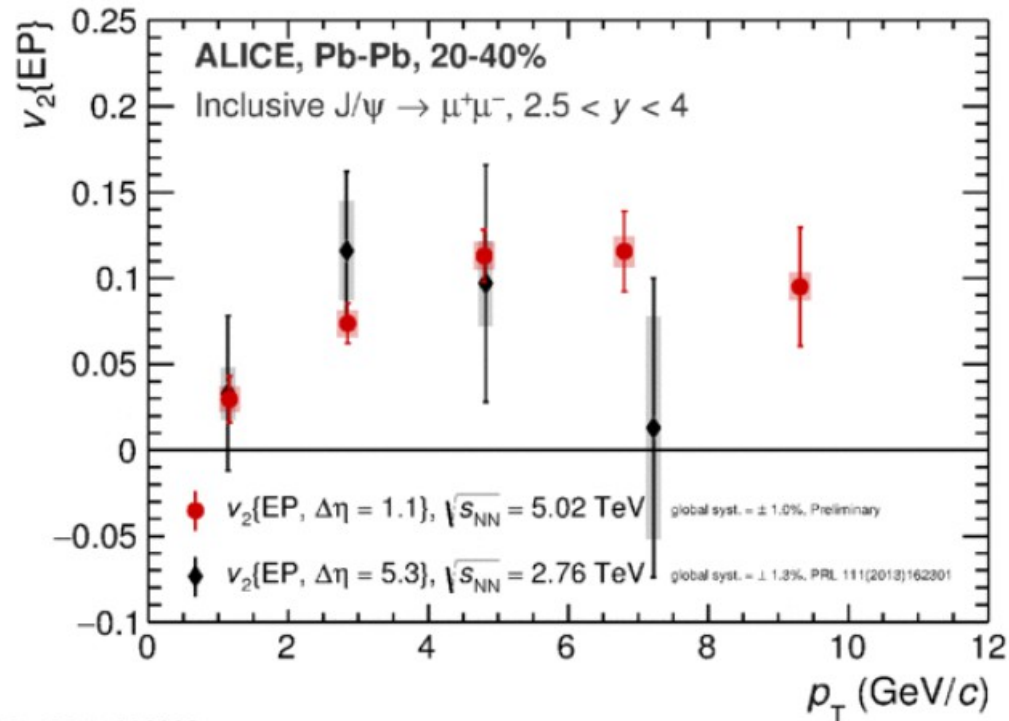
ALICE coll., arXiv:1606.08197

## dependence on transverse momentum (II) mid-rapidity vs forward rapidity



indication of J/psi enhancement at low  $p_t$  near mid-rapidity

# elliptic flow of charmonium



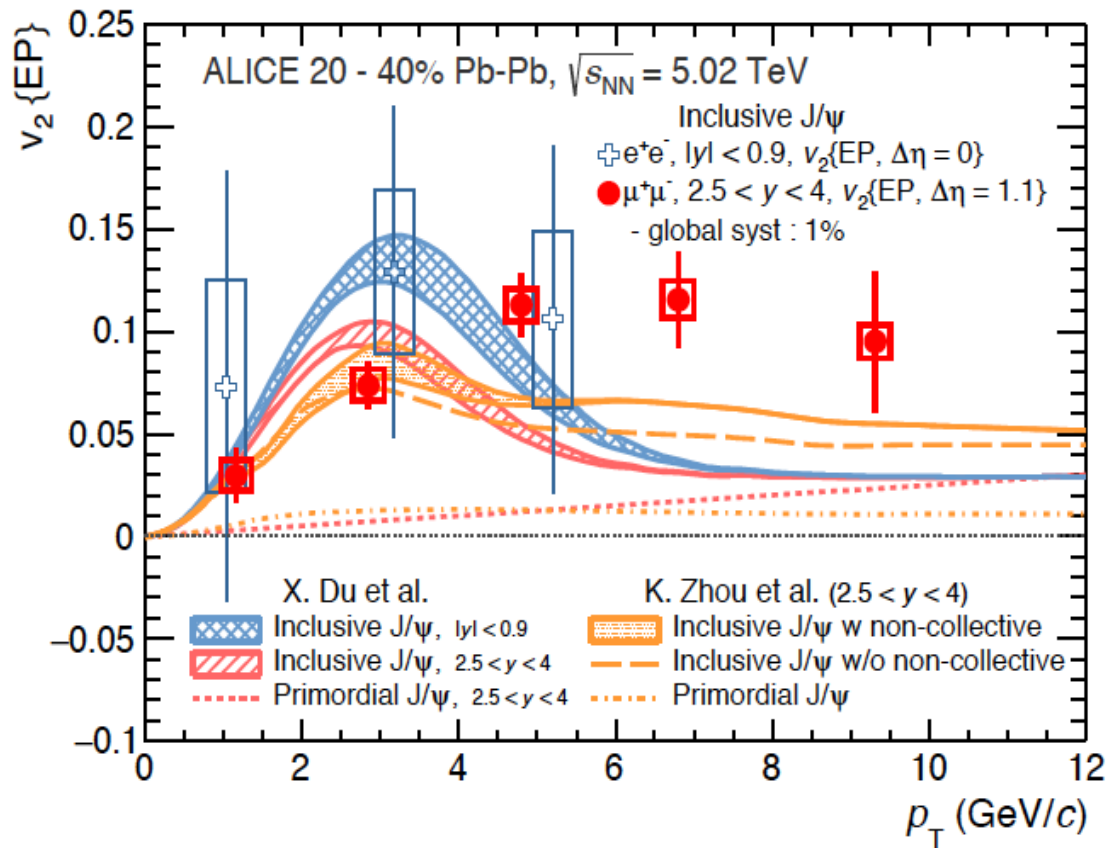
arXiv:1709.05260

ALI-PREL-118883

$p_T$ (GeV/c)	0-2	2-4	4-6	6-8	8-12
$\Delta\eta = 1.1$	$2.2\sigma$	$6.3\sigma$	$7.4\sigma$	$5.0\sigma$	$2.8\sigma$
$\Delta\eta = 5.3$	$1.4\sigma$	$6.2\sigma$	$5.0\sigma$	$3.3\sigma$	$1.3\sigma$

most recent LHC Run2 result,  
charm quarks participate in the hydrodynamical evolution of the QGP fireball  
support for statistical hadronization of deconfined charm quarks

# J/psi flow at mid-rapidity and forward rapidity



J/psi flow larger than expected at high transverse momentum transition from hydrodynamic flow to energy loss?

# summary

overall the LHC data provide strong support for chemical freeze-out driven by the phase transition at  $T_c = 156$  MeV

the full QCD statistical operator is encoded in the nuclear collision data on hadron multiplicities

success to describe also yields of loosely bound states: are they produced as virtual multi-quark states?

statistical hadronization model describes hadrons including charmonia formed from deconfined charm quarks

knowledge of hadron mass spectrum up to 2.5 GeV is important for description → connection to hadron physics community

**connection between LQCD and data**

**experimental evidence for:  
QCD phase boundary  
deconfinement of charm quarks**



additional slides



# The Hypertriton

mass = 2.990 MeV

Lambda sep. energy. = 0.13 MeV

molecular structure: (p+n) + Lambda

2-body threshold: (p+p+n) + pi- =  ${}^3\text{He}$  + pi-

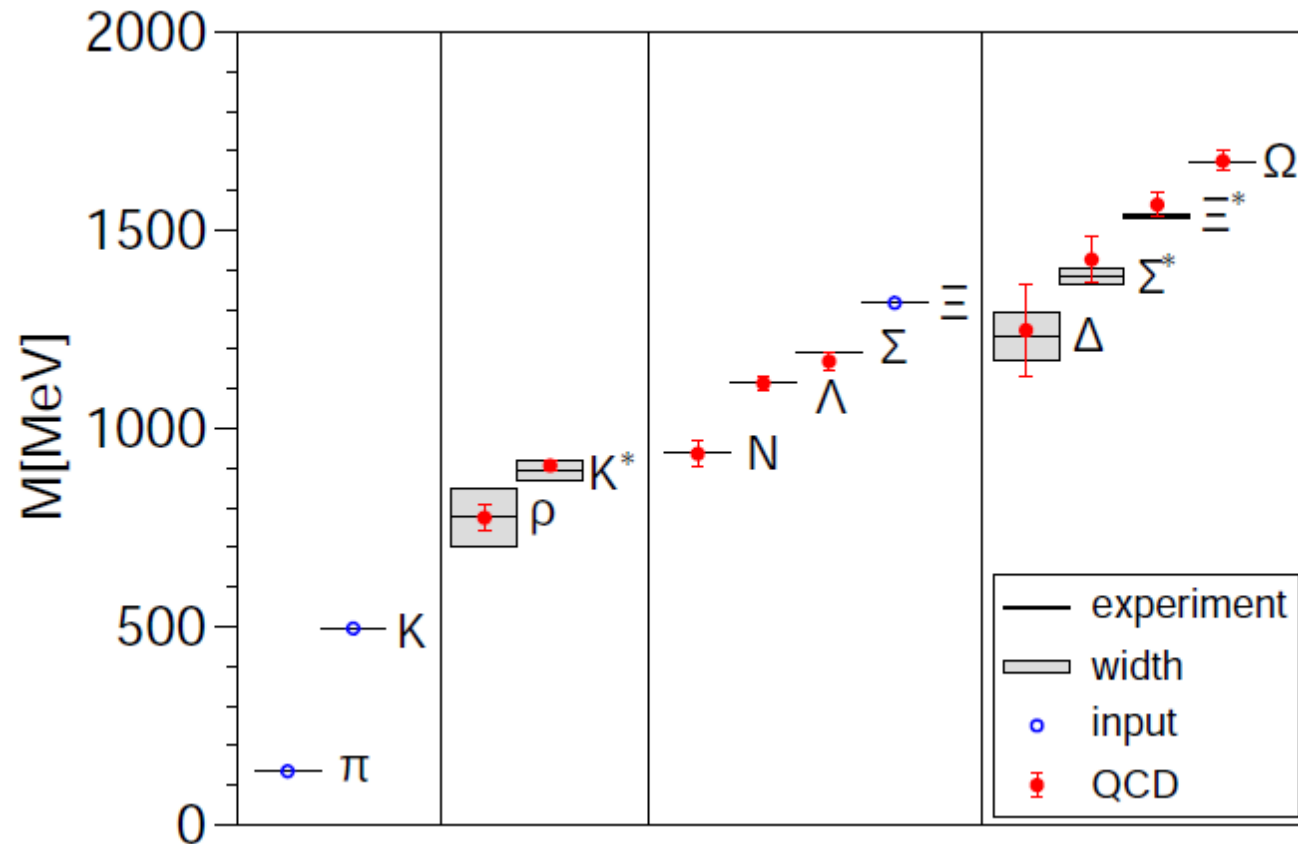
rms radius =  $(4 \text{ B.E. } M_{\text{red}})^{-1/2} = 10.3 \text{ fm} =$

rms separation between d and Lambda

in that sense: hypertriton = (p n Lambda) =  
(d Lambda) is the ultimate halo state

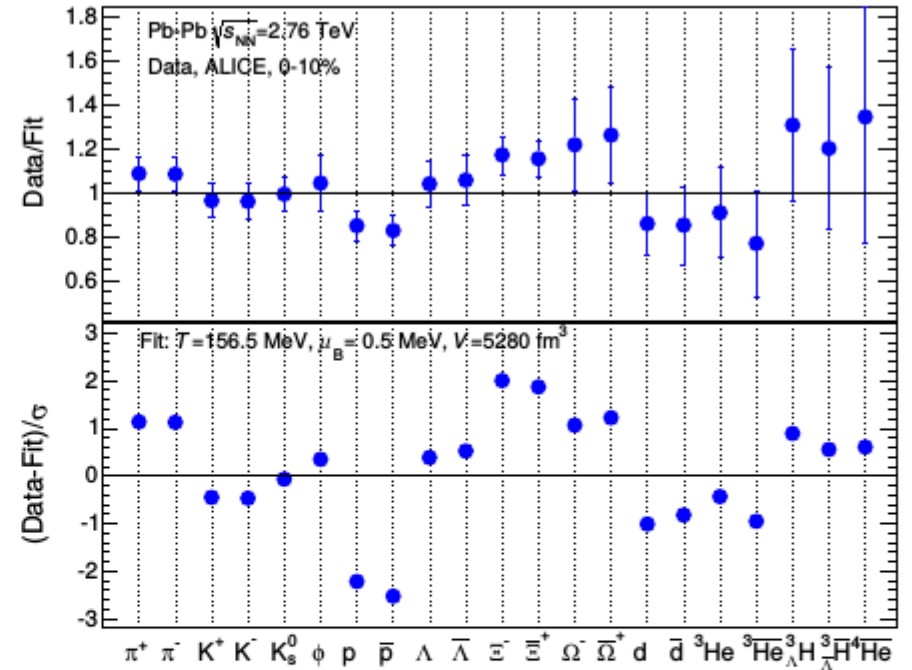
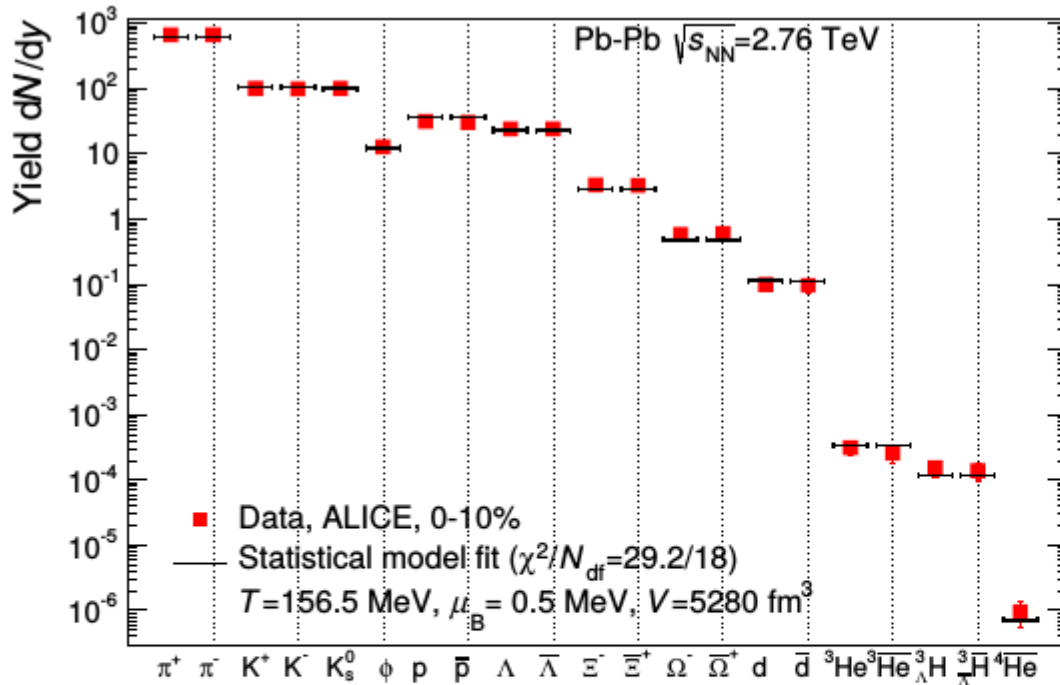
yet production yield is fixed at 156 MeV temperature  
(about 1000 x separation energy.)

# the hadron mass spectrum and lattice QCD



S. Duerr et al., Science 322 (2008) 1224-1227

# details on thermal description

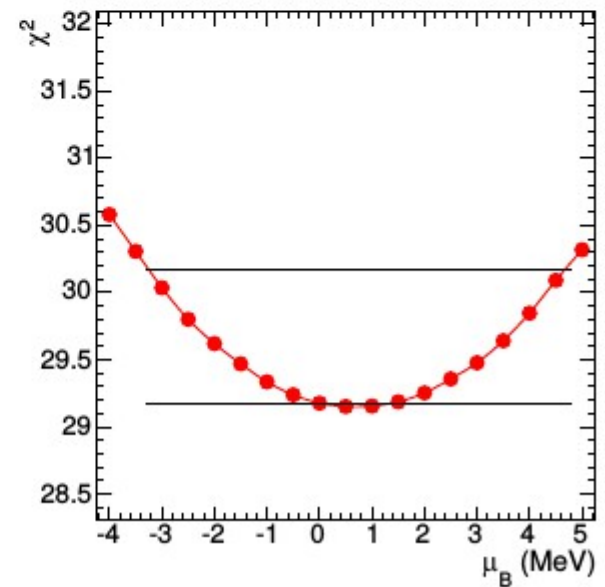
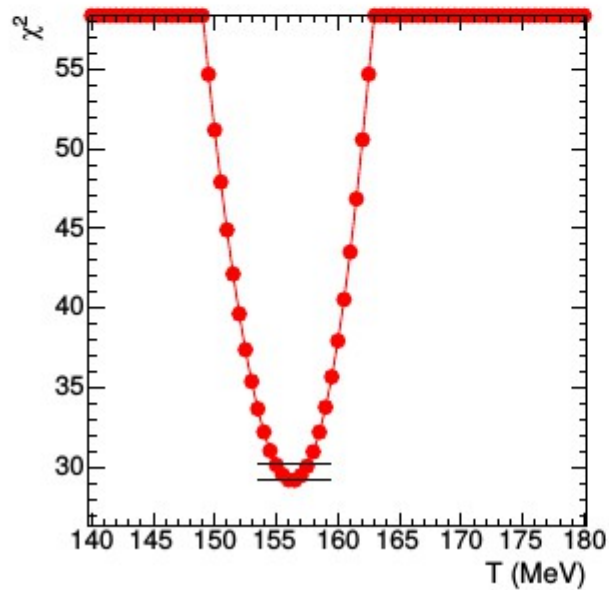
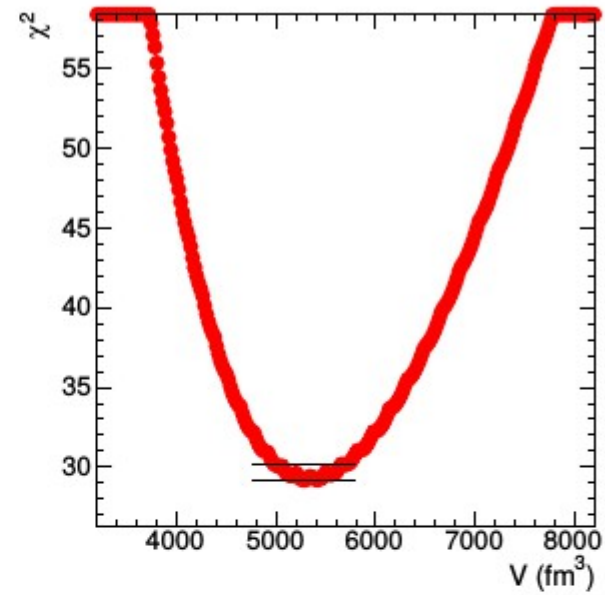
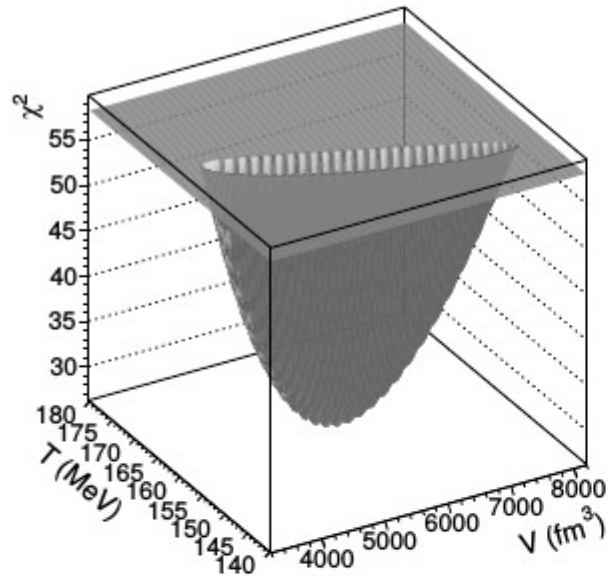


all species in fit

$\pi$ ,  $K^\pm$ ,  $K^0$  from charm included (0.7%, 2.9%, 3.1% for best fit)

$T = 156.5 \pm 1.5$  MeV,  $\mu_B = 0.5 \pm 3.8$  MeV,  $V = 5280 \pm 410$  fm<sup>3</sup>

# chi<sup>2</sup> curves in (T,V) for fit



for the special case of uncorrelated emission (Skellam distribution) and net baryon number  $N = B$ , the susceptibility is related to the total mean number of baryons + anti-baryons via

$$\frac{\chi_N}{T^2} = \frac{1}{VT^3} (\langle N_q \rangle + \langle N_{-q} \rangle)$$

in this limit, we can make a direct comparison between the susceptibility from LQCD, and the experimentally measured total mean number of baryons and anti-baryons.

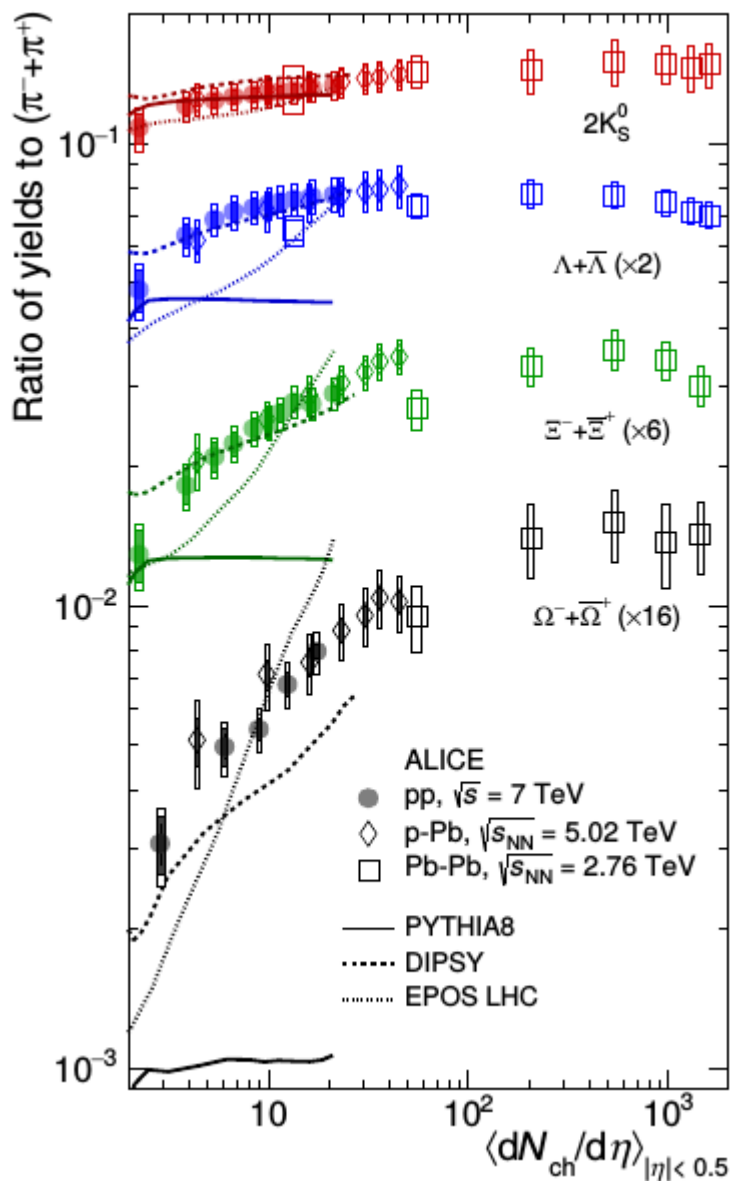
for  $N =$  strangeness  $S$  or charge  $Q$ , similar expressions, with  $|q| = (1,2)$  and  $|q| = (1,2,3)$  hold:

$$\frac{\chi_N}{T^2} = \frac{1}{VT^3} \sum_{n=1}^{|q|} n^2 (\langle N_n \rangle + \langle N_{-n} \rangle)$$

within this approach, a direct link between ALICE LHC data and LQCD predictions can be established

LQCD predictions from: A. Bazavov *et al.* [HotQCD Collaboration], Phys. Rev. D **86**, 034509 (2012).  
A. Bazavov, H.-T. Ding, P. Hegde, O. Kaczmarek, F. Karsch, E. Laermann, Y. Maezawa and S. Mukherjee, Phys. Rev. Lett. **113**, 072001 (2014).

# multiplicity dependence of yield ratios approach to grand-canonical limit observed



← grand-canonical  
Omega/pi

arXiv:1606.07424  
ALICE

## ...more details

- $\bar{\Lambda}$  from S.Schuchmann, [PhD Thesis \(Jul.2015\)](#)

- fragments from ALICE, [arXiv:1506.08951](#)

derived anti-particles from published ratios:

$$d: (9.82 \pm 1.58) \times 10^{-2}, \bar{d}/d = 0.98 \pm 0.13 \rightarrow \bar{d}: (9.62 \pm 2.01) \times 10^{-2}$$

$${}^3\text{He}: \text{rescale from 0-20\% to 0-10\% using } d, \text{ factor } 1.127 \rightarrow (3.11 \pm 0.706) \times 10^{-4}$$

$${}^3\bar{\text{He}}/{}^3\text{He} = 0.83 \pm 0.08 \pm 0.16 \rightarrow {}^3\bar{\text{He}}: (2.58 \pm 0.81) \times 10^{-4}$$

excluded volume correction:

our standard case:  $R_b = R_m = 0.3$  fm

# equilibration at the phase boundary

- statistical model analysis of (u,d,s) hadron production: an important test of equilibration of quark matter near the phase boundary, **no equilibrium → no QGP matter**
- no (strangeness) equilibration in hadronic phase
- present understanding: multi-hadron collisions near phase boundary bring hadrons close to equilibrium – supported by success of statistical model analysis
- this implies little energy dependence above RHIC energy
- analysis of hadron production → determination of  $T_c$

pbm, Stachel, Wetterich,  
Phys.Lett. B596 (2004) 61-69

at what energy is phase boundary reached?



# a few remarks about analysis of higher moments of conserved charges

- already for second moments there is a delicate balance between influence of conservation laws (at large acceptance) and trivial fluctuations (at small acceptance)
- for small acceptance,  $\Delta_\eta \ll 1$ , probability distributions become Poisson and are not sensitive to critical behavior. in this limit all efficiencies are binomially distributed.
- for large acceptance,  $\Delta_\eta > 1$ , effect of conservation laws becomes large. Efficiencies are not anymore binomially distributed. But data are sensitive to dynamical behavior.
- corrections for baryon number conservation become mandatory
- for large values of  $\mu_b$ , impact parameter (volume) fluctuations become largest source of 'trivial' fluctuations, very unpleasant for search for critical endpoint (details see below)
- for higher moments, situation becomes more difficult.
- effect of purity in PID needs to be carefully studied, crucial for higher moment analysis

# a few remarks about analysis of higher moments of conserved charges

- volume fluctuations
- independent source model:
- for  $N$ : total number of particles,  $N_s$ : number of sources,  $n$ : number of particles from a single source

$$c_2(N) = \langle N_s \rangle c_2(n) + \langle n \rangle^2 c_2(N_s)$$

- 2 limits:
  - (i)  $\langle n \rangle = N_p$  low energy limit, fluctuations dominated by trivial volume fluctuations
  - (ii)  $\langle n \rangle = \langle N_p - N_{pbar} \rangle = 0$  high energy (LHC) limit, volume fluctuations drop out

stay tuned for more results in Anar Rustamov's talk on Friday

also ALICE higher moments results soon

**major advantage at LHC energy: EbE measurements of conserved quantities sensitive to dynamical fluctuations**

# quark-gluon plasma and hadron yields in central nuclear collisions

QCD implies duality between (quarks and gluons) – hadrons

hadron gas is equilibrated state of all known hadrons

QGP is equilibrated state of deconfined quarks and gluons

at a critical temperature  $T_c$  a hadronic system converts to QGP

consequence:

QGP in central nuclear collisions if:

1. all hadrons in **equilibrium state** at common temperature  $T$
2. as function of cm energy the hadron state must reach a **limiting temperature**  $T_{lim}$
3. all hadron yields must agree with predictions using the **full QCD partition function** at the QCD critical temperature  $T_c = T_{lim}$

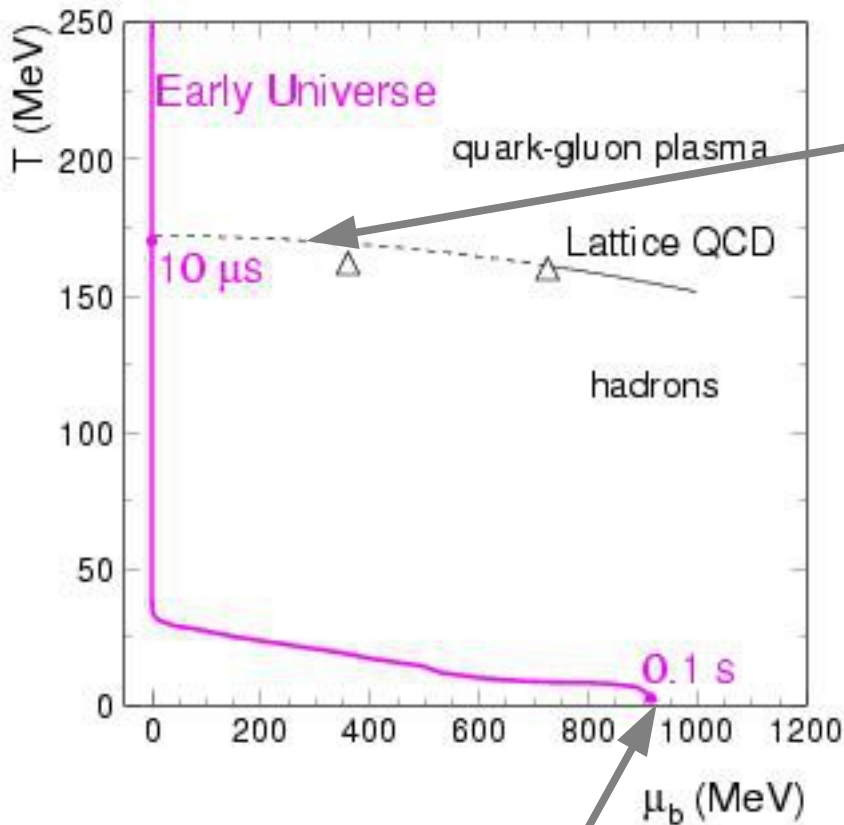
# The size of loosely bound molecular objects

Examples: deuteron, hypertriton, XYZ 'charmonium states, molecules near Feshbach resonances in cold quantum gases

Quantum mechanics predicts that a bound state that is sufficiently close to a 2-body threshold and that couples to that threshold through a short-range S-wave interaction has universal properties that depend only on its binding energy. Such a bound state is necessarily a loosely-bound molecule in which the constituents are almost always separated by more than the range. One of the universal predictions is that the root-mean-square (rms) separation of the constituents is  $(4\mu E_X)^{-1/2}$ , where  $E_X$  is the binding energy of the resonance and  $\mu$  is the reduced mass of the two constituents. As the binding energy is tuned to zero, the size of the molecule increases without bound. A classic example of a loosely-bound S-wave molecule is the deuteron, which is a bound state of the proton and neutron with binding energy 2.2 MeV. The proton and neutron are correctly predicted to have a large rms separation of about 3.1 fm.

Artoisenet and Braaten,  
arXiv:1007.2868

# evolution of the early universe and the QCD phase diagram



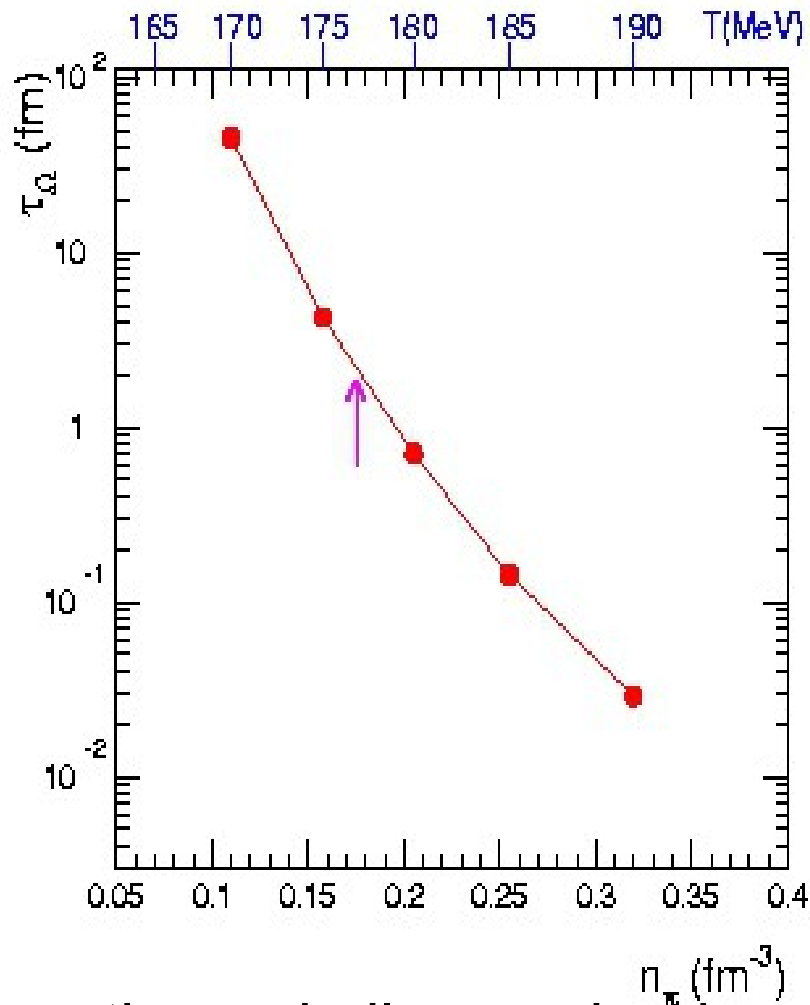
QCD phase boundary

homogeneous Universe in equilibrium, this matter can only be investigated in nuclear collisions

- charge neutrality
- net lepton number = net baryon number
- constant entropy/baryon

neutrinos decouple and light nuclei begin to be formed

# The QGP phase transition drives chemical equilibration for small $\beta_b$

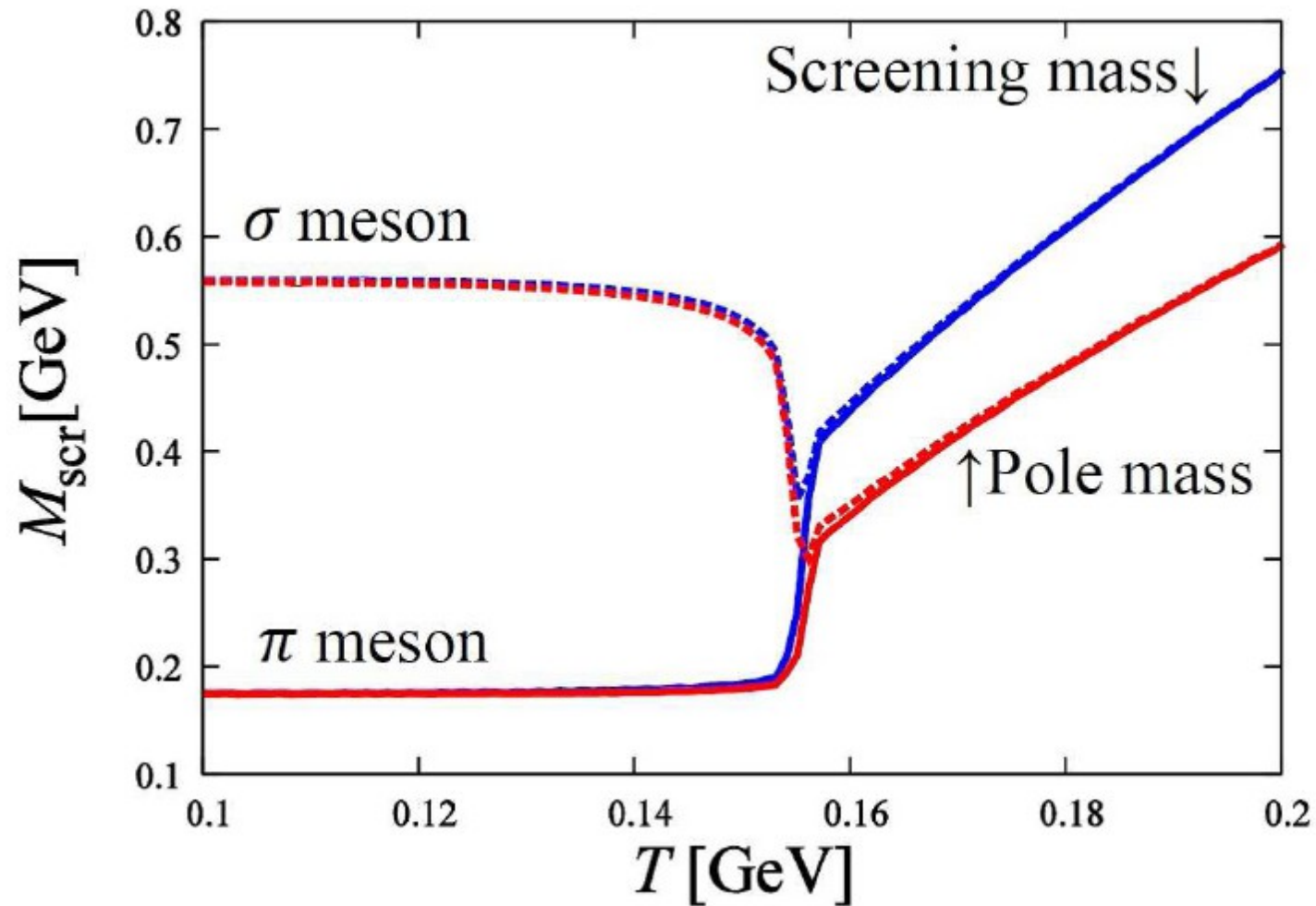


are there similar mechanisms for large  $\beta_b$ ?

- Near phase transition particle density varies rapidly with  $T$ .
- For small  $\beta_b$ , reactions such as  $KKK \rightarrow \bar{N}_{\text{bar}}$  bring multi-strange baryons close to equilibrium.
- Equilibration time  $\propto T^{-60}$ !
- All particles freeze out within the same very narrow temperature window.

pbm, J. Stachel, C. Wetterich  
 Phys. Lett. B596 (2004) 61  
 nucl-th/0311005

# temperature dependence of meson masses in a NJL model



Mesonic correlation functions at finite temperature and density in the Nambu-Jona-Lasinio model with a Polyakov loop

H. Hansen, W.M. Alberico (INFN, Turin & Turin U.), A. Beraudo (Saclay, SPhT), A. Molinari, M. Nardi (INFN, Turin & Turin U.), C. Ratti (ECT, Trento & INFN, Trento). Sep 2006. 26 pp.

Published in Phys.Rev. D75 (2007) 065004